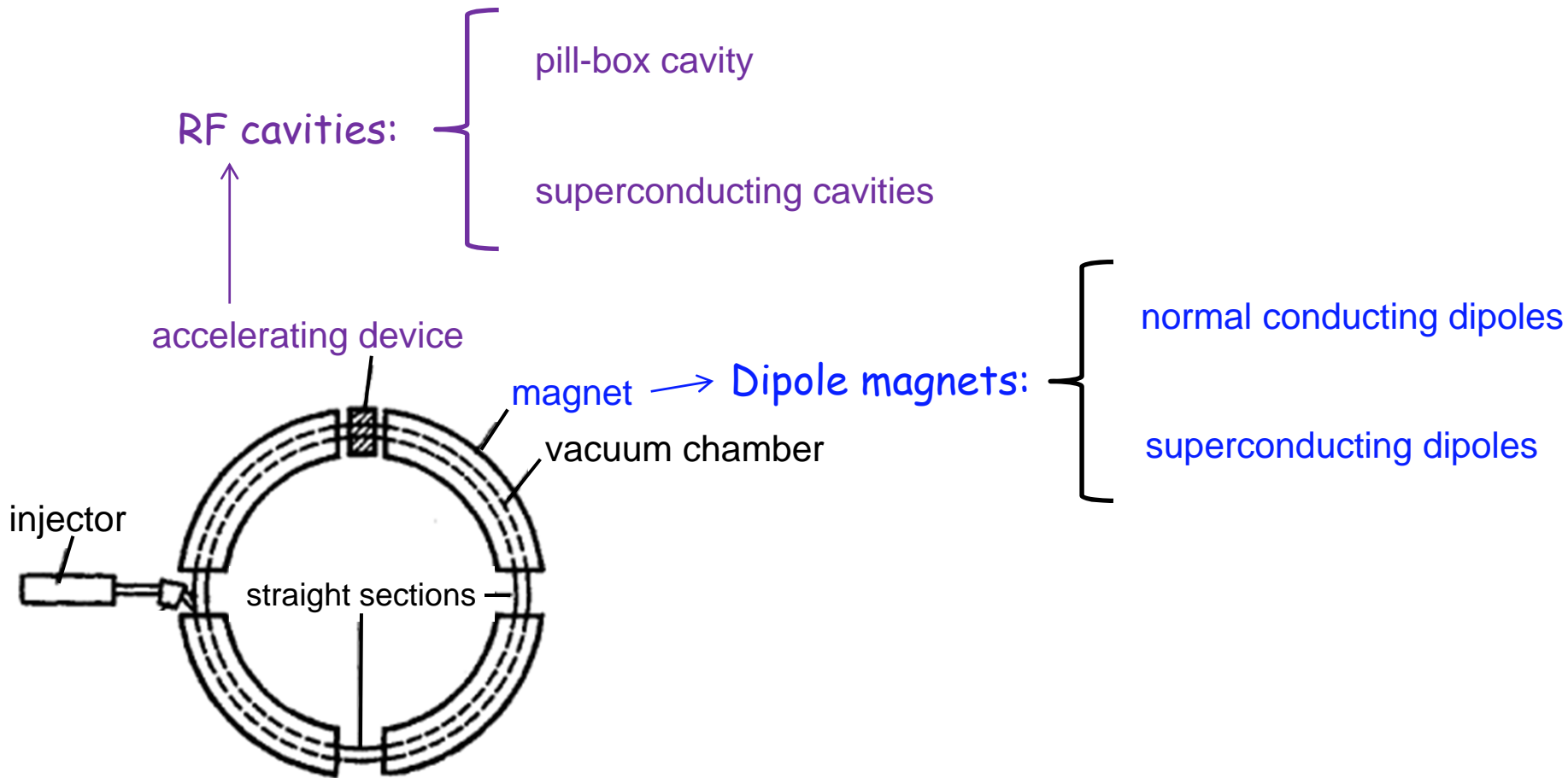


Colliders - part 2

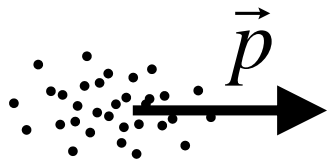
Accelerator physics - Colliders

Pedro Castro / Accelerator Physics Group (MPY)
Introduction to Accelerator Physics
DESY, 31st July 2012

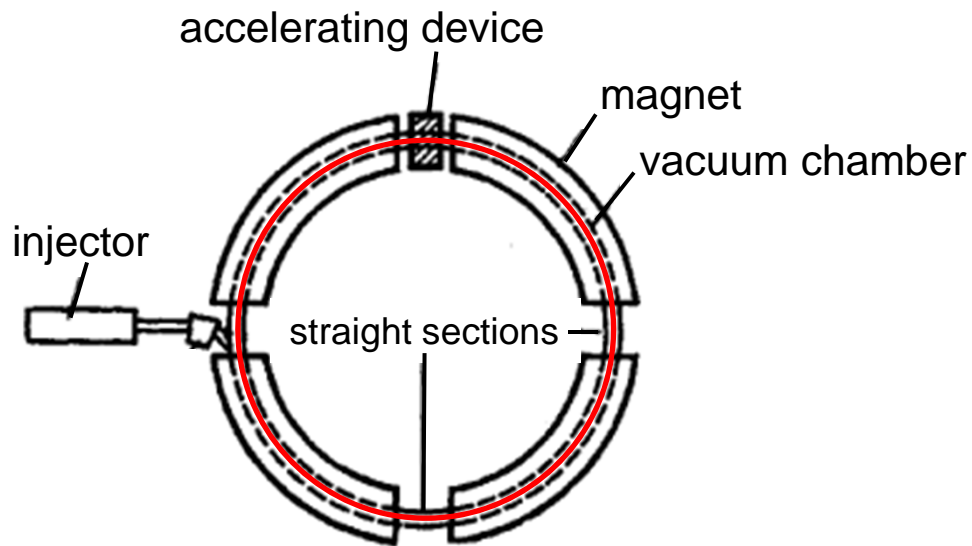
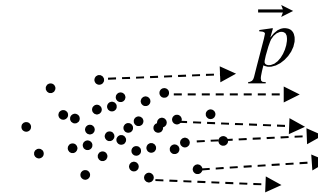
From part 1



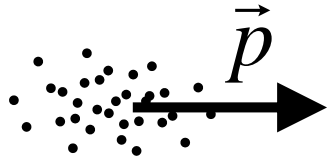
Need of focusing



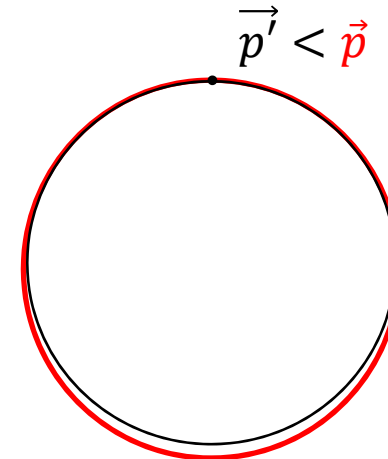
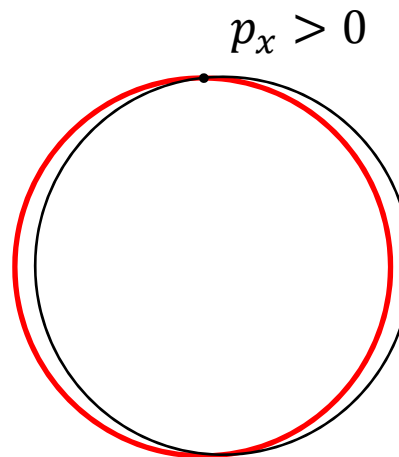
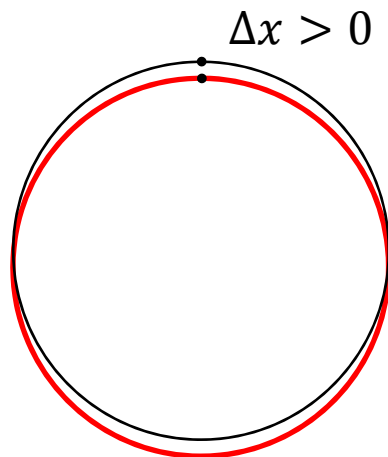
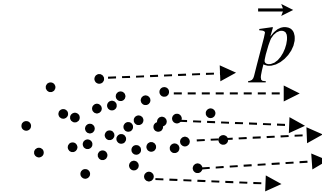
beam / bunch



Need of focusing

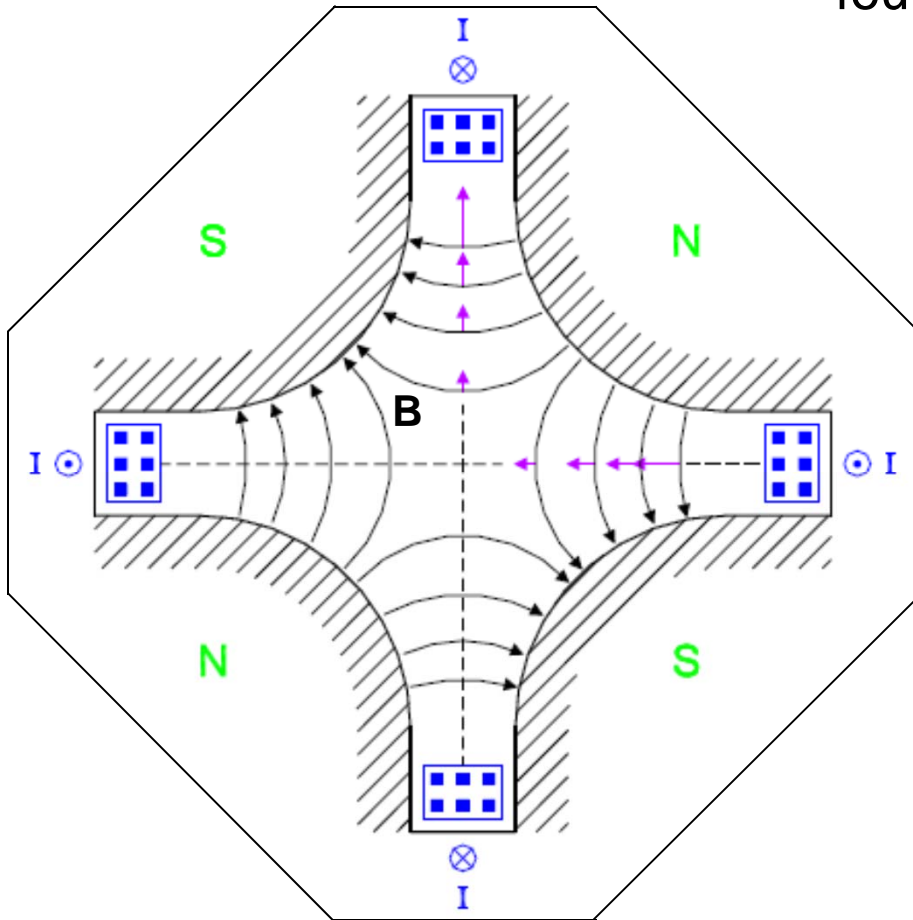


beam / bunch



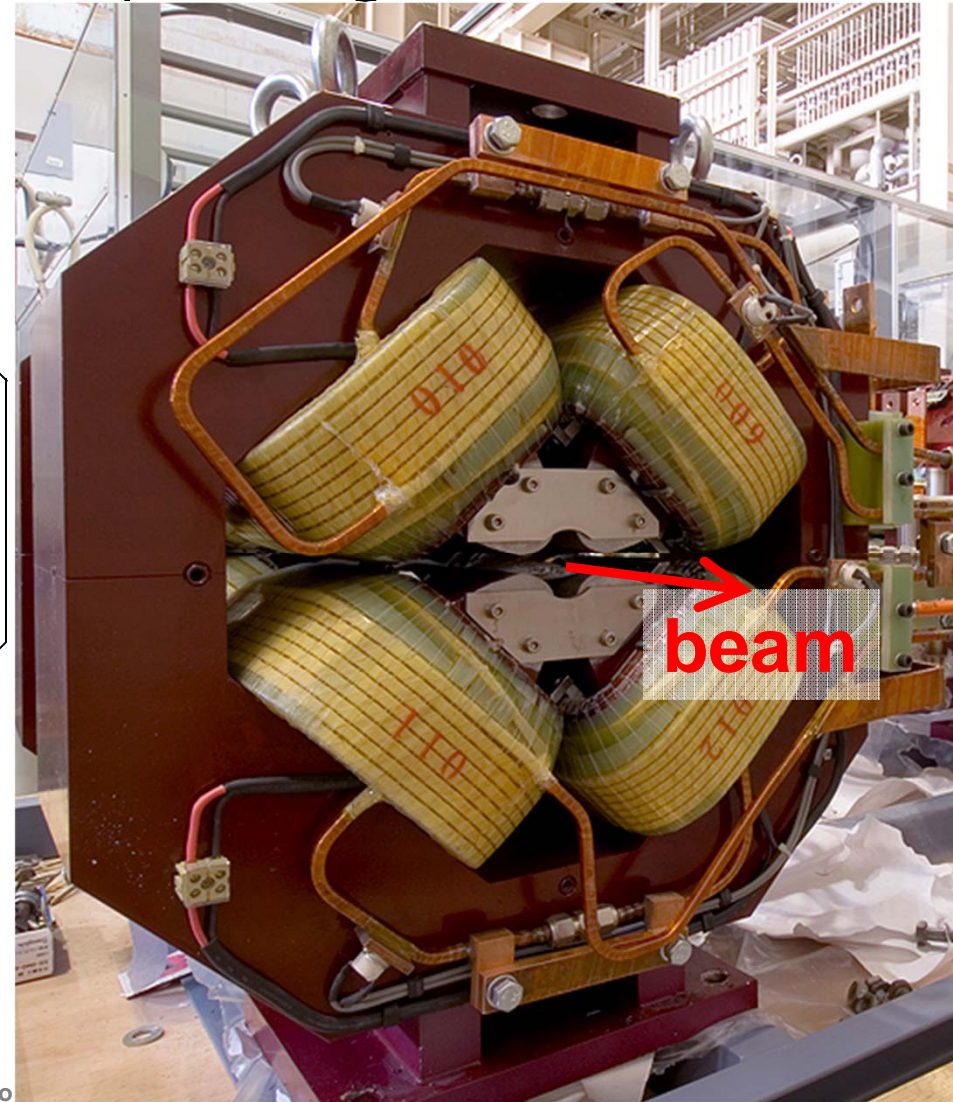
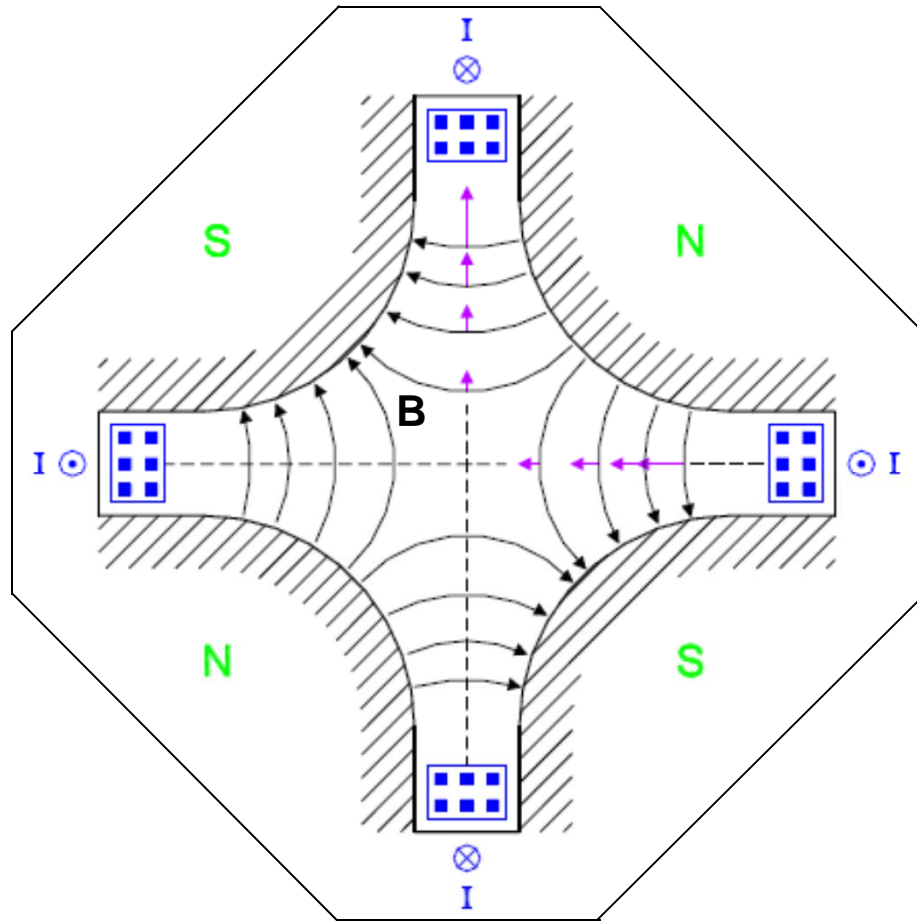
Need of focusing

quadrupole magnet:
four iron poles

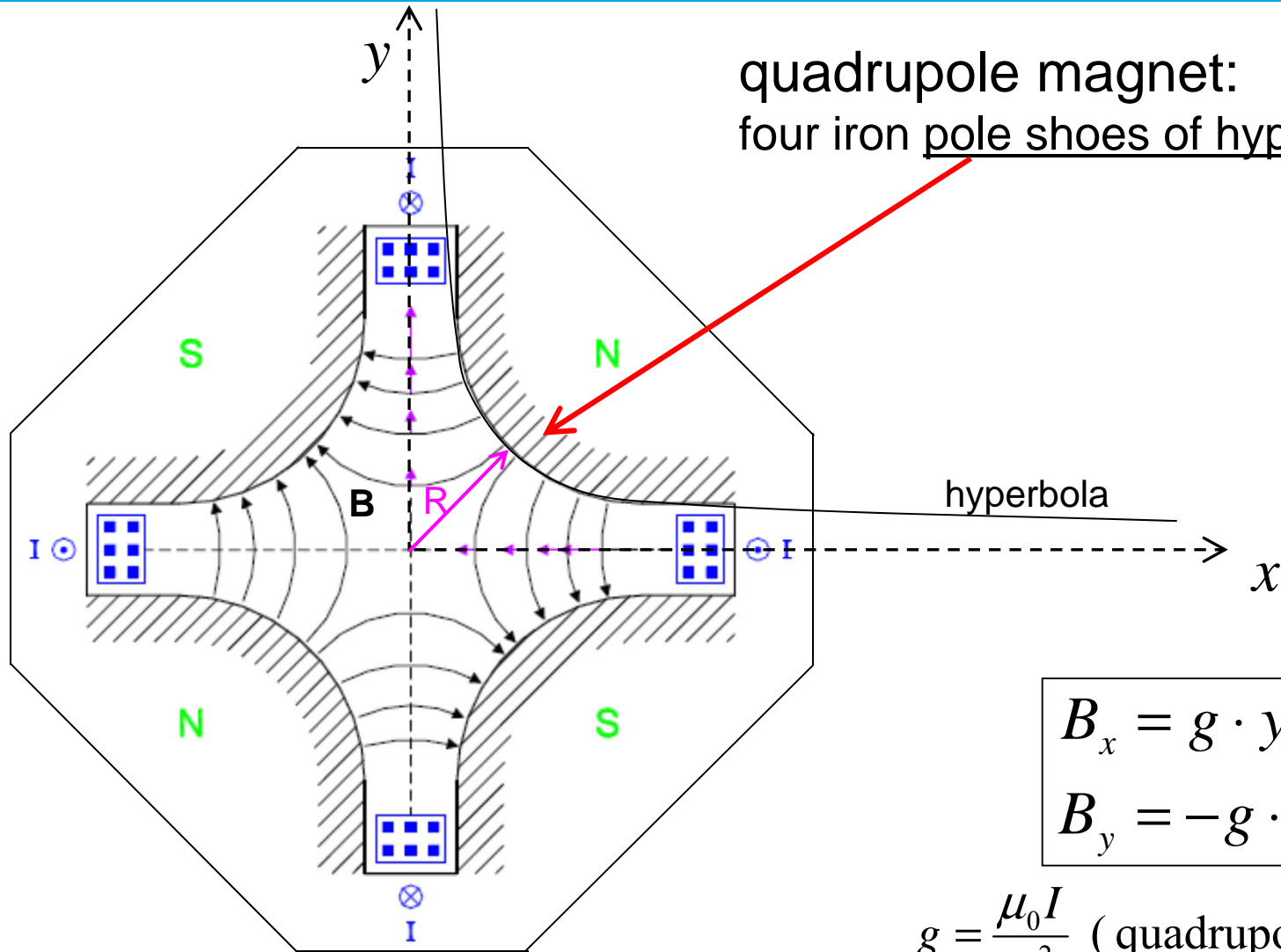


Quadrupole magnets

quadrupole magnet:



Quadrupole magnets

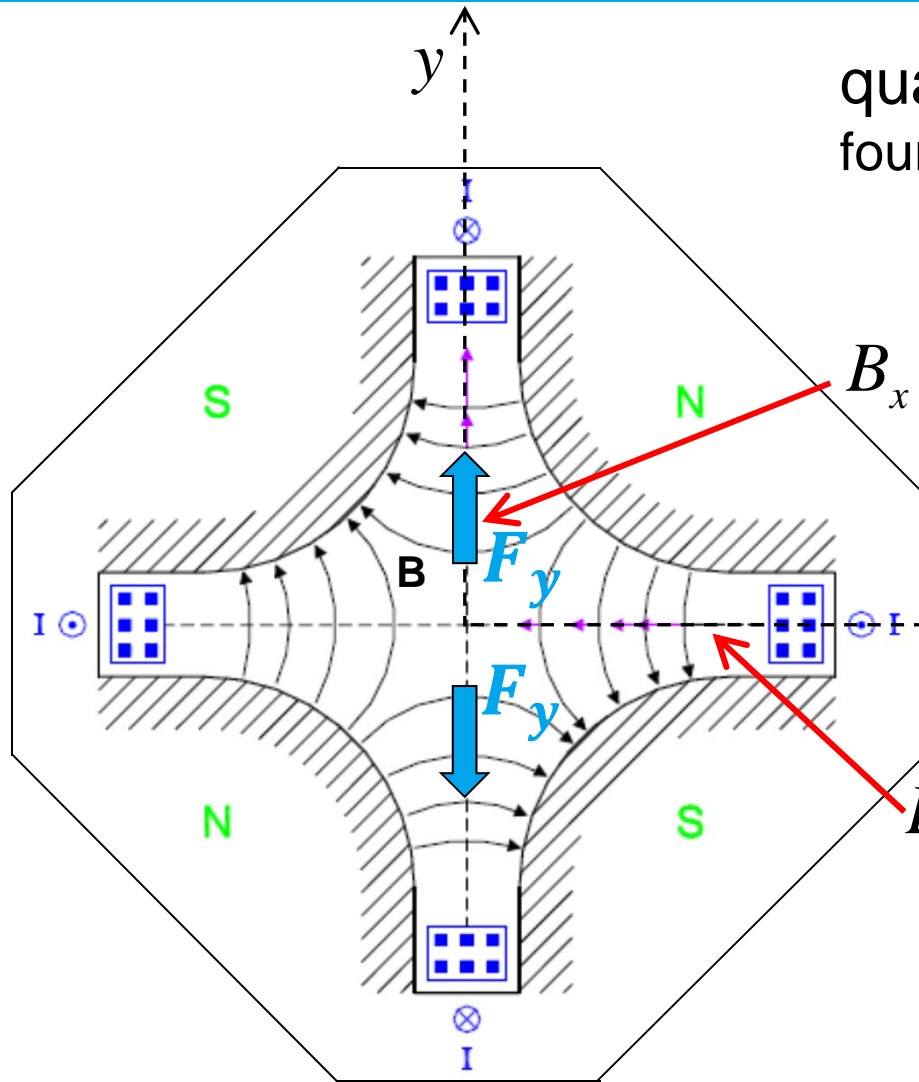


quadrupole magnet:
four iron pole shoes of hyperbolic contour

$$\begin{aligned} B_x &= g \cdot y \\ B_y &= -g \cdot x \end{aligned}$$

$$g = \frac{\mu_0 I}{R^2} \text{ (quadrupole gradient)}$$

Quadrupole magnets



quadrupole magnet:
four iron pole shoes of hyperbolic contour

$$B_x = g \cdot y \Rightarrow F_y = g \cdot y$$

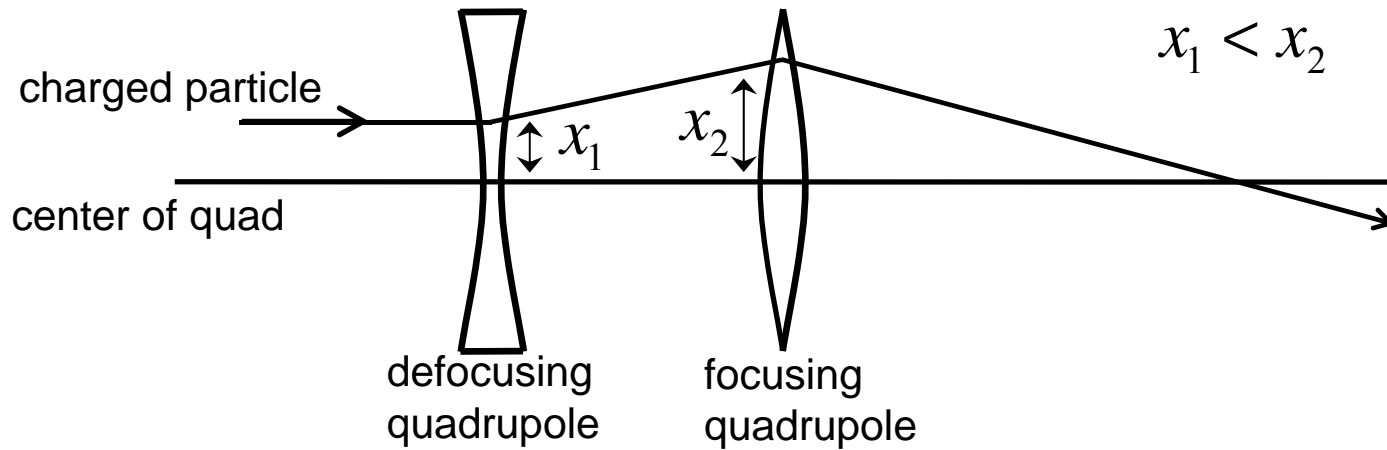
defocusing

$$B_y = -g \cdot x \Rightarrow F_x = -g \cdot x$$

focusing !

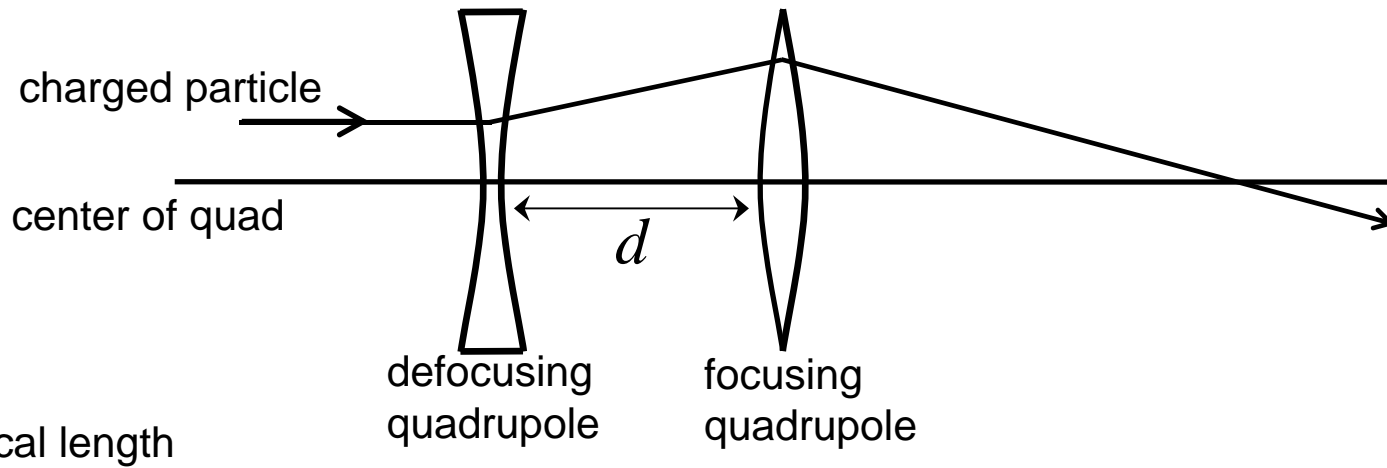
Quadrupole magnets

QD + QF = net focusing effect:



Quadrupole magnets

QD + QF = net focusing effect:

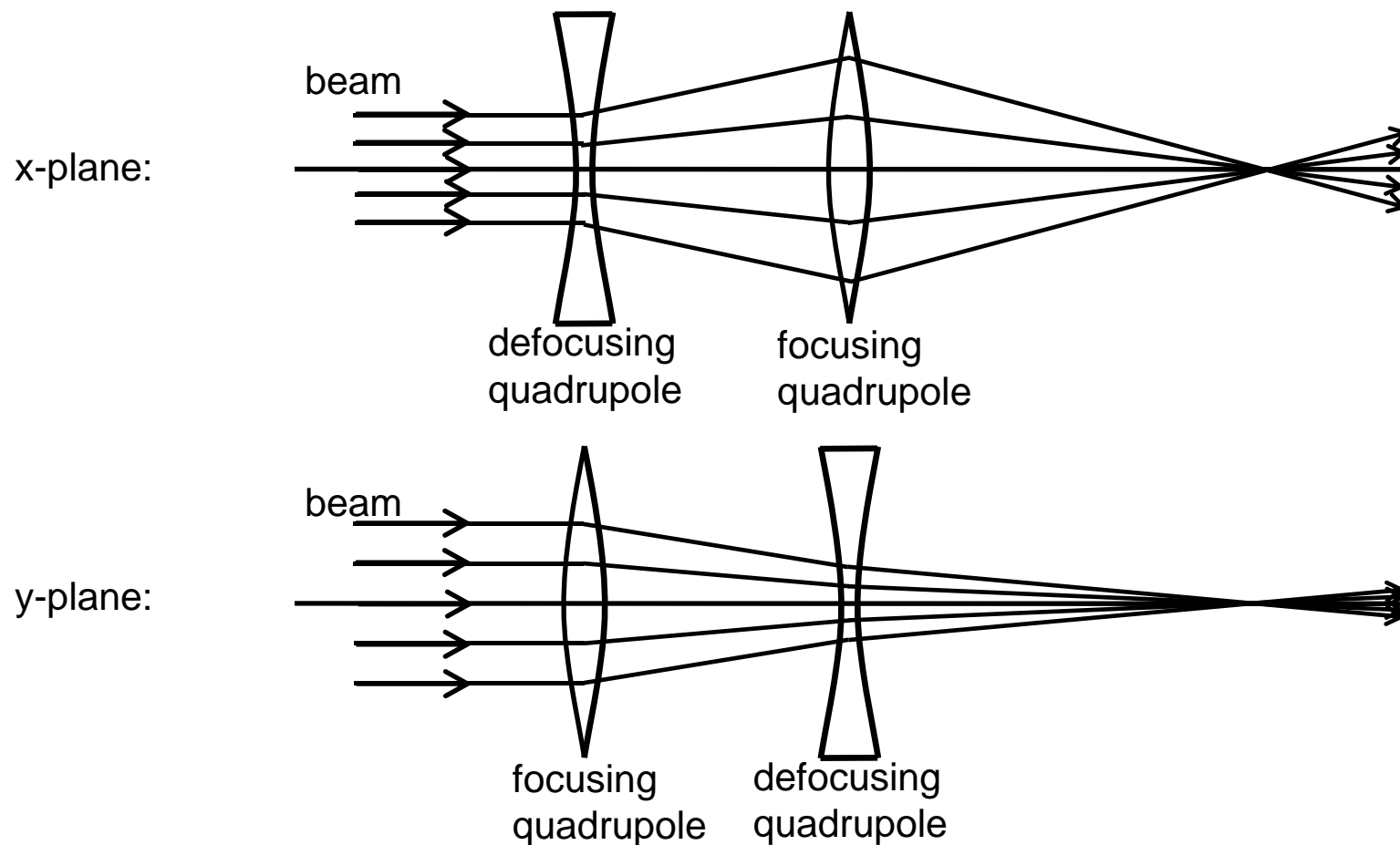


$$\frac{1}{f^*} = \frac{1}{f_D} + \frac{1}{f_F} - \frac{d}{f_D f_F} \quad (\text{light optics})$$

$$\text{if } f_D = -f_F = f \quad \frac{1}{f^*} = \frac{d}{f^2} > 0$$

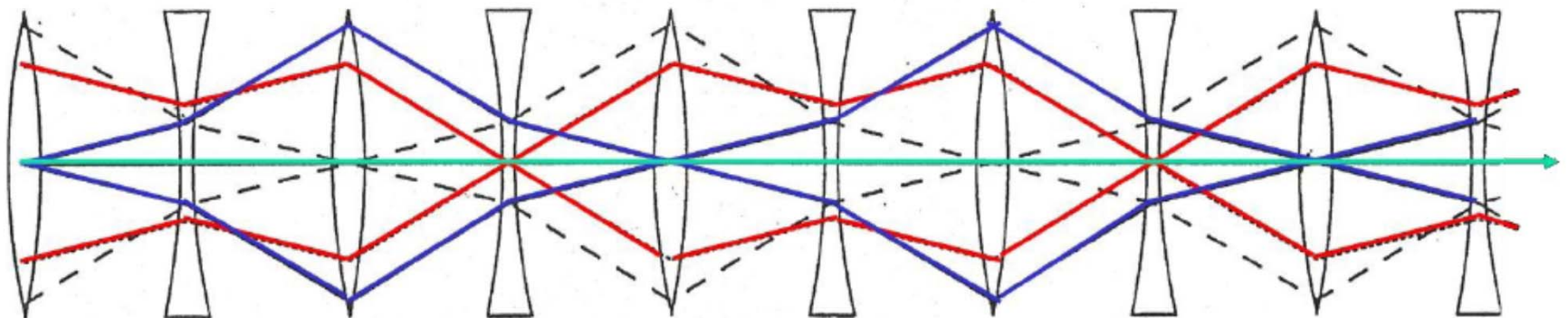
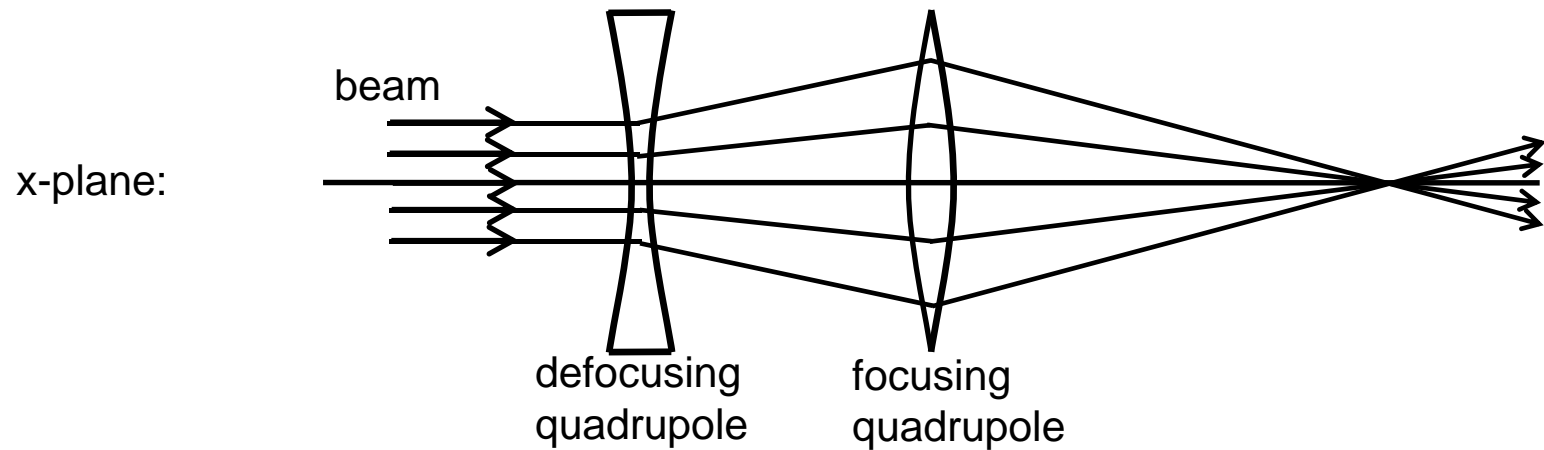
Quadrupole magnets

QD + QF = net focusing effect:

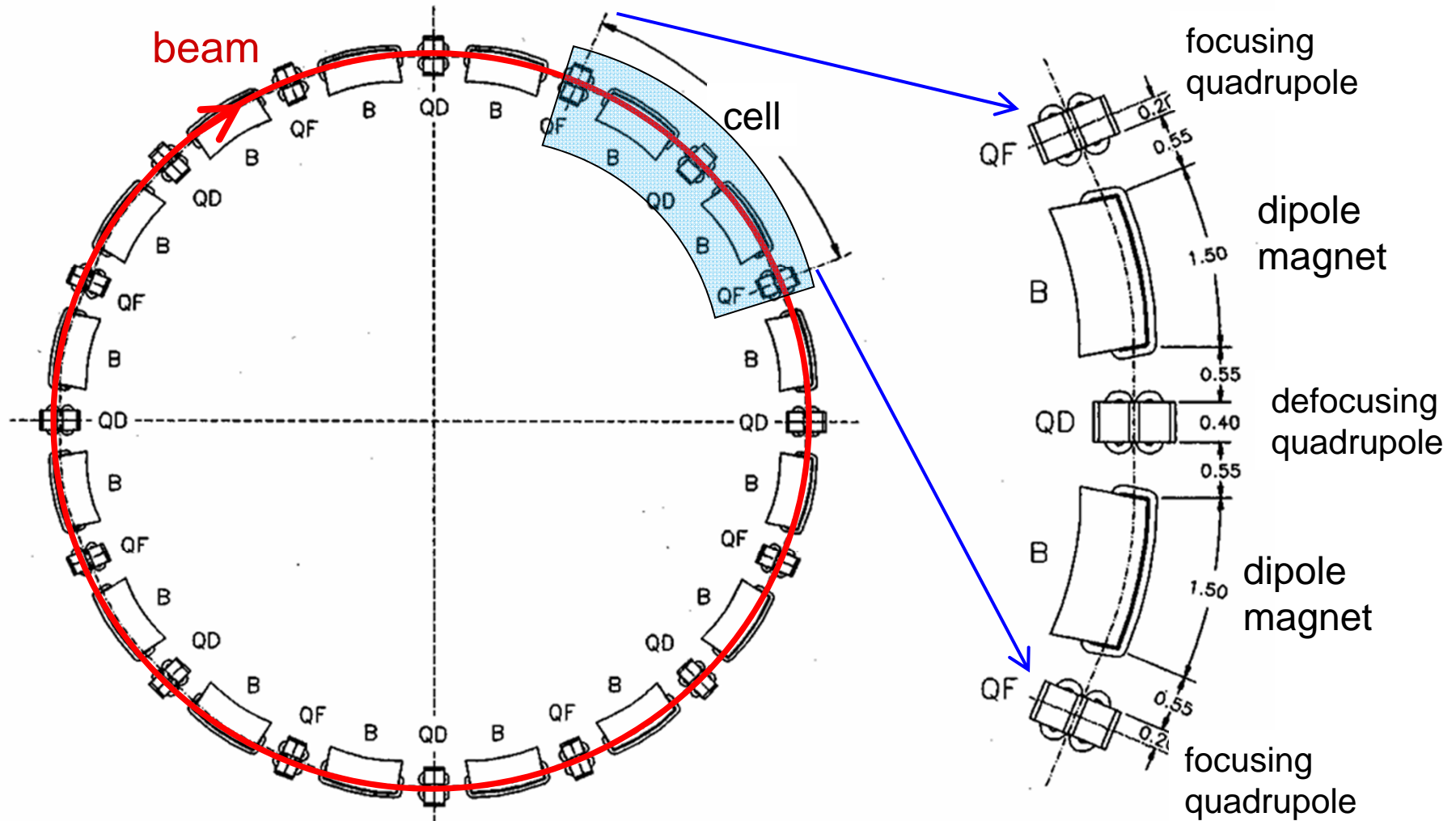


Quadrupole magnets

QD + QF = net focusing effect:

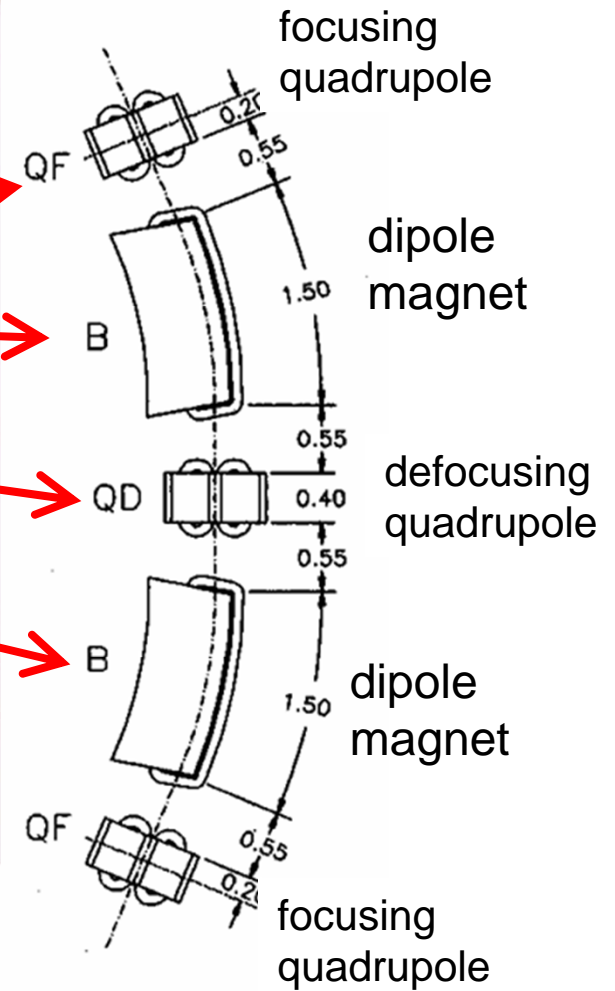
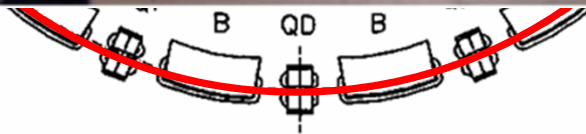


Circular accelerator



Circular accelerator

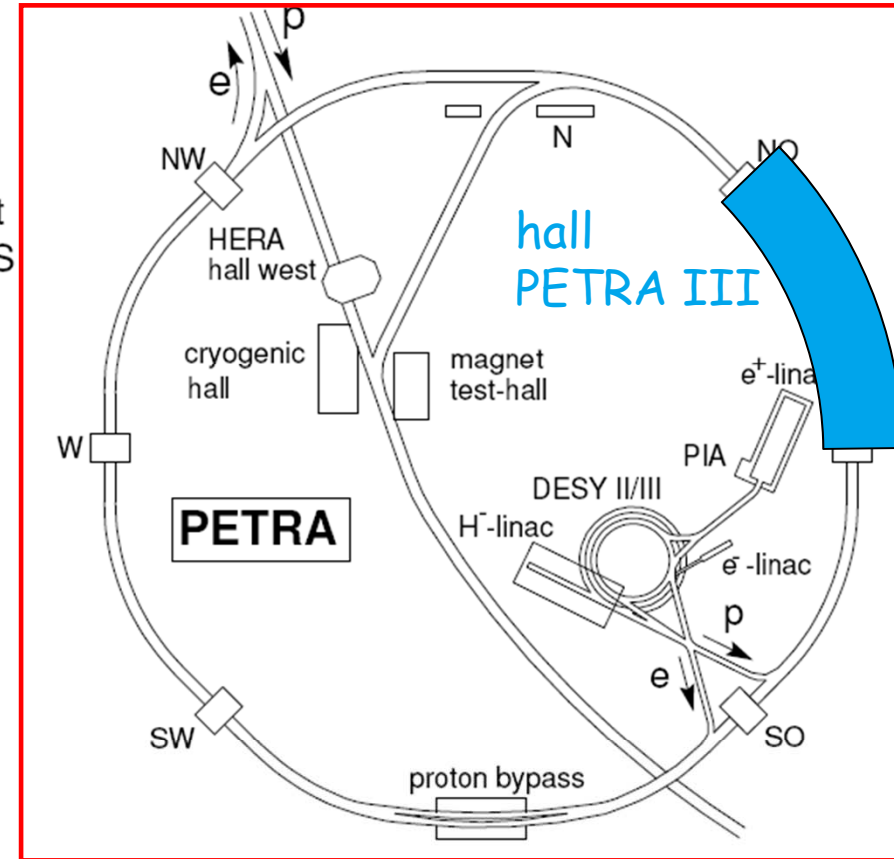
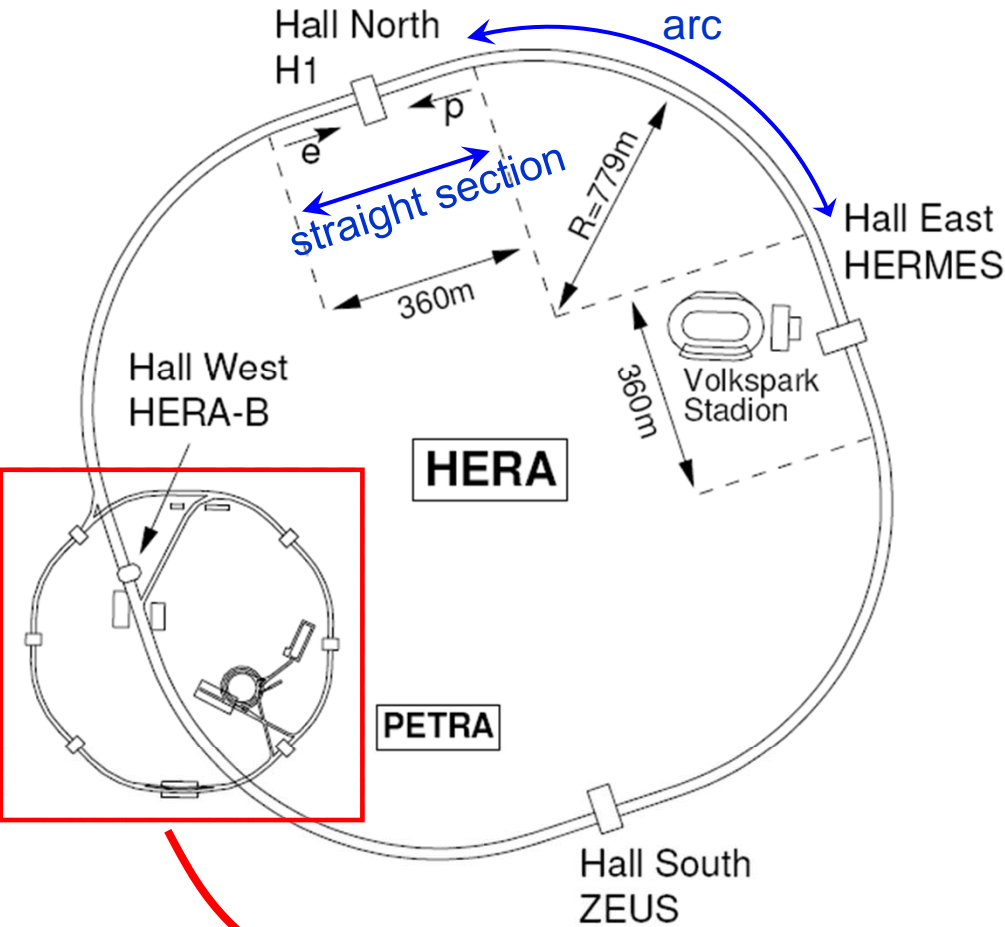
PETRA



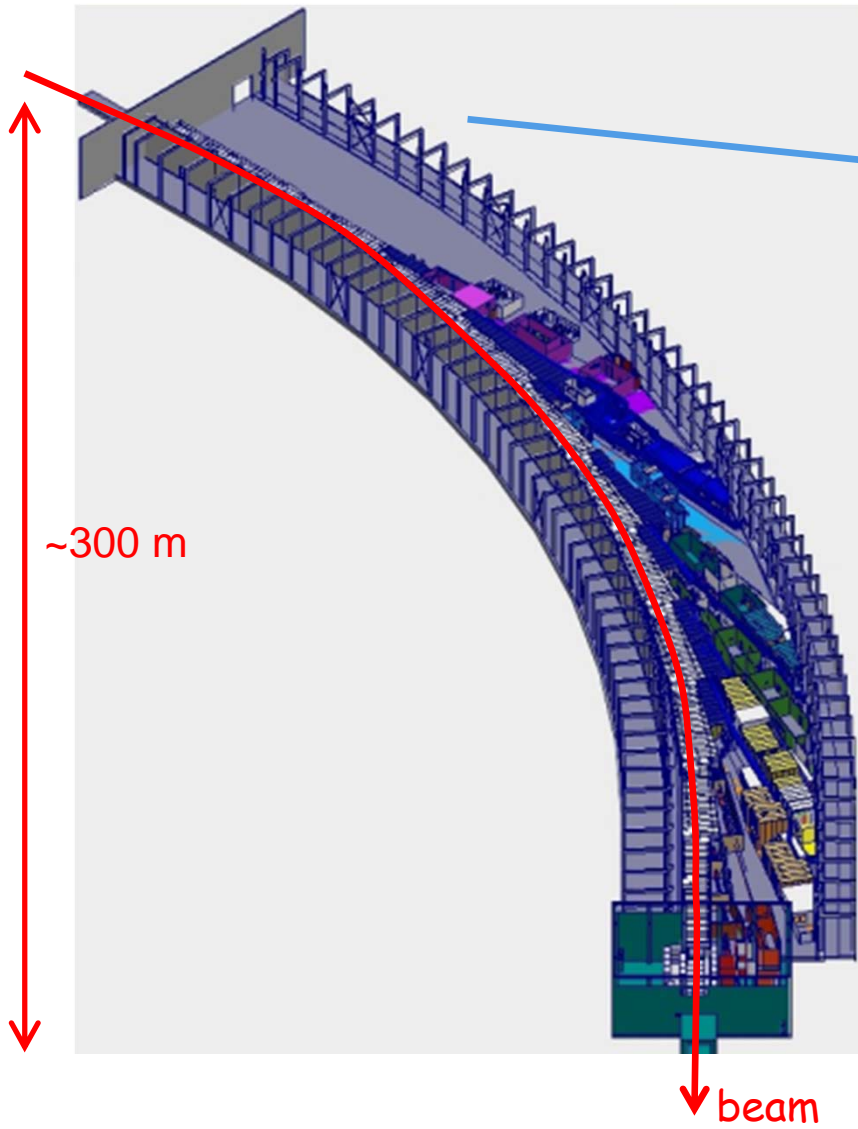
HERA collider and injector chain

HERA: 4 arcs + 4 straight sections

PETRA: 8 arcs + 8 straight sections



PETRA III



Why are the energies so different?

HERA (Hadron Electron Ring Accelerator) tunnel:

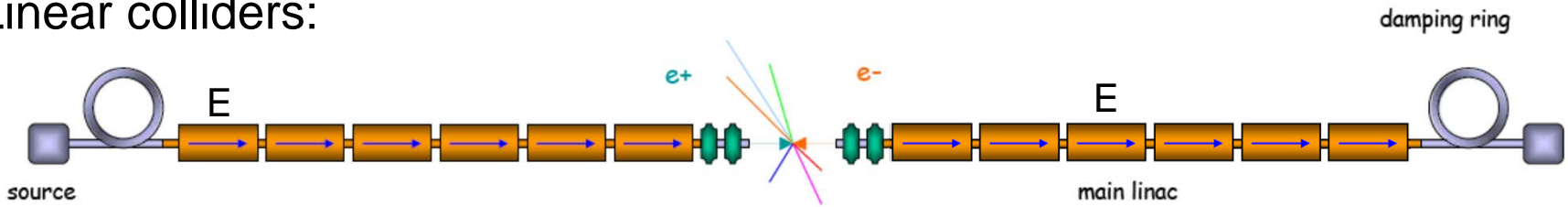


protons
at 920 GeV

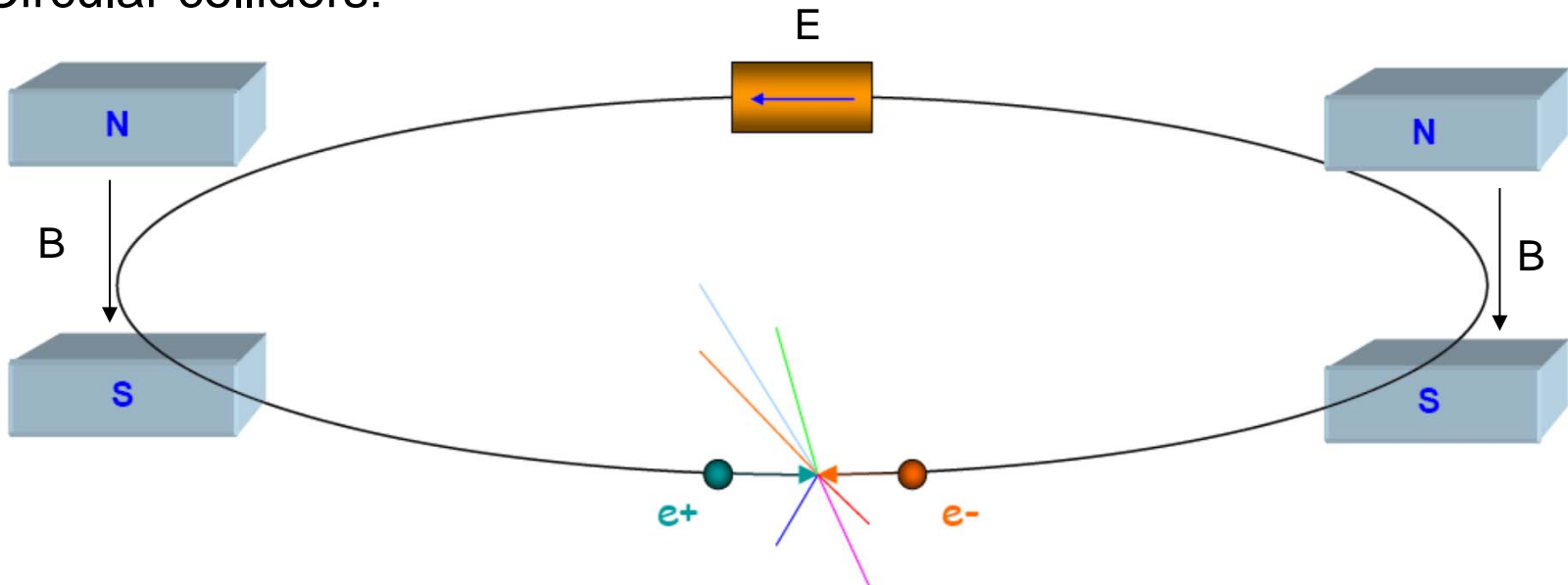
electrons at 27.5 GeV

Circular and linear colliders

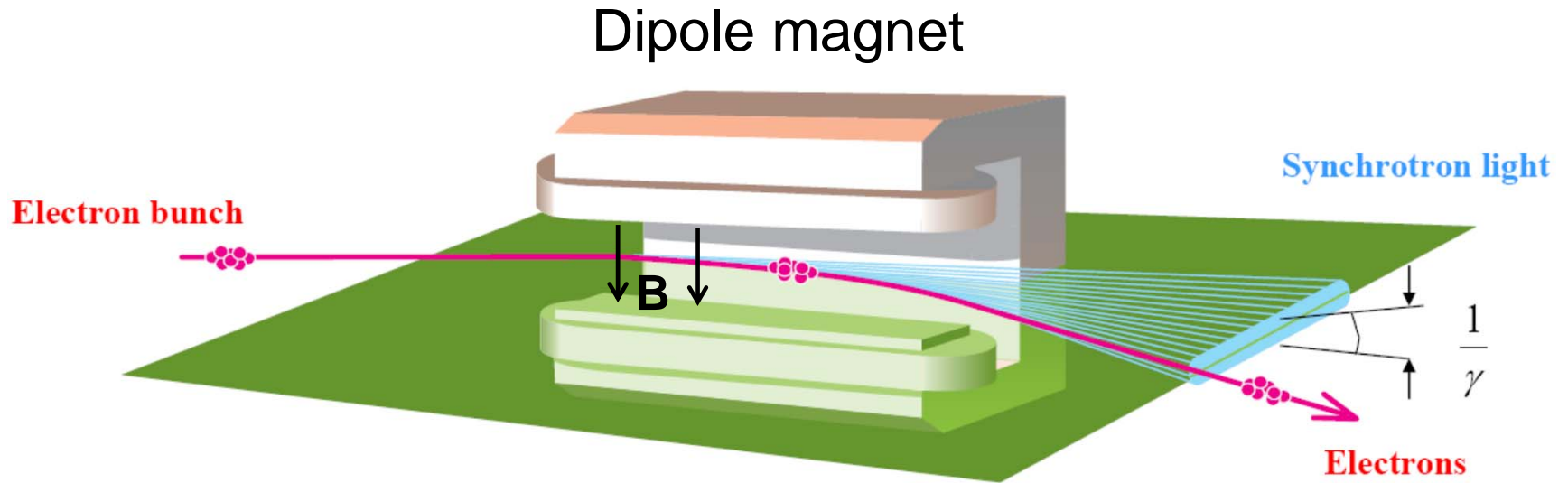
Linear colliders:



Circular colliders:



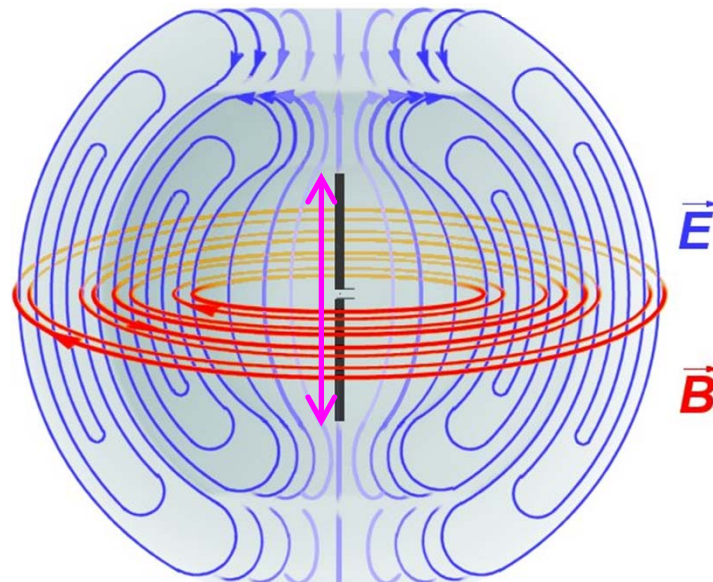
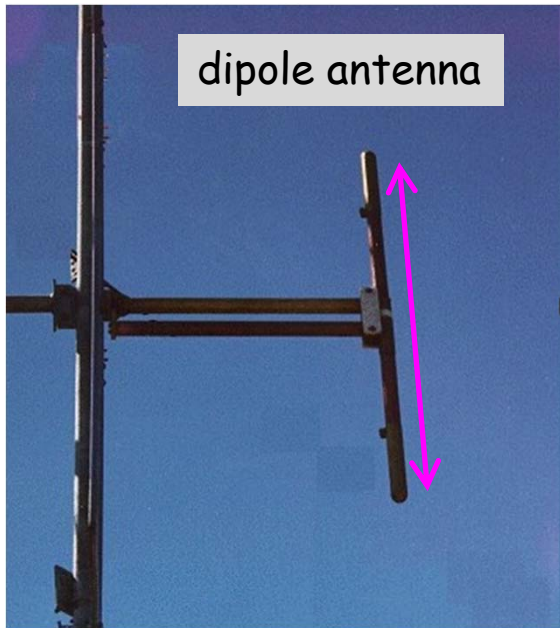
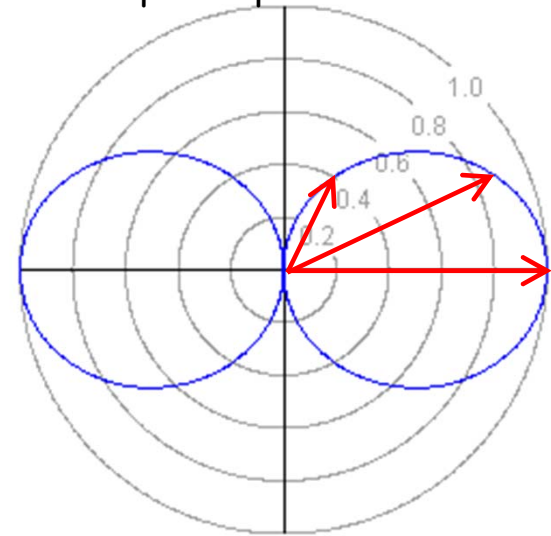
Synchrotron radiation



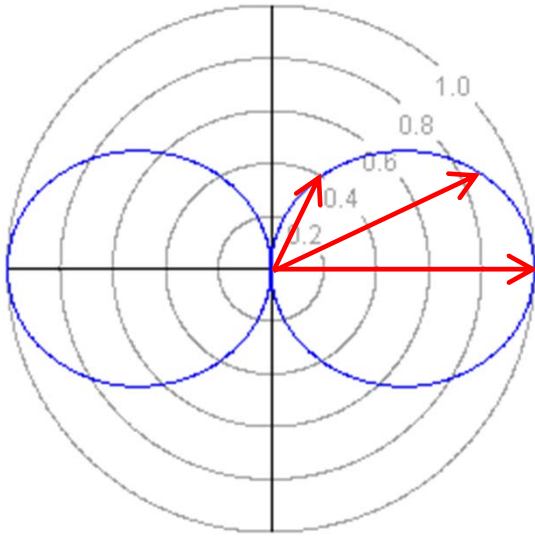
Radio antenna



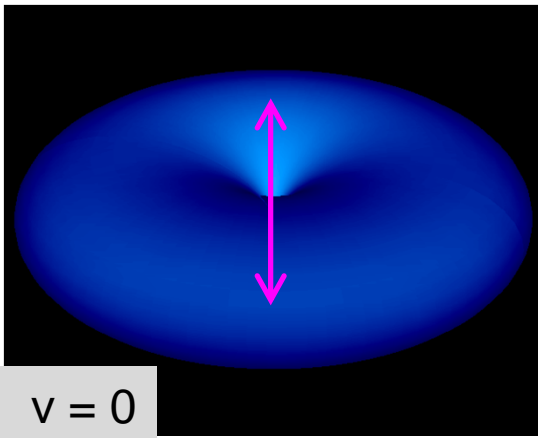
radiation power pattern:



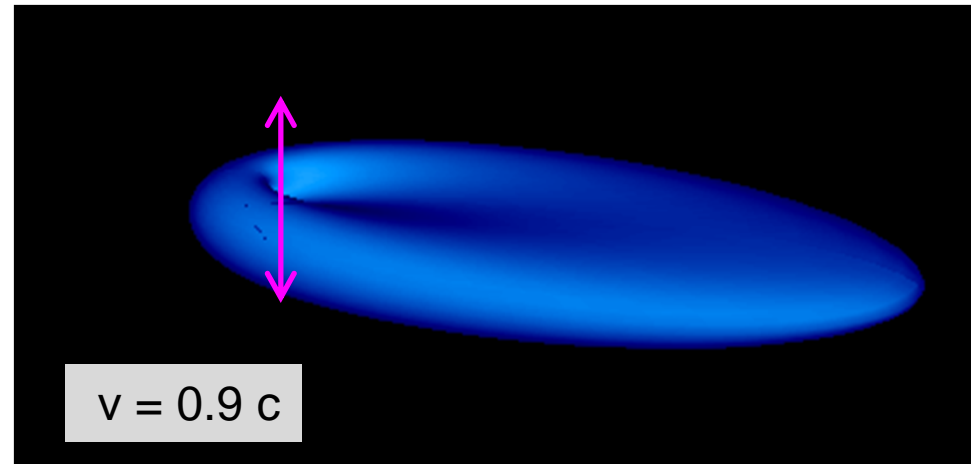
Radiation of a dipole antenna



Radiation of an oscillating dipole



Radiation of a moving oscillating dipole



Radiation of a dipole antenna

local oscillator:

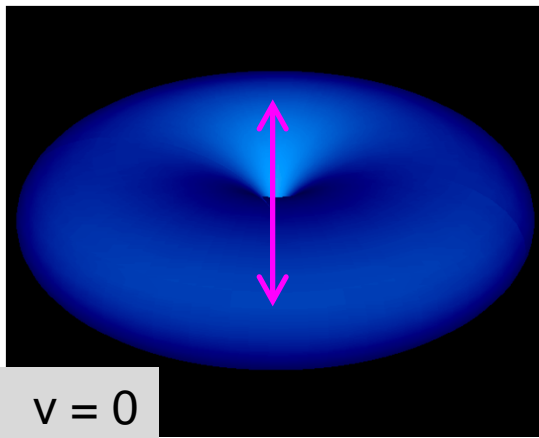
$$P = \frac{q^2 a^2}{12\pi\epsilon_0 c^3} \omega^4$$

(oscillation amplitude: $a < \lambda$)

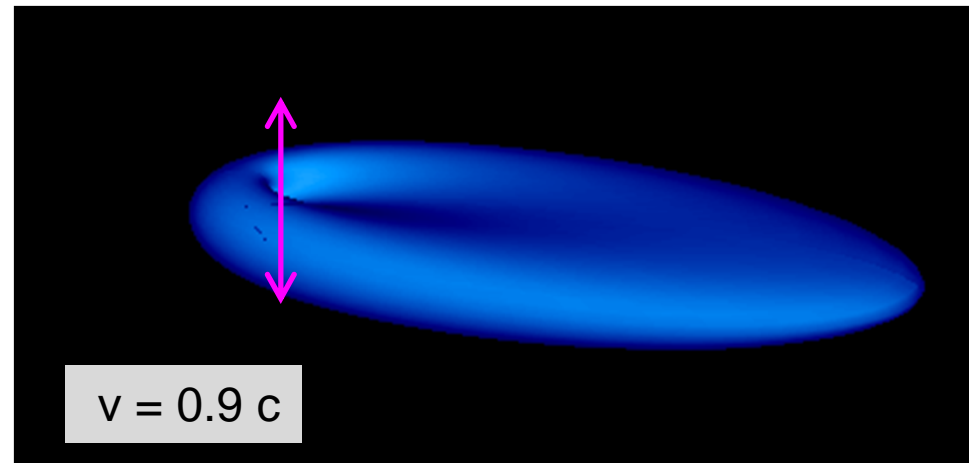
moving oscillator:

$$P = \frac{q^2 a^2}{12\pi\epsilon_0 c^3} \gamma^4 \omega^4$$
$$\gamma = \frac{E}{m_0 c^2}$$

Radiation of an oscillating dipole



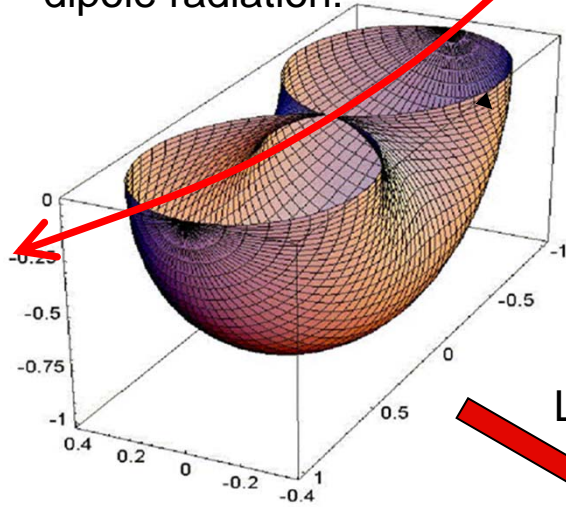
Radiation of a moving oscillating dipole



Radiation of a oscillating dipole under relativistic conditions

dipole radiation:

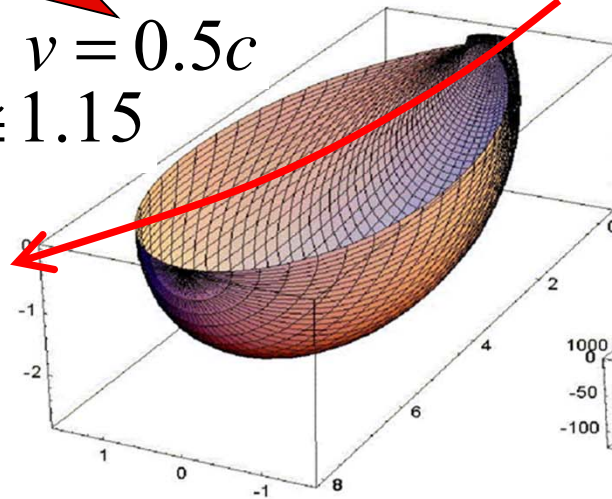
electron trajectory



DORIS: $\gamma = 8900$
PETRA: $\gamma = 12000$

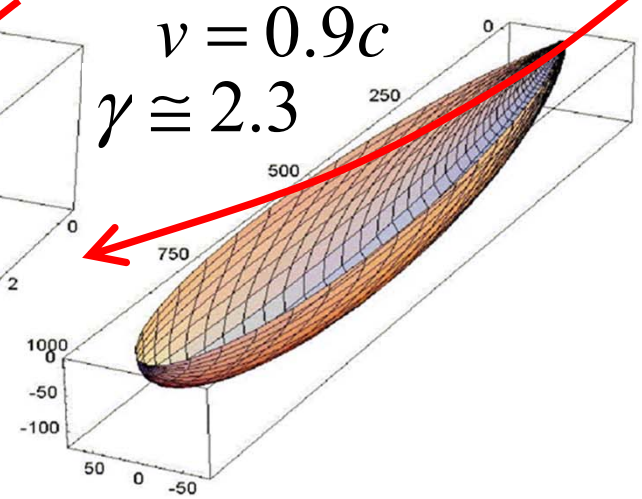
Lorentz-contraction

$v = 0.5c$
 $\gamma \cong 1.15$



electron trajectory

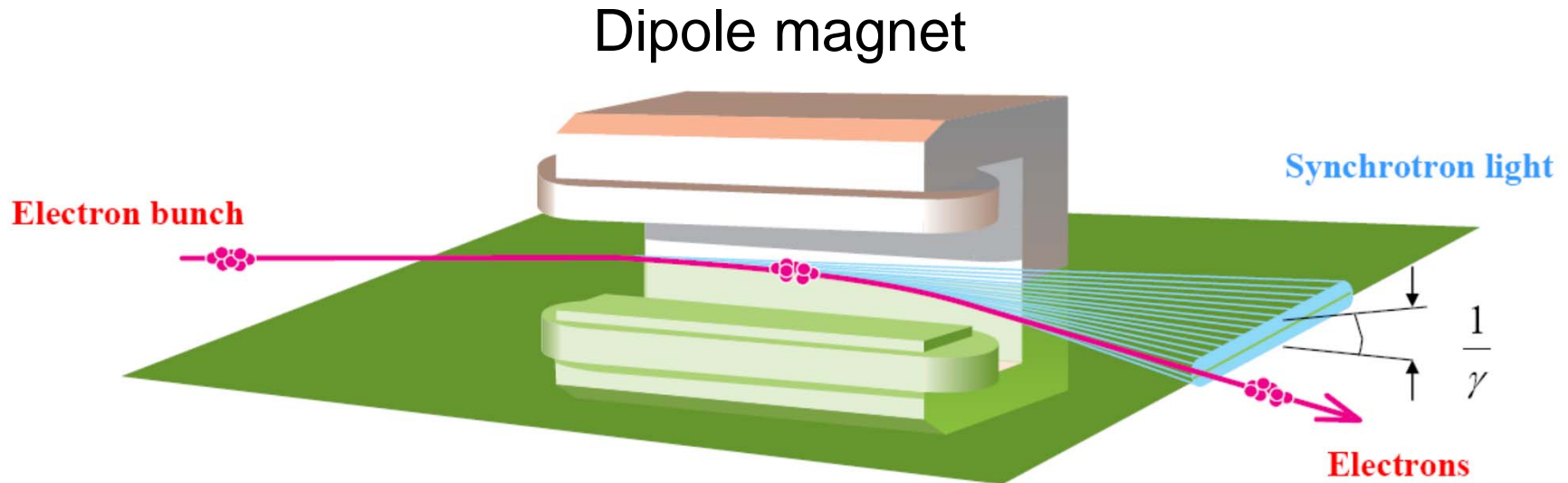
$v = 0.9c$
 $\gamma \cong 2.3$



electron trajectory



Synchrotron radiation



Power radiated by one electron in a dipole field B :

$$P = \frac{c q^2}{6\pi \epsilon_0} \frac{\gamma^4}{r^2}$$

$$\gamma = \frac{E}{m_0 c^2}$$

$$\frac{1}{r} = \frac{q B}{p}$$

vacuum permittivity

Synchrotron radiation

Total energy loss after one full turn:

$$\Delta E_{\text{turn}} = \frac{q^2}{3\epsilon_0} \frac{\gamma^4}{r} \quad \Rightarrow \quad \Delta E_{\text{turn}} [\text{GeV}] = 6.032 \times 10^{-18} \frac{\gamma^4}{r[\text{m}]}$$

HERA electron ring:

$$r = 580 \text{ m}$$

$$E = 27.5 \text{ GeV}$$

$$\gamma = 54000$$

$$\Delta E_{\text{turn}} = 87 \text{ MeV (0.3\%)}$$

HERA proton ring:

$$r = 580 \text{ m}$$

$$E = 920 \text{ GeV}$$

$$\gamma = 980$$

$$\Delta E_{\text{turn}} \cong 10 \text{ eV (10}^{-9}\text{\%)}$$

← same →

need acceleration = 87 MV per turn



Synchrotron radiation

Total energy loss after one full turn:

$$\Delta E_{\text{turn}} = \frac{q^2}{3\epsilon_0} \frac{\gamma^4}{r} \quad \Rightarrow \quad \Delta E_{\text{turn}} [\text{GeV}] = 6.032 \times 10^{-18} \frac{\gamma^4}{r[\text{m}]}$$

HERA electron ring:

$$r = 580 \text{ m}$$

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$$\Delta E_{\text{turn}} = 87 \text{ MeV (0.3\%)}$$

need acceleration = 87 MV per turn

HERA proton ring:

$$r = 580 \text{ m}$$

$$E = 920 \text{ GeV}$$

$$\gamma = 980$$

← same →

the limit is the max. dipole field = 5.5 Tesla

$$\frac{1}{r} = \frac{qB}{p}$$



Synchrotron radiation

Total energy loss after one full turn:

$$\Delta E_{\text{turn}} = \frac{q^2}{3\epsilon_0} \frac{\gamma^4}{r} \Rightarrow \Delta E_{\text{turn}} [\text{GeV}] = 6.032 \times 10^{-18} \frac{\gamma^4}{r[\text{m}]}$$

HERA electron ring:

$$r = 580 \text{ m}$$

$$E = 27.5 \text{ GeV}$$

$$\gamma = 54000$$

$$\Delta E_{\text{turn}} = 87 \text{ MeV (0.3\%)}$$

need acceleration = 87 MV per turn

LEP collider:

$$r = 2800 \text{ m}$$

$$E = 105 \text{ GeV}$$

$$\gamma = 205000$$

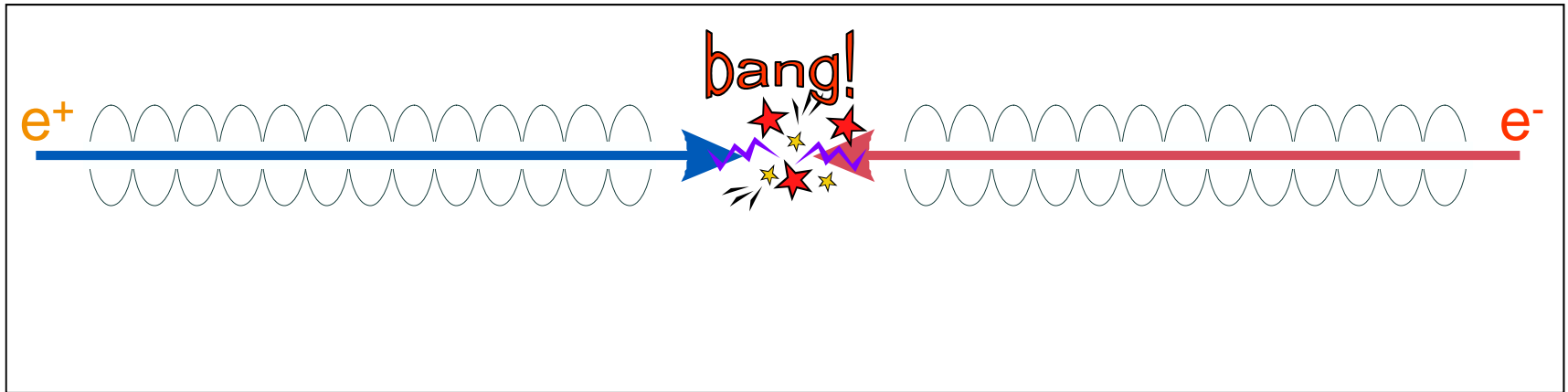
$$\Delta E_{\text{turn}} \cong 4 \text{ GeV (4\%)}$$

need 4 GV per turn !!



