Investigation of Matter Effects in Neutrino Oscillations with IceCube Sensitivity

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Neutrino Oscillations

- All neutrinos undergo oscillations as they propagate
- Simplest case probability formula:

$$P_{\nu_{\alpha} \to \nu_{\beta}}(L, E) = \sin^{2}(2\theta) \sin^{2}\left(\frac{\Delta m^{2}L}{4E}\right)$$

$$|v_l\rangle = \sum_{i=1}^{5} U_{li}^* |v_i\rangle$$

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- Effect is enhanced for larger $\frac{L}{E}$
- DeepCore:
 - □ ~10-100GeV
 - 0-12,720km



Earth's Density and State Amplitude

• In matter, a potential term is added:

$$V(x) = \sqrt{2}G_F N_e(x) = \frac{A_{CC}(x)}{2E}$$

• Density profile for the Earth:



A. M. Dziewonski, D. L. Anderson, Phys. Earth Planet. Interiors, 25, 297 (1981) • In every layer, state amplitude changes:

$$\left|\Psi_{\alpha}\right\rangle = U_{M}MU_{M}^{*}\left|\Psi_{\alpha}\right\rangle$$

- *U* is a mixing matrix
- From the Schrödinger equation, *M* consists of terms of the form:

$$\exp\!\left(\frac{-i\Delta m^2 L}{2E}\right)$$

 First approximation: a series of constant density layers

Matter Modification

Matters

- Neutrino mass hierarchy is unknown
- changing hierarchy changes the sign of Δm_{31}^2
- Modified mixing angle:

The mass difference is modified in matter:

 $\tan 2\theta_{13}^M = ---$

$$\Delta m_{M31}^2 = \sqrt{(\Delta m_{31}^2 \cos 2\theta_{13} - A_{CC})^2 + (\Delta m_{31}^2 \sin 2\theta_{13})^2}$$

- Different values of Δm_{M31}^2 depend on the mass hierarchy
- This leads to different values of the probability
- Is it detectable?



Probability Variation

- Using a mantle-core-mantle step function density profile
- Using an initial muon neutrino
- As a function of energy
- 12,720km



- As a function of length
- 5GeV:





Atmospheric Flux Spectrum

- Used the Honda atmospheric neutrino flux spectrum
 - This means the initial state is mixed





M. Honda, T. Kajita, K. Kasahara, S. Midorikawa, Phys. Rev. D, 83 123001 (2011)

Neutrino Oscillograms



• 3: Matter; inverse hierarchy



• 1: Vacuum case



Colour = Likelihood of numu detection

• 4: Vacuum - Matter difference



• (normal hierarchy)

Flux of NuMu events

• Variation with energy



• Variation with zenith angle





Triggering and filtering of detector

• Reconstruct to find the direction: x, y, z, zenith and azimuth

• Can fit to 5/6 DOM hits

Can fit to a single string:
Only 5 hits now required



Energy Spectrum and Detector Response

Energy Spectrum



• Results including triggering and filtering





Cuts to the simulation

- Energies above 25GeV
- Angles above the horizon
- Track lengths shorter than 20m
- Fewer than 5/6 DOMs hit
- Non- Charged Current Muon interactions (track-like events only)

Results after cuts

• Results including cuts to Monte Carlo:



• Results after reconstruction to Monte Carlo:



What Next?

- Study of Systematic Errors:
 - IceCube flux reconstruction
 - DOM acceptance
 - Properties of the ice
 - Improvement of low energy reconstruction

- Extension to the model:
 - Inclusion of further layers
 - Different density profile

Extending the Model

• Inclusion of: - 15km average production height

- the inner core



Thanks for Listening!

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Back-Up Slides

Probability Variation



Probability Variation

Including 15km average production height and the inner core:



Matter Modified Mixing Matrix

$$U_{M} = \begin{pmatrix} \cos \theta_{13}^{M} & 0 & \sin \theta_{13}^{M} e^{-i\delta_{CP}} \\ -\sin \theta_{23} \sin \theta_{13}^{M} e^{i\delta_{CP}} & \cos \theta_{23} & \sin \theta_{23} \cos \theta_{13}^{M} \\ -\cos \theta_{23} \sin \theta_{13}^{M} e^{i\delta_{CP}} & -\sin \theta_{23} & \cos \theta_{23} \cos \theta_{13}^{M} \end{pmatrix}$$

Inclusion of a Layer of Atmosphere

At 8GeV:

- Neutrinos are produced at an average height of 15km
- At 5GeV:

