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# Scalar and Vector Leptoquark Pair Production in $e^+e^-$ and $\gamma\gamma$ Collisions

Johannes Blümlein

DESY

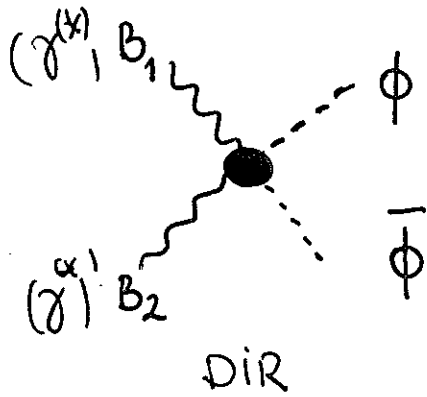
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# 1 Introduction

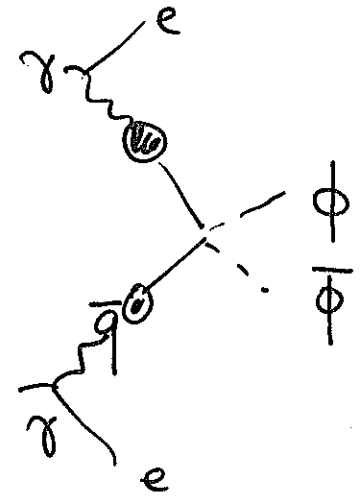
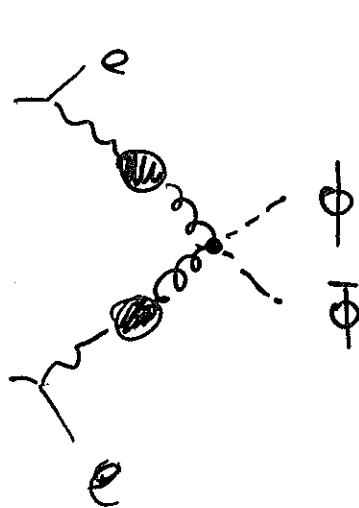
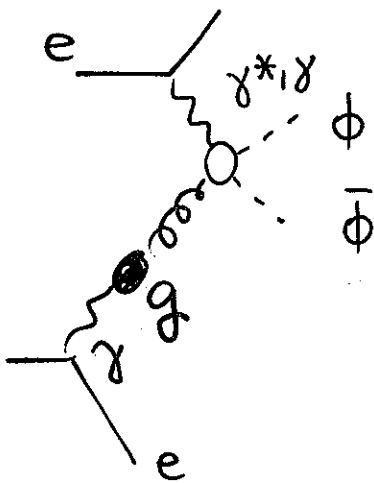
## WHY LQ PAIR PRODUCTION ?

- SINGLE PRODUCTION (real or virtual) :

$$\sigma \propto \lambda_{lq}^2 \ll e^2, M \lesssim 1 \dots 2 \text{TeV.}$$



ONLY GAUGE COUPLINGS  
& ANOMALOUS COUPLINGS  
(IV)



SCALARS: DIRECT MASS LIMITS

VECTORS: MASS LIMITS AND LIMITS ON  
 $K_{A,G}$  ;  $\lambda_{A,G}$

## 2 Basic Notation

$$\mathcal{L} = \mathcal{L}_S^g + \mathcal{L}_V^g, \quad (2)$$

$$\mathcal{L}_S^g = \sum_{\text{scalar}_s} \left[ (D_{ij}^\mu \Phi^j)^\dagger (D_\mu^{ik} \Phi_k) - M_S^2 \Phi^{i\dagger} \Phi_i \right], \quad (3)$$

$$\mathcal{L}_V^g = \sum_{\text{vector}_s} \left\{ -\frac{1}{2} G_{\mu\nu}^{i\dagger} G_i^{\mu\nu} + M_V^2 \Phi_\mu^{i\dagger} \Phi_i^\mu - i g_s \left[ (1 - \kappa_G) \Phi_\mu^{i\dagger} t_{ij}^a \Phi_\nu^j G_a^{\mu\nu} + \frac{\lambda_G}{M_V^2} G_{\sigma\mu}^{i\dagger} t_{ij}^a G_\nu^{j\mu} G_a^{\nu\sigma} \right] \right\}. \quad (4)$$

$$\begin{aligned} G_{\mu\nu}^a &= \partial_\mu \mathcal{A}_\nu^a - \partial_\nu \mathcal{A}_\mu^a + g_s f^{abc} \mathcal{A}_{\mu b} \mathcal{A}_{\nu c}, \\ G_{\mu\nu}^{ri} &= D_\mu^{ik} \Phi_{\nu k} - D_\nu^{ik} \Phi_{\mu k}, \end{aligned} \quad (5)$$

$$D_\mu^{ij} = \partial_\mu \delta^{ij} - i g_s t_a^{ij} \mathcal{A}_\mu^a. \quad (6)$$

$$\begin{aligned} \mu_{\Phi, G} &= \frac{g_s}{2M_\Phi} (2 - \kappa_G + \lambda_G), \\ q_{\Phi, G} &= -\frac{g_s}{M_\Phi^2} (1 - \kappa_G - \lambda_G). \end{aligned} \quad (7)$$

### 3 Production Cross Sections

$$\sigma \equiv [\gamma\gamma] \oplus [\gamma g] \oplus [gg + q\bar{q}]$$

For  $\gamma\gamma$  scattering three terms contribute to the cross section: the direct process  $\gamma\gamma \rightarrow \Phi\bar{\Phi}$ ,  $\sigma_{dir}$ , a term in which one of the photons is resolved and the second couples directly to the leptons,  $\sigma_{dir/res}$ , and the resolved contribution,  $\sigma_{res}$ ,

$$\sigma_{S,V}^{\gamma\gamma,tot} = \sigma_{S,V}^{\gamma\gamma,dir} + \sigma_{S,V}^{\gamma\gamma,dir/res} + \sigma_{S,V}^{\gamma\gamma,res}. \quad (51)$$

The third term (eq. (56)) is charge independent, but the first and the second terms behave  $\propto Q_\Phi^4$  and  $\propto Q_\Phi^2$ , respectively. The cross section for the direct contribution reads [11]

$$\sigma_{S,V}^{\gamma\gamma,dir}(s, M_\Phi) = \int_{y_{min}/y_{max}}^{y_{max}} dy_1 \int_{y_{min}/y_1}^{y_{max}} dy_2 \Phi_{\gamma/e}(y_1) \Phi_{\gamma/e}(y_2) \hat{\sigma}_{S,V}^{dir}(\hat{s}, M_\Phi) \theta(\hat{s} - 4M_\Phi^2). \quad (52)$$

Here the subsystem cross sections are:

$$\hat{\sigma}_{S,V}^{dir}(\hat{s}, M_\Phi) = \frac{\pi\alpha^2}{\hat{s}} Q_\Phi^4 N_c R_{S,V}^*(\hat{s}, M_\Phi), \quad (53)$$

with  $\hat{s} = y_1 y_2 S$ ,  $S = 4E_{e^+} E_{e^-}$ , and

$$\begin{aligned} R_S^* &= 2R_S, \\ R_V^* &= 2 \sum_{j=0}^{20} \chi_j^*(\kappa_A, \kappa_A, \lambda_A, \lambda_A) \bar{H}_j(\hat{s}, \beta). \end{aligned} \quad K_A, \lambda_A \quad (54)$$

$$\begin{aligned} \sigma_{S,V}^{\gamma\gamma,dir/res}(s, M_\Phi) &= 2 \int_{y_{min}/y_{max}}^{y_{max}} dy_1 \int_{y_{min}/y_1}^{y_{max}} dy_2 \int_{4M_\Phi^2/S y_1 y_2}^1 dz \Phi_{\gamma/e}(y_1) \Phi_{\gamma/e}(y_2) G_\gamma(z, \mu) \\ &\times \hat{\sigma}_{S,V}^{g\gamma}(\hat{s}, M_\Phi) \theta(\hat{s} - 4M_\Phi^2). \end{aligned} \quad K_A, \lambda_A, K_G, \lambda_G \quad (55)$$

with  $\mu$  the factorization scale. Note that due to the smallness of the couplings  $\lambda_{i,q} \ll e$  only the subprocess due to gluon-photon fusion contributes.

The double-resolved contribution reads:

$$\begin{aligned} \sigma_{S,V}^{\gamma\gamma,res}(s, M_\Phi) &= \int_{y_{min}/y_{max}}^{y_{max}} dy_1 \int_{y_{min}/y_1}^{y_{max}} dy_2 \int_{4M_\Phi^2/S y_1 y_2}^1 dz_1 \int_{4M_\Phi^2/S y_1 y_2 z_1}^1 dz_2 \Phi_{\gamma/e}(y_1) \Phi_{\gamma/e}(y_2) \\ &\times \left\{ \sum_{f=1}^{N_f} [q_f^\gamma(z_1, \mu_1) \bar{q}_f^\gamma(z_2, \mu_2) + \bar{q}_f^\gamma(z_1, \mu_1) q_f^\gamma(z_2, \mu_2)] \hat{\sigma}_{S,V}^g(\hat{s}, M_\Phi) \right. \\ &\left. + G^\gamma(z_1, \mu_1) G^\gamma(z_2, \mu_2) \hat{\sigma}_{S,V}^g(\hat{s}, M_\Phi) \right\} \theta(\hat{s} - 4M_\Phi^2). \end{aligned} \quad K_G, \lambda_G \quad (56)$$

## Scalar Leptoquarks

The differential and integral pair production cross sections for  $gg$  and  $q\bar{q}$  scattering are

$$\frac{d\hat{\sigma}_{S\bar{S}}^{gg}}{d\cos\theta} = \frac{\pi\alpha_s^2}{6\hat{s}}\beta \left\{ \frac{1}{32} [25 + 9\beta^2 \cos^2\theta - 18\beta^2] - \frac{1}{16} \frac{(25 - 34\beta^2 + 9\beta^4)}{1 - \beta^2 \cos^2\theta} + \frac{(1 - \beta^2)^2}{(1 - \beta^2 \cos^2\theta)^2} \right\}, \quad (17)$$

$$\hat{\sigma}_{S\bar{S}}^{gg} = \frac{\pi\alpha_s^2}{96\hat{s}} \left\{ \beta (41 - 31\beta^2) - (17 - 18\beta^2 + \beta^4) \log \left| \frac{1 + \beta}{1 - \beta} \right| \right\}, \quad (18)$$

and

$$\frac{d\hat{\sigma}_{S\bar{S}}^{q\bar{q}}}{d\cos\theta} = \frac{\pi\alpha_s^2}{18\hat{s}}\beta^3 \sin^2\theta, \quad (19)$$

$$\hat{\sigma}_{S\bar{S}}^{q\bar{q}} = \frac{2\pi\alpha_s^2}{27\hat{s}}\beta^3, \quad (20)$$

## Vector Leptoquarks

The differential and integral pair production cross sections for  $gg$  scattering are

$$\frac{d\hat{\sigma}_{V\bar{V}}^{gg}}{d\cos\theta} = \frac{\pi\alpha_s^2}{192\hat{s}}\beta \sum_{i=0}^{14} \chi_i^g(\kappa_G, \lambda_G) \frac{F_i(\hat{s}, \beta, \cos\theta)}{(1 - \beta^2 \cos^2\theta)^2}, \quad (21)$$

with

$$\begin{aligned} \sum_{i=0}^{14} \chi_i^g(\kappa_G, \lambda_G) F_i &= F_0 + \kappa_G F_1 + \lambda_G F_2 + \kappa_G^2 F_3 + \kappa_G \lambda_G F_4 \\ &\quad \lambda_G^2 F_5 + \kappa_G^3 F_6 + \kappa_G^2 \lambda_G F_7 + \kappa_G \lambda_G^2 F_8 + \lambda_G^3 F_9 \\ &\quad \kappa_G^4 F_{10} + \kappa_G^3 \lambda_G F_{11} + \kappa_G^2 \lambda_G^2 F_{12} + \kappa_G \lambda_G^3 F_{13} + \lambda_G^4 F_{14}, \end{aligned} \quad (22)$$

$$\hat{\sigma}_{V\bar{V}}^{gg} = \frac{\pi\alpha_s^2}{96M_V^2} \sum_{i=0}^{14} \chi_i(\kappa_G, \lambda_G) \tilde{F}_i(\hat{s}, \beta), \quad (23)$$

$$\tilde{F}_i = \frac{M_V^2}{\hat{s}} \int_0^\beta d\xi \frac{F_i(\xi = \beta \cos\theta)}{(1 - \xi^2)^2}. \quad (24)$$

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and

$$\hat{\sigma}_s(\hat{s}, \beta) = \frac{\pi\alpha^2}{\hat{s}} Q_*^4 N_c \left\{ 2(2 - \beta^2)\beta - (1 - \beta^4) \log \left| \frac{1 + \beta}{1 - \beta} \right| \right\} \quad (25)$$

where  $N_c = 3$ . Numerical results have been derived for the case of a  $\gamma\gamma$  collider operating at  $\sqrt{s} = 500$  GeV in [13]. As seen in figure 13 only leptoquarks with large charges can be pair produced at a sufficient rate in this reaction.

In [21] single production of scalar leptoquarks is considered for  $\gamma\gamma$  fusion via  $\gamma\gamma \rightarrow \bar{l}qS$ . At typical luminosities the search limits reach 0.8 to  $0.9\sqrt{s}$  for  $M_s$ .

0.2. Vector Leptoquarks

The differential and integral production cross section for vector leptoquarks are

$$\frac{d\hat{\sigma}_v}{d\cos\theta} = \frac{\pi\alpha^2}{\hat{s}} Q_*^4 N_c \sum_{j=0}^{14} \chi_j \frac{F_j(\hat{s}, \beta, \cos\theta)}{(1 - \beta^2 \cos^2\theta)^2} \quad (26)$$

with  $\chi_j = \chi_j(\kappa_\lambda, \lambda_\lambda)$  and

$$\begin{aligned} \sum_{j=0}^{14} \chi_j F_j &= F_0 + \kappa_\lambda F_1 \\ + \kappa_\lambda^2 F_2 &+ \kappa_\lambda^3 F_3 + \kappa_\lambda^4 F_4 \\ + \lambda_\lambda F_5 &+ \lambda_\lambda^2 F_6 + \lambda_\lambda^3 F_7 \\ + \lambda_\lambda^4 F_8 &+ \kappa_\lambda \lambda_\lambda F_9 + \kappa_\lambda \lambda_\lambda^2 F_{10} \\ + \kappa_\lambda \lambda_\lambda^3 F_{11} &+ \kappa_\lambda^2 \lambda_\lambda F_{12} + \kappa_\lambda^3 \lambda_\lambda F_{13} \\ + \kappa_\lambda^2 \lambda_\lambda^2 F_{14} & \end{aligned}$$

and

$$\hat{\sigma}_v = \frac{2\pi\alpha^2}{M_*^2} Q_*^4 N_c \sum_{j=0}^{14} \chi_j(\kappa_\lambda, \lambda_\lambda) \bar{F}_j(\hat{s}, \beta) \quad (27)$$

with

$$\bar{F}_j = \frac{M_*^2}{\hat{s}} \int_0^\beta d\xi \frac{F_j(\xi = \beta \cos\theta)}{(1 - \xi^2)^2} \quad (28)$$

Eq. (26) agrees analytically with a result obtained in [28]. The functions  $F_j(\hat{s}, \beta, \cos\theta)$  are not given here but can be obtained as linear combinations from relations given in eqs. (12,13) and (17) in [9].

$$\bar{F}_0 = \beta \left( \frac{11}{2} - \frac{9}{4}\beta^2 + \frac{3}{4}\beta^4 \right)$$

$$- \frac{3}{8} (1 - \beta^2 - \beta^4 + \beta^6) \ln \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_1 = -8\beta - \frac{3}{2} (1 - \beta^2) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_2 = 3\beta + \frac{1}{4}\beta \frac{\hat{s}}{M_*^2} + \left( \frac{7}{2} - 2\beta^2 \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_3 = -\frac{1}{4}\beta \frac{\hat{s}}{M_*^2} + \left( -2 + \frac{3}{4}\beta^2 \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_4 = -\frac{1}{96}\beta + \frac{5}{48}\beta \frac{\hat{s}}{M_*^2} + \frac{4 - \beta^2}{16} \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_5 = -(1 - \beta^2) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_6 = -\frac{1}{6}\beta + \frac{17}{12}\beta \frac{\hat{s}}{M_*^2}$$

$$+ \left( -3 - \frac{\beta^2}{2} + \frac{1}{2} \frac{\hat{s}}{M_*^2} \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_7 = -\beta + \frac{11}{6}\beta \frac{\hat{s}}{M_*^2} - \frac{1}{3}\beta \frac{\hat{s}^2}{M_*^4}$$

$$- \frac{3 + \beta^2}{4} \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_8 = -\frac{1}{96}\beta + \frac{59}{80}\beta \frac{\hat{s}}{M_*^2} - \frac{113}{320}\beta \frac{\hat{s}^2}{M_*^4} + \frac{43}{960}\beta \frac{\hat{s}^3}{M_*^6}$$

$$+ \left( -\frac{1}{2} - \frac{1}{16}\beta^2 + \frac{1}{8} \frac{\hat{s}}{M_*^2} \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_9 = 2\beta + (2 + \beta^2) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_{10} = 2\beta - \frac{7}{3}\beta \frac{\hat{s}}{M_*^2}$$

$$+ \left( 3 + \frac{5}{4}\beta^2 - \frac{1}{2} \frac{\hat{s}}{M_*^2} \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_{11} = \frac{1}{24}\beta - \frac{59}{48}\beta \frac{\hat{s}}{M_*^2} + \frac{5}{32}\beta \frac{\hat{s}^2}{M_*^4}$$

$$+ \frac{5 + \beta^2}{4} \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_{12} = -\beta - \frac{1}{2}\beta \frac{\hat{s}}{M_*^2}$$

$$+ \left( -\frac{1}{4} - \frac{7}{4}\beta^2 \right) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

$$\bar{F}_{13} = \frac{1}{24}\beta + \frac{1}{3}\beta \frac{\hat{s}}{M_*^2} - \frac{1}{4} (1 - \beta^2) \log \left| \frac{1 + \beta}{1 - \beta} \right|$$

## Appendix

The functions  $F_i(\xi, \beta, \cos\theta)$  of (12) are:

$$F_0 = 19 - 6\beta^2 + 6\beta^4 + (16 - 6\beta^2)\beta^2 \cos^2\theta + 3\beta^4 \cos^4\theta,$$

$$F_1 = -22 - 10\beta^2 \cos^2\theta,$$

$$F_2 = 4 + \frac{\xi}{M_\Phi^2} \frac{1 - \beta^4 \cos^4\theta}{2} + \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{16},$$

$$F_3 = 28 + 4\beta^2 \cos^2\theta + \frac{\xi}{M_\Phi^2} \beta^2 \cos^2\theta (1 - \beta^2 \cos^2\theta) + \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{8},$$

$$F_4 = -5 + \beta^2 \cos^2\theta + \frac{\xi}{M_\Phi^2} \frac{-3 + \beta^2 \cos^2\theta + 2\beta^4 \cos^4\theta}{4} - \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{8},$$

$$F_5 = \frac{3 - \beta^2 \cos^2\theta}{4} + \frac{\xi}{M_\Phi^2} \frac{5 - 4\beta^2 \cos^2\theta - \beta^4 \cos^4\theta}{16} + \frac{\xi^2}{M_\Phi^4} \frac{13 - 25\beta^2 \cos^2\theta + 11\beta^4 \cos^4\theta + \beta^6 \cos^6\theta}{128},$$

$$F_6 = -4 + 4\beta^2 \cos^2\theta,$$

$$F_7 = 4 + \frac{\xi}{M_\Phi^2} \frac{-7 + 8\beta^2 \cos^2\theta - \beta^4 \cos^4\theta}{2} + \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{2} + \frac{\xi^3}{M_\Phi^6} \frac{(1 - \beta^2 \cos^2\theta)^3}{16},$$

$$F_8 = -\frac{\xi}{M_\Phi^2} (1 - \beta^2 \cos^2\theta) + \frac{\xi^2}{M_\Phi^4} \frac{11 - 13\beta^2 \cos^2\theta + \beta^4 \cos^4\theta + \beta^6 \cos^6\theta}{8} - \frac{\xi^3}{M_\Phi^6} \frac{(1 - \beta^2 \cos^2\theta)^3}{8},$$

$$F_9 = 1 - \beta^2 \cos^2\theta + \frac{\xi}{M_\Phi^2} \frac{-3 + 4\beta^2 \cos^2\theta - \beta^4 \cos^4\theta}{2} + \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{2} + \frac{\xi^3}{M_\Phi^6} \frac{-3 + 7\beta^2 \cos^2\theta - 5\beta^4 \cos^4\theta + \beta^6 \cos^6\theta}{16},$$

$$F_{10} = \frac{3 - \beta^2 \cos^2\theta}{4} + \frac{\xi}{M_\Phi^2} \frac{-19 + 20\beta^2 \cos^2\theta - \beta^4 \cos^4\theta}{16} + \frac{\xi^2}{M_\Phi^4} \frac{141 - 249\beta^2 \cos^2\theta + 107\beta^4 \cos^4\theta + \beta^6 \cos^6\theta}{128}$$

$$+ \frac{\xi^3}{M_\Phi^6} \frac{-53 + 119\beta^2 \cos^2\theta - 79\beta^4 \cos^4\theta + 13\beta^6 \cos^6\theta}{128} + \frac{\xi^4}{M_\Phi^8} \frac{27 - 68\beta^2 \cos^2\theta + 58\beta^4 \cos^4\theta - 20\beta^6 \cos^6\theta + 3\beta^8 \cos^8\theta}{512},$$

$$F_{11} = -8 + \frac{\xi}{M_\Phi^2} (3 - 4\beta^2 \cos^2\theta + \beta^4 \cos^4\theta),$$

$$F_{12} = \frac{\xi}{M_\Phi^2} (2 - 3\beta^2 \cos^2\theta + 4\beta^4 \cos^4\theta),$$

$$F_{13} = -2(1 - \beta^2 \cos^2\theta) + \frac{\xi}{M_\Phi^2} \frac{9 - 13\beta^2 \cos^2\theta + 4\beta^4 \cos^4\theta}{4} - \frac{\xi^2}{M_\Phi^4} \frac{2 - 3\beta^2 \cos^2\theta + \beta^4 \cos^4\theta}{2} + \frac{\xi^3}{M_\Phi^6} \frac{(1 - \beta^2 \cos^2\theta)^3}{16},$$

$$F_{14} = -5 + \beta^2 \cos^2\theta + \frac{\xi}{M_\Phi^2} \frac{7 - 8\beta^2 \cos^2\theta + \beta^4 \cos^4\theta}{2} - \frac{\xi^2}{M_\Phi^4} \frac{(1 - \beta^2 \cos^2\theta)^2}{16} - \frac{\xi^3}{M_\Phi^6} \frac{(1 - \beta^2 \cos^2\theta)^3}{16},$$

$$F_{15} = \frac{3 - \beta^2 \cos^2\theta}{2} + \frac{\xi}{M_\Phi^2} \frac{13 - 14\beta^2 \cos^2\theta + \beta^4 \cos^4\theta}{8} - \frac{\xi^2}{M_\Phi^4} \frac{41 - 81\beta^2 \cos^2\theta + 30\beta^4 \cos^4\theta + \beta^6 \cos^6\theta}{64} + \frac{\xi^3}{M_\Phi^6} \frac{11 - 25\beta^2 \cos^2\theta + 17\beta^4 \cos^4\theta - 3\beta^6 \cos^6\theta}{128},$$

$$F_{16} = 1 - \beta^2 \cos^2\theta - \frac{\xi}{M_\Phi^2} \frac{3 - 5\beta^2 \cos^2\theta + 2\beta^4 \cos^4\theta}{4},$$

$$F_{17} = \frac{3 - \beta^2 \cos^2\theta}{4} - \frac{\xi}{M_\Phi^2} \frac{7 - 8\beta^2 \cos^2\theta + \beta^4 \cos^4\theta}{16} - \frac{\xi^2}{M_\Phi^4} \frac{3 - 7\beta^2 \cos^2\theta + 5\beta^4 \cos^4\theta - \beta^6 \cos^6\theta}{128} + \frac{\xi^3}{M_\Phi^6} \frac{(1 - \beta^2 \cos^2\theta)^3}{32},$$

[78] dir

20 fets.

$$\begin{aligned}
 F_{18} &= 2(5 - \beta^2 \cos^2 \theta) - \frac{s}{M_\phi^2} \frac{11 - 15\beta^2 \cos^2 \theta + 4\beta^4 \cos^4 \theta}{4} \\
 &\quad - \frac{s^2 (1 - \beta^2 \cos^2 \theta)^2}{4M_\phi^4}, \\
 F_{19} &= 3 - \beta^2 \cos^2 \theta - \frac{s}{M_\phi^2} \frac{7 - 8\beta^2 \cos^2 \theta + \beta^4 \cos^4 \theta}{4} \\
 &\quad + \frac{s^2}{M_\phi^4} \frac{11 - 13\beta^2 \cos^2 \theta + \beta^4 \cos^4 \theta + \beta^6 \cos^6 \theta}{32} \\
 &\quad + \frac{s^3}{M_\phi^6} \frac{5 - 7\beta^2 \cos^2 \theta - \beta^4 \cos^4 \theta + 3\beta^6 \cos^6 \theta}{128}, \\
 F_{20} &= -\frac{3 - \beta^2 \cos^2 \theta}{2} + \frac{s}{M_\phi^2} \frac{(1 - \beta^2 \cos^2 \theta)^2}{8} \\
 &\quad + \frac{s^2}{M_\phi^4} \frac{11 - 23\beta^2 \cos^2 \theta + 13\beta^4 \cos^4 \theta - \beta^6 \cos^6 \theta}{64}.
 \end{aligned}
 \tag{A.1}$$

The functions  $\bar{F}_i(s, \beta)$ , which describe the different contributions to the integrated cross-section (13), are:

$$\begin{aligned}
 \bar{F}_0 &= \beta \left( \frac{11}{2} - \frac{9}{4}\beta^2 + \frac{3}{4}\beta^4 \right) - \frac{3}{8} (1 - \beta^2 - \beta^4 + \beta^6) \ln \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_1 &= -4\beta - \frac{3}{4} (1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_2 &= \frac{1}{16} \beta \frac{s}{M_\phi^2} + \frac{3 - \beta^2}{4} \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_3 &= 3\beta + \frac{1}{8} \beta \frac{s}{M_\phi^2} + \left( 2 - \frac{3}{2}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_4 &= -\frac{1}{8} \beta \frac{s}{M_\phi^2} + \left( -1 + \frac{3}{8}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_5 &= -\frac{1}{96} \beta + \frac{5}{48} \beta \frac{s}{M_\phi^2} + \frac{4 - \beta^2}{16} \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_6 &= -\frac{1}{2} (1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right|,
 \end{aligned}$$

$$\begin{aligned}
 \bar{F}_7 &= \frac{7}{12} \beta \frac{s}{M_\phi^2} + \frac{1}{24} \beta \frac{s^2}{M_\phi^4} - \frac{5 + \beta^2}{4} \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_8 &= -\frac{1}{6} \beta + \frac{1}{4} \beta \frac{s}{M_\phi^2} - \frac{1}{12} \beta \frac{s^2}{M_\phi^4} + \left( -\frac{1}{2} + \frac{1}{2} \frac{s}{2M_\phi^2} \right) \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_9 &= -\frac{1}{2} \beta + \frac{11}{12} \beta \frac{s}{M_\phi^2} - \frac{1}{6} \beta \frac{s^2}{M_\phi^4} - \frac{3 + \beta^2}{8} \log \left| \frac{1+\beta}{1-\beta} \right|, \\
 \bar{F}_{10} &= -\frac{1}{96} \beta + \frac{59}{80} \beta \frac{s}{M_\phi^2} - \frac{113}{320} \beta \frac{s^2}{M_\phi^4} + \frac{43}{960} \beta \frac{s^3}{M_\phi^6} \\
 &\quad + \left( -\frac{1}{2} - \frac{1}{16} \beta^2 + \frac{1}{8} \frac{s}{M_\phi^2} \right) \log \left| \frac{1+\beta}{1-\beta} \right|,
 \end{aligned}$$

$$\bar{F}_{11} = \frac{1}{2} (1 + \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{12} = \beta + \frac{1}{2} \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{13} = \beta - \frac{5}{12} \beta \frac{s}{M_\phi^2} + \frac{1}{24} \beta \frac{s^2}{M_\phi^4} + \left[ -\frac{1}{4} \frac{s}{M_\phi^2} + \left( \frac{3}{8} + \frac{1}{4} \beta^2 \right) \right] \log \left| \frac{1+\beta}{1-\beta} \right|, \tag{A.2}$$

$$\bar{F}_{14} = -\frac{11}{24} \beta \frac{s}{M_\phi^2} - \frac{1}{24} \beta \frac{s^2}{M_\phi^4} + \frac{9 + 3\beta^2}{8} \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{15} = \frac{1}{48} \beta - \frac{59}{96} \beta \frac{s}{M_\phi^2} + \frac{5}{64} \beta \frac{s^2}{M_\phi^4} + \frac{5 + \beta^2}{8} \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{16} = -\frac{1}{2} \beta - \frac{1}{8} \beta^2 \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{17} = -\frac{1}{96} \beta + \frac{1}{48} \beta \frac{s}{M_\phi^2} + \frac{1}{48} \beta \frac{s^2}{M_\phi^4} - \frac{2 + \beta^2}{16} \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{18} = -\frac{1}{4} \beta \frac{s}{M_\phi^2} - \frac{1 - 6\beta^2}{8} \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{19} = -\frac{1}{24} \beta + \frac{7}{96} \beta \frac{s}{M_\phi^2} + \frac{3}{64} \beta \frac{s^2}{M_\phi^4} + \left[ \frac{1}{8} \frac{s}{M_\phi^2} - \frac{2 + \beta^2}{4} \right] \log \left| \frac{1+\beta}{1-\beta} \right|,$$

$$\bar{F}_{20} = \frac{1}{48} \beta + \frac{1}{6} \beta \frac{s}{M_\phi^2} - \frac{1}{8} (1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right|.$$



## B Coefficients of the production cross section of vector leptoquarks

The functions  $F_i(\hat{s}, \beta, \cos \theta)$  of (21) which determine the differential pair production cross section for  $gg \rightarrow V\bar{V}$  are:  $[gg]_{rr} : 14 \text{ fets.}$

$$F_0 = \left[ 19 - 6\beta^2 + 6\beta^4 + (16 - 6\beta^2) \beta^2 \cos^2 \theta + 3\beta^4 \cos^4 \theta \right] \cdot (7 + 9\beta^2 \cos^2 \theta) \quad (85)$$

$$F_1 = -4 \cdot (77 + 143\beta^2 \cos^2 \theta + 36\beta^4 \cos^4 \theta) \quad (86)$$

$$F_2 = -8 \cdot (7 + 11\beta^2 \cos^2 \theta - 18\beta^4 \cos^4 \theta) \quad (87)$$

$$F_3 = 2 \cdot (117 + 185\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) + 2 \frac{\hat{s}}{M_\star^2} (8 - \beta^2 \cos^2 \theta - 7\beta^4 \cos^4 \theta) + \frac{7}{4} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta)^2 \quad (88)$$

$$F_4 = -4 \cdot (19 + 27\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) + 10 \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (7 - \beta^2 \cos^2 \theta) \quad (89)$$

$$F_5 = 2 \cdot (19 + 27\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) - \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (65 + 29\beta^2 \cos^2 \theta) + \frac{1}{8} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta) (97 + 2\beta^2 \cos^2 \theta - 115\beta^4 \cos^4 \theta) + \frac{\hat{s}^3}{M_\star^6} \frac{9}{4} (1 - \beta^2 \cos^2 \theta)^3 \quad (90)$$

$$F_6 = -61 - 67\beta^2 \cos^2 \theta - \frac{1}{2} \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (39 + 14\beta^2 \cos^2 \theta) - \frac{7}{4} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta)^2 \quad (91)$$

$$F_7 = 127 + 129\beta^2 \cos^2 \theta - \frac{1}{2} \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (89 + 3\beta^2 \cos^2 \theta) + \frac{1}{4} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta)^2 (-23 + 18\beta^2 \cos^2 \theta) \quad (92)$$

$$F_8 = -71 - 57\beta^2 \cos^2 \theta + \frac{1}{2} \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (170 + 21\beta^2 \cos^2 \theta) + \frac{1}{4} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta) (-59 + 40\beta^2 \cos^2 \theta + 27\beta^4 \cos^4 \theta) - \frac{9}{4} \frac{\hat{s}^3}{M_\star^6} (1 - \beta^2 \cos^2 \theta)^3 \quad (93)$$

$$F_9 = 5 (1 - \beta^2 \cos^2 \theta) - \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (21 + 2\beta^2 \cos^2 \theta) + \frac{1}{4} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta)^2 (74 + 9\beta^2 \cos^2 \theta) + \frac{1}{4} \frac{\hat{s}^3}{M_\star^6} (1 - \beta^2 \cos^2 \theta)^2 (-15 + 8\beta^2 \cos^2 \theta) \quad (94)$$

$$F_{10} = 3 + 5\beta^2 \cos^2 \theta + \frac{5}{4} \frac{\hat{s}}{M_\star^2} (1 - \beta^2 \cos^2 \theta) (4 - \beta^2 \cos^2 \theta) + \frac{1}{32} \frac{\hat{s}^2}{M_\star^4} (1 - \beta^2 \cos^2 \theta)^2 (25 + 13\beta^2 \cos^2 \theta) \quad (95)$$

$$\begin{aligned}
F_{11} &= -4 \cdot (3 + 5\beta^2 \cos^2 \theta) - 5 \frac{\hat{s}}{M_\Phi^2} (1 - \beta^2 \cos^2 \theta)^2 \\
&+ \frac{1}{8} \frac{\hat{s}^2}{M_\Phi^4} (1 - \beta^2 \cos^2 \theta)^2 (35 - 13\beta^2 \cos^2 \theta)
\end{aligned} \tag{96}$$

$$\begin{aligned}
F_{12} &= 6 \cdot (3 + 5\beta^2 \cos^2 \theta) - \frac{15}{2} \frac{\hat{s}}{M_\Phi^2} (1 - \beta^2 \cos^2 \theta) (2 + \beta^2 \cos^2 \theta) \\
&+ \frac{1}{16} \frac{\hat{s}^2}{M_\Phi^4} (1 - \beta^2 \cos^2 \theta) (-23 + 54\beta^2 \cos^2 \theta - 39\beta^4 \cos^4 \theta) \\
&+ \frac{1}{64} \frac{\hat{s}^3}{M_\Phi^6} (1 - \beta^2 \cos^2 \theta)^2 (113 - 49\beta^2 \cos^2 \theta)
\end{aligned} \tag{97}$$

$$\begin{aligned}
F_{13} &= -4 \cdot (3 + 5\beta^2 \cos^2 \theta) + 5 \frac{\hat{s}}{M_\Phi^2} (1 - \beta^2 \cos^2 \theta) (5 + \beta^2 \cos^2 \theta) \\
&- \frac{1}{8} \frac{\hat{s}^2}{M_\Phi^4} (1 - \beta^2 \cos^2 \theta)^2 (119 + 13\beta^2 \cos^2 \theta) \\
&+ \frac{1}{32} \frac{\hat{s}^3}{M_\Phi^6} (1 - \beta^2 \cos^2 \theta)^2 (79 - 15\beta^2 \cos^2 \theta)
\end{aligned} \tag{98}$$

$$\begin{aligned}
F_{14} &= 3 + 5\beta^2 \cos^2 \theta - \frac{5}{4} \frac{\hat{s}}{M_\Phi^2} (1 - \beta^2 \cos^2 \theta) (8 + \beta^2 \cos^2 \theta) \\
&+ \frac{1}{32} \frac{\hat{s}^2}{M_\Phi^4} (1 - \beta^2 \cos^2 \theta) (321 - 324\beta^2 \cos^2 \theta - 13\beta^4 \cos^4 \theta) \\
&+ \frac{11}{64} \frac{\hat{s}^3}{M_\Phi^6} (1 - \beta^2 \cos^2 \theta)^2 (-23 + 7\beta^2 \cos^2 \theta) \\
&+ \frac{1}{256} \frac{\hat{s}^4}{M_\Phi^8} (1 - \beta^2 \cos^2 \theta)^2 (135 - 22\beta^2 \cos^2 \theta + 15\beta^4 \cos^4 \theta).
\end{aligned} \tag{99}$$

The coefficients  $\bar{F}_i(\hat{s}, \beta)$  for the integrated cross section for  $gg \rightarrow V\bar{V}$  are:

$$\begin{aligned}
\bar{F}_0 &= \beta \left( \frac{523}{4} - 90\beta^2 + \frac{93}{4}\beta^4 \right) - \frac{3}{4} (65 - 83\beta^2 + 19\beta^4 - \beta^6) \log \left| \frac{1+\beta}{1-\beta} \right| \\
\bar{F}_1 &= -4\beta(41 - 9\beta^2) - \frac{87}{2}(1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right|
\end{aligned} \tag{100}$$

$$\bar{F}_2 = 36\beta(1 - \beta^2) - 25(1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{101}$$

$$\bar{F}_3 = \beta(75 - 9\beta^2) + \frac{7}{4}\beta \frac{\hat{s}}{M_\Phi^2} - \frac{1}{4}(1 - 61\beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{102}$$

$$\bar{F}_4 = -2\beta(20 - 9\beta^2) + \frac{1}{2}(91 - 31\beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{103}$$

$$\bar{F}_5 = \beta \left( \frac{209}{6} - 9\beta^2 \right) + \frac{263}{12}\beta \frac{\hat{s}}{M_\Phi^2} + \frac{3}{2}\beta \frac{\hat{s}^2}{M_\Phi^4} - \left( \frac{219}{4} - \frac{31}{4}\beta^2 + \frac{\hat{s}}{M_\Phi^2} \right) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{104}$$

$$\bar{F}_6 = -9\beta - \frac{7}{4}\beta \frac{\hat{s}}{M_\Phi^2} - \left( \frac{103}{8} + \frac{3}{8}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{105}$$

$$\bar{F}_7 = \frac{55}{2}\beta - \frac{17}{4}\beta \frac{\hat{s}}{M_\Phi^2} - \left( \frac{185}{8} - \frac{1}{8}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right| \tag{106}$$

$$\bar{F}_8 = -\frac{35}{2}\beta - 22\beta\frac{\hat{s}}{M_\Phi^2} - \frac{3}{2}\beta\frac{\hat{s}^2}{M_\Phi^4} + \left(\frac{375}{8} + \frac{7}{8}\beta^2 + \frac{\hat{s}}{M_\Phi^2}\right) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (107)$$

$$\bar{F}_9 = -\beta + \frac{199}{12}\beta\frac{\hat{s}}{M_\Phi^2} - \frac{37}{12}\beta\frac{\hat{s}^2}{M_\Phi^4} - \left(\frac{87}{8} + \frac{5}{8}\beta^2\right) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (108)$$

$$\bar{F}_{10} = \frac{41}{24}\beta + \frac{11}{12}\beta\frac{\hat{s}}{M_\Phi^2} + \left(\frac{7}{4} + \frac{1}{8}\beta^2\right) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (109)$$

$$\bar{F}_{11} = -\frac{41}{6}\beta + \frac{23}{6}\beta\frac{\hat{s}}{M_\Phi^2} + \frac{1}{2}(1-\beta^2) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (110)$$

$$\bar{F}_{12} = \frac{41}{4}\beta + \frac{43}{48}\beta\frac{\hat{s}}{M_\Phi^2} + \frac{145}{96}\beta\frac{\hat{s}^2}{M_\Phi^4} - \left(12 - \frac{3}{4}\beta^2 + \frac{1}{4}\frac{\hat{s}}{M_V^2}\right) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (111)$$

$$\bar{F}_{13} = -\frac{41}{6}\beta - \frac{355}{24}\beta\frac{\hat{s}}{M_V^2} + \frac{37}{16}\beta\frac{\hat{s}^2}{M_\Phi^4} + \left(\frac{31}{2} - \frac{1}{2}\beta^2\right) \log\left|\frac{1+\beta}{1-\beta}\right| \quad (112)$$

$$\bar{F}_{14} = \frac{41}{24}\beta + \frac{37}{4}\beta\frac{\hat{s}}{M_\Phi^2} - \frac{113}{32}\beta\frac{\hat{s}^2}{M_\Phi^4} + \frac{49}{96}\beta\frac{\hat{s}^3}{M_\Phi^6} - \left(\frac{23}{4} - \frac{1}{8}\beta^2 + \frac{1}{4}\frac{\hat{s}}{M_\Phi^2}\right) \log\left|\frac{1+\beta}{1-\beta}\right|. \quad (113)$$

$$(114)$$

Finally, the coefficients for the differential and the integrated cross section for  $q\bar{q} \rightarrow V\bar{V}$ ,  $G_i(\hat{s}, \beta, \cos\theta)$  and  $\tilde{G}_i(\hat{s}, \beta)$ , are given by  $[99]_r$  : 5 fcts.

$$G_0 = 1 + \frac{1}{16} \left[ \frac{\hat{s}}{M_\Phi^2} - (1 + 3\beta^2) \right] \sin^2\theta \quad (115)$$

$$G_1 = -1 - \frac{1}{8} \left[ \frac{\hat{s}}{M_\Phi^2} - 2 \right] \sin^2\theta \quad (116)$$

$$G_2 = 1 \quad (117)$$

$$G_3 = \frac{1}{4} + \frac{1}{16} \left[ \frac{\hat{s}}{M_\Phi^2} - 2 \right] \sin^2\theta \quad (118)$$

$$G_4 = -\frac{1}{2} + \frac{1}{4} \sin^2\theta \quad (119)$$

$$G_5 = \frac{1}{4} + \frac{1}{8} \left[ \frac{\hat{s}}{M_\Phi^2} - 1 \right] \sin^2\theta \quad (120)$$

$$\tilde{G}_0 = \frac{1}{24} \frac{\hat{s}}{M_\Phi^2} + \frac{23 - 3\beta^2}{24} \quad (121)$$

$$\tilde{G}_1 = -\frac{1}{12} \frac{\hat{s}}{M_\Phi^2} - \frac{5}{6} \quad (122)$$

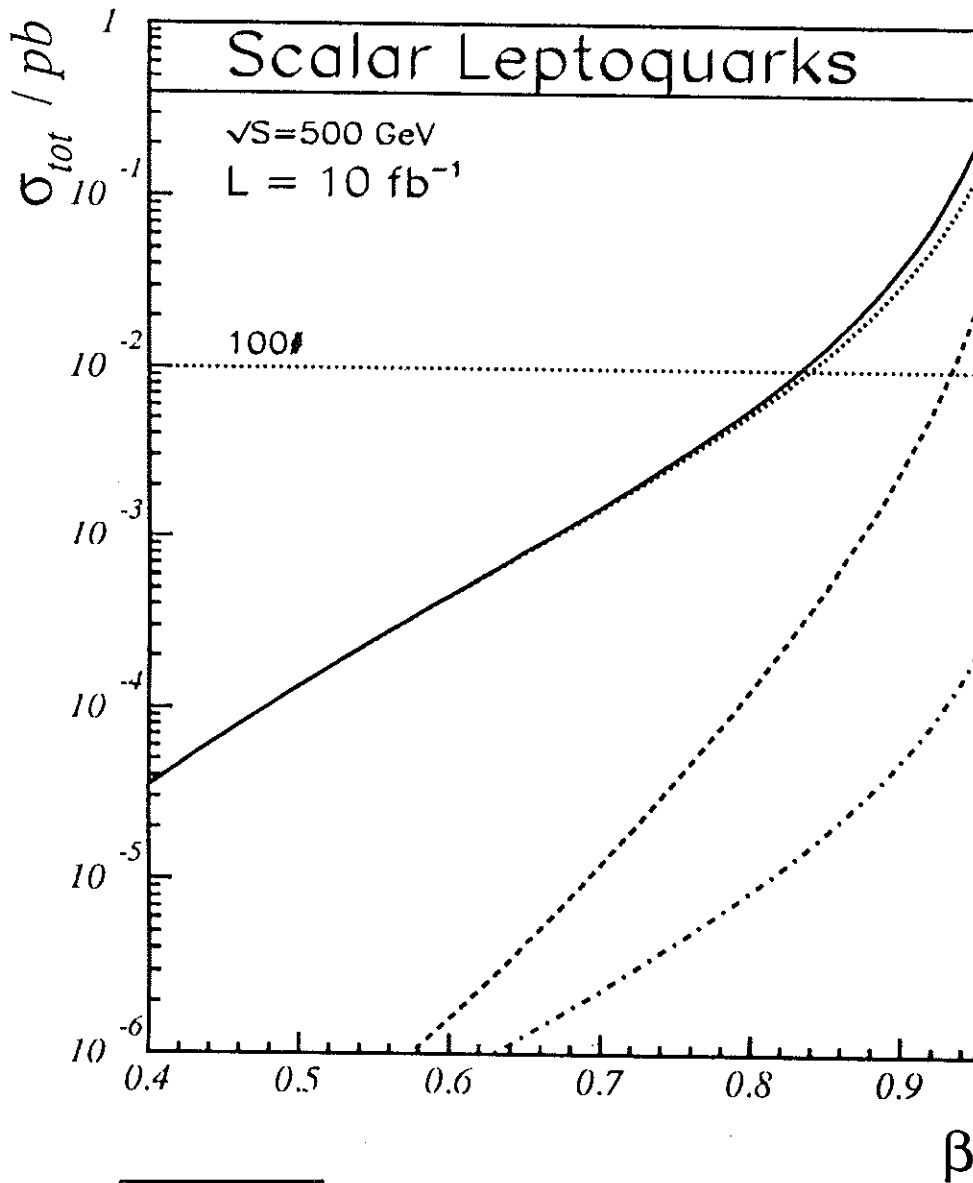
$$\tilde{G}_2 = 1 \quad (123)$$

$$\tilde{G}_3 = \frac{1}{24} \frac{\hat{s}}{M_\Phi^2} + \frac{1}{6} \quad (124)$$

$$\tilde{G}_4 = -\frac{1}{3} \quad (125)$$

$$\tilde{G}_5 = \frac{1}{12} \frac{\hat{s}}{M_\Phi^2} + \frac{1}{6}. \quad (126)$$

## 4 Numerical Results



$$\beta = \sqrt{1 - \frac{4M^2}{S}}$$

Figure 11a: Integrated cross sections for scalar leptoquark pair production through  $\gamma^*\gamma^* \rightarrow S\bar{S}$  (WWA spectrum) at future  $e^+e^-$  colliders for  $\sqrt{S} = 500 \text{ GeV}$  as a function of  $\beta$ . Full line:  $\sigma_{tot}$  for  $|Q_\Phi| = 5/3$ ; dotted line:  $\sigma_{dir}$  for  $|Q_\Phi| = 5/3$ ; dashed line:  $\sigma_{tot}$  for  $|Q_\Phi| = 1/3$ ; dash-dotted line:  $\sigma_{dir}$  for  $|Q_\Phi| = 1/3$ .

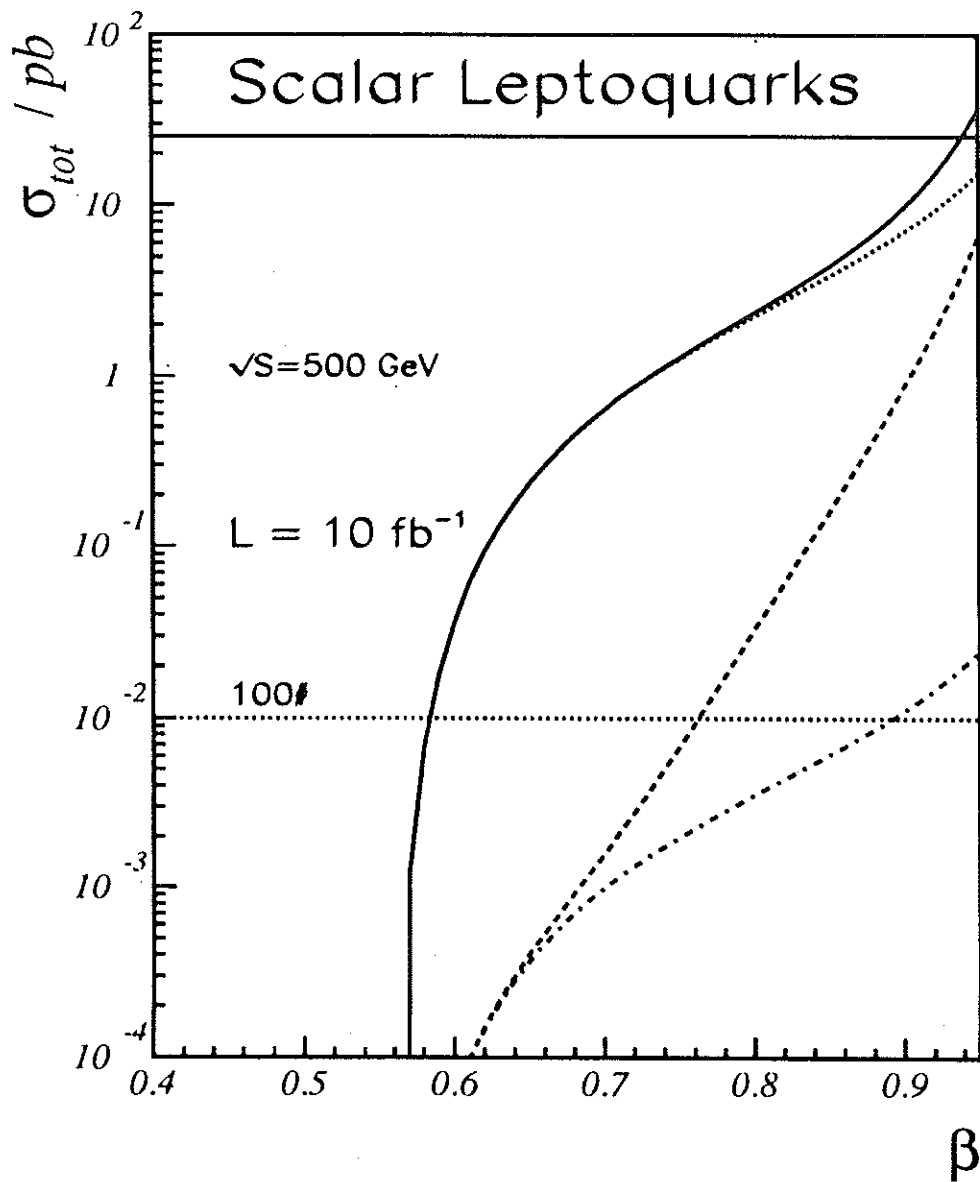


Figure 11b: Integrated cross sections for scalar leptoquark pair production at future  $\gamma\gamma$  colliders using Laser back scattering for electron beam conversion. The parameters are the same as in figure 10a.

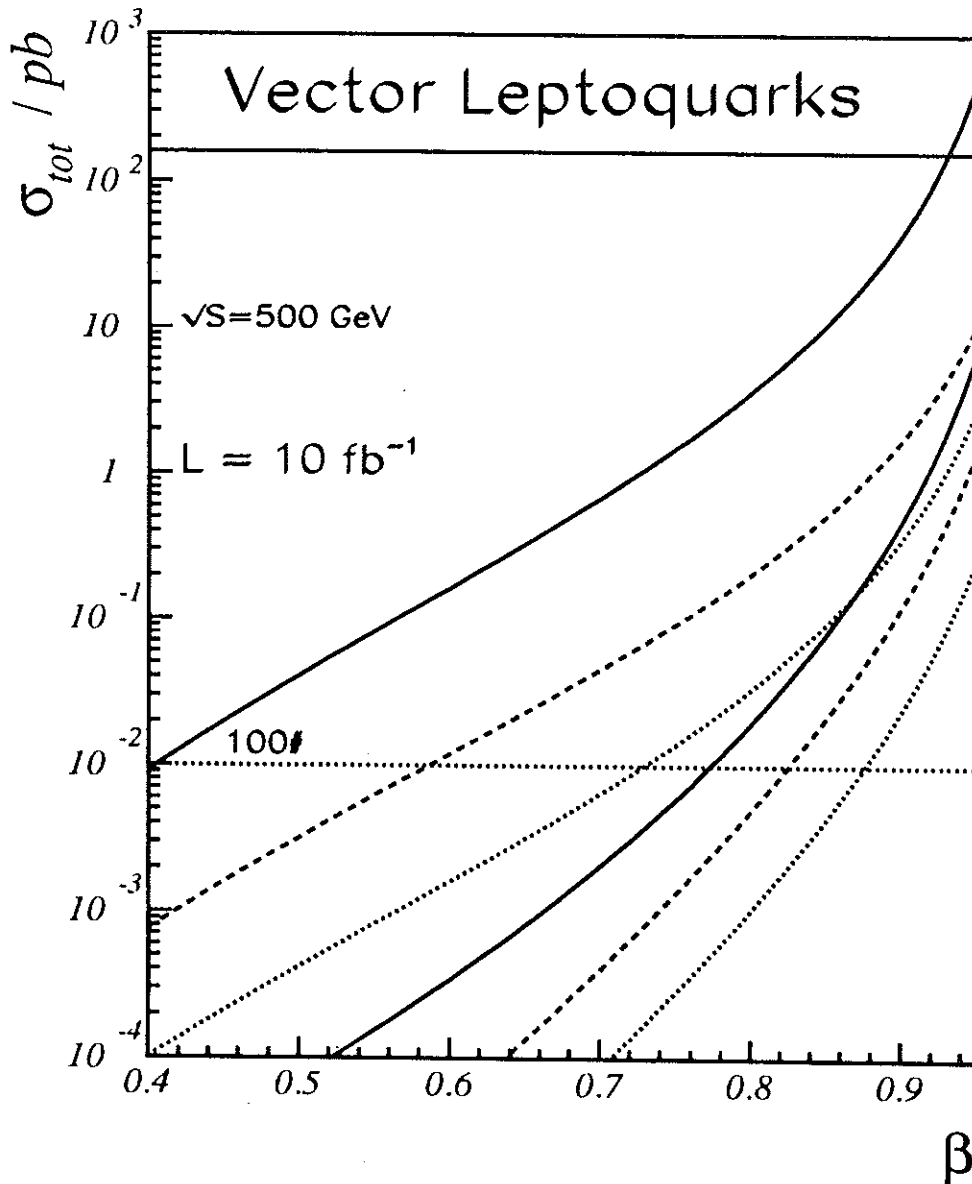


Figure 12a: Integrated cross sections for vector leptoquark pair production through  $\gamma^*\gamma^* \rightarrow S\bar{S}$  (WWA spectrum) at future  $e^+e^-$  colliders for  $\sqrt{S} = 500$  GeV as a function of  $\beta$ . Integrated cross  
 Upper full line:  $|Q_\Phi| = 5/3, \kappa_{A,G} = \lambda_{A,G} = -1$  (MM5); Upper dashed line:  $|Q_\Phi| = 5/3, \kappa_{A,G} = \lambda_{A,G} = 0$  (YM5); Upper dotted line:  $|Q_\Phi| = 5/3, \kappa_{A,G} = 1, \lambda_{A,G} = 0$  (MC5); The corresponding lower lines are those for  $|Q_\Phi| = 1/3$ .

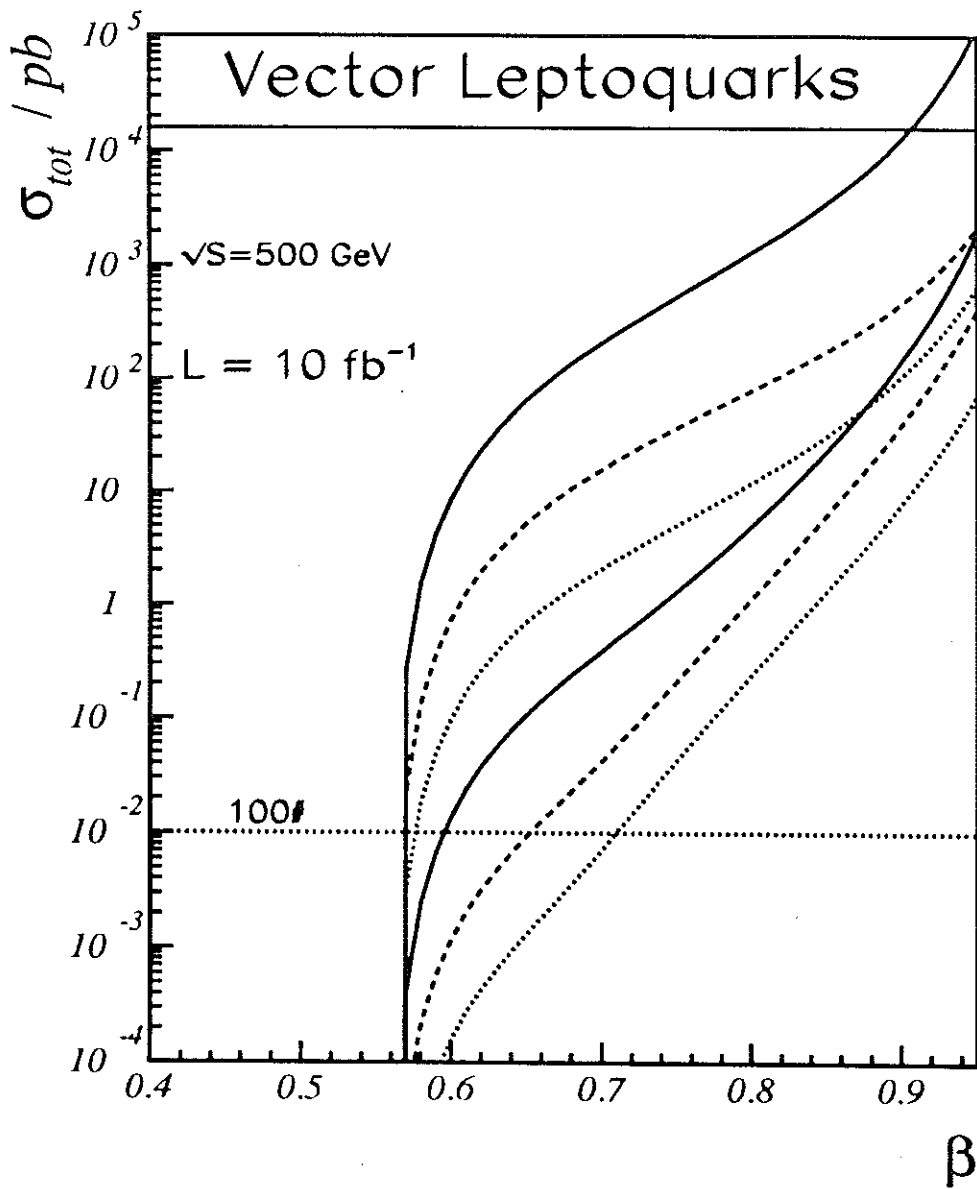


Figure 12b: Integrated cross sections for vector leptoquark pair production at future  $\gamma\gamma$  colliders using Laser back scattering for electron beam conversion. The parameters are the same as in figure 12a.

## 5 Comparison with Future Search Limits at other Colliders

| Collider          | Mode                      | $\sqrt{S}$ | Luminosity   | Q   | Scalar Leptoquarks |      | Vector Leptoquarks |      |
|-------------------|---------------------------|------------|--------------|-----|--------------------|------|--------------------|------|
|                   |                           |            |              |     | 100#               | 10#  | 100#               | 10#  |
| TEVATRON          | $p\bar{p}$                | 1.8 TeV    | $100pb^{-1}$ |     | 140                | 200  | 195                | 270  |
| TEV33             | $p\bar{p}$                | 2.0 TeV    | $1fb^{-1}$   |     | 210                | 290  | 290                | 370  |
| LHC               | $pp$                      | 14 TeV     | $10fb^{-1}$  |     | 900                | 1200 | 1200               | 1500 |
| HERA              | $ep$                      | 314 GeV    | $100pb^{-1}$ | 1/3 | -                  | -    | -                  | 50   |
|                   |                           |            |              | 5/3 | 45                 | 60   | 55                 | 70   |
| LEP @ LHC         | $ep$                      | 1.26 TeV   | $1fb^{-1}$   | 1/3 | 90                 | 130  | 130                | 180  |
|                   |                           |            |              | 5/3 | 105                | 220  | 200                | 260  |
|                   |                           |            |              |     |                    |      |                    |      |
| LINAC<br>$e^+e^-$ | $\gamma^*\gamma^*$<br>WWA | 500 GeV    | $10fb^{-1}$  | 1/3 | 90                 | 125  | 120                | 155  |
|                   |                           |            |              | 5/3 | 135                | 185  | 170                | 210  |
| LINAC<br>$e^+e^-$ | $\gamma\gamma$<br>Compton | 500 GeV    | $10fb^{-1}$  | 1/3 | 160                | 185  | 175                | 190  |
|                   |                           |            |              | 5/3 | 200                | 205  | 200                | 205  |
| LINAC<br>$e^+e^-$ | $\gamma^*\gamma^*$<br>WWA | 1 TeV      | $10fb^{-1}$  | 1/3 | 140                | 195  | 285                | 345  |
|                   |                           |            |              | 5/3 | 220                | 325  | 435                | 470  |
| LINAC<br>$e^+e^-$ | $\gamma\gamma$<br>Compton | 1 TeV      | $10fb^{-1}$  | 1/3 | 300                | 340  | 390                | 405  |
|                   |                           |            |              | 5/3 | 400                | 405  | 410                | 410  |

V: MC.