Project for a future e-e+ collider: ILC

The International Linear Collider

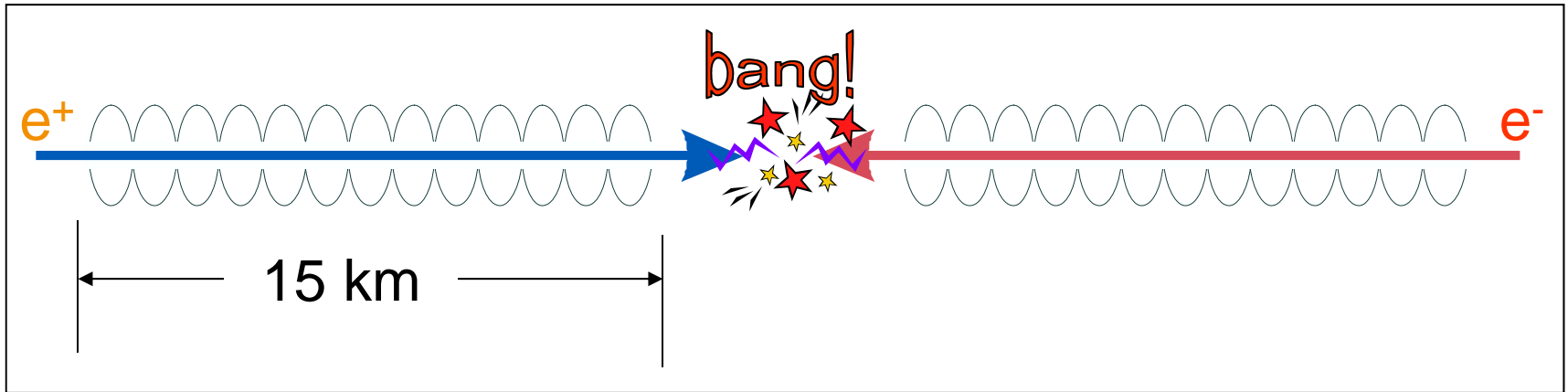


Colliding beams with $E_{CM} = 500 \text{ GeV}$

more about ILC: lecture on 'Linear Collider' by S. Riemann (24th Aug.)

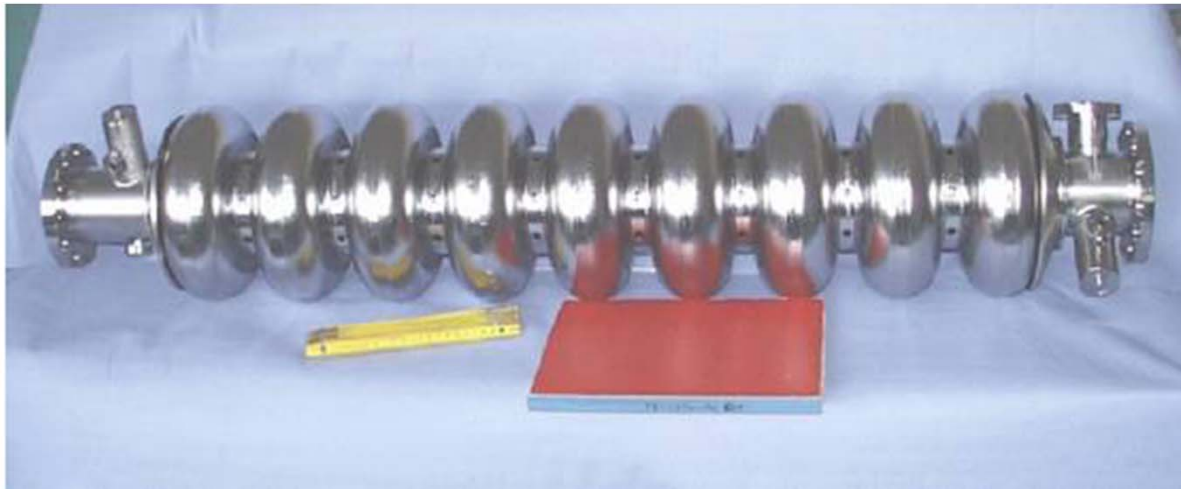
Project for a future e^-e^+ collider: ILC

The International Linear Collider



Colliding beams with $E_{CM} = 500 \text{ GeV}$

using superconducting cavities for acceleration:

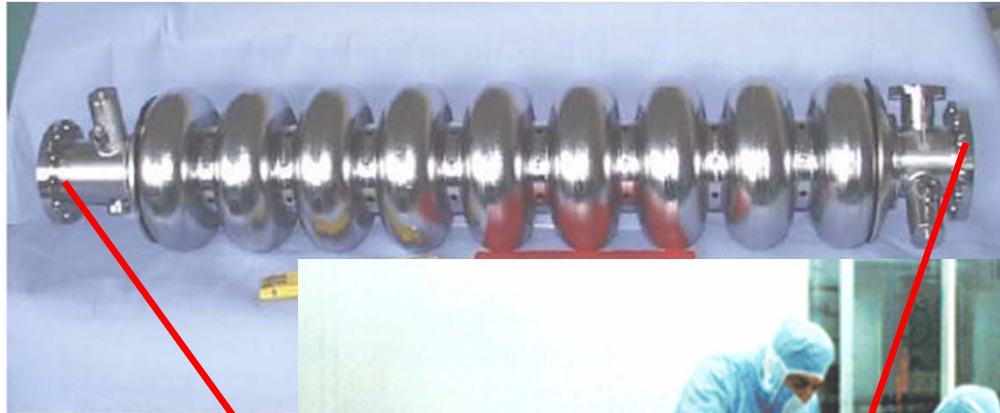


Superconducting cavities for acceleration

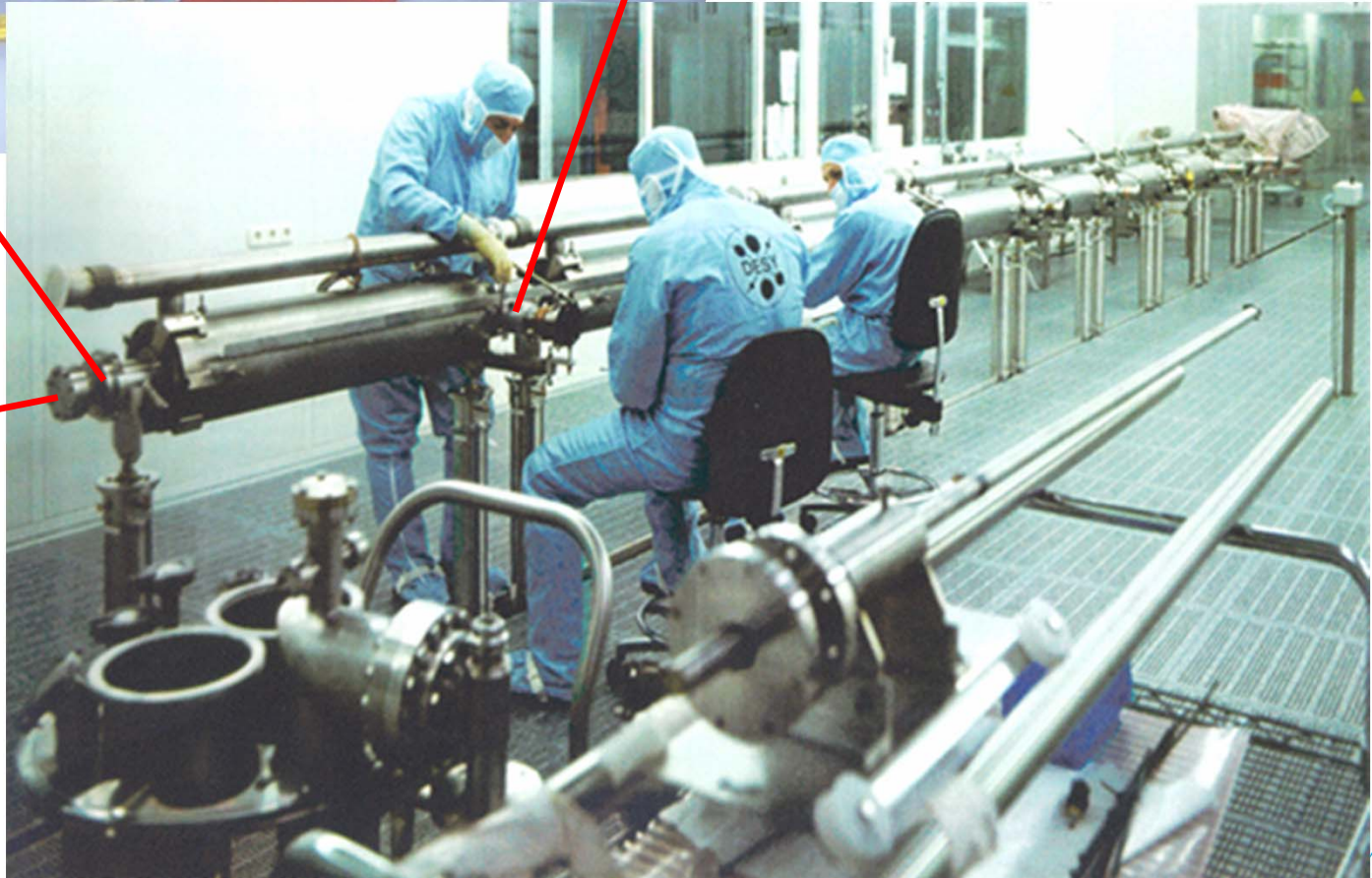


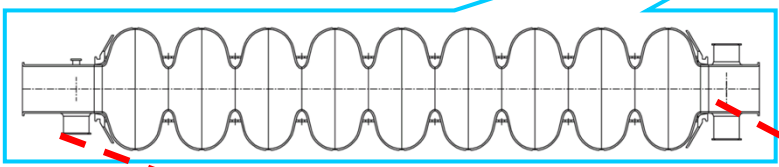
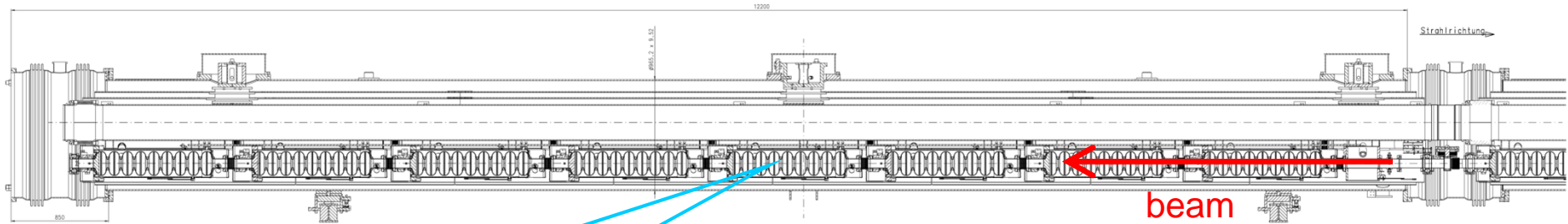
- International Linear Collider (ILC)
(future project)
- European X-ray Free-Electron Laser (XFEL)
(in construction)
- Free-electron LASer in Hamburg (FLASH)
(in operation)

Cavities inside a cryostat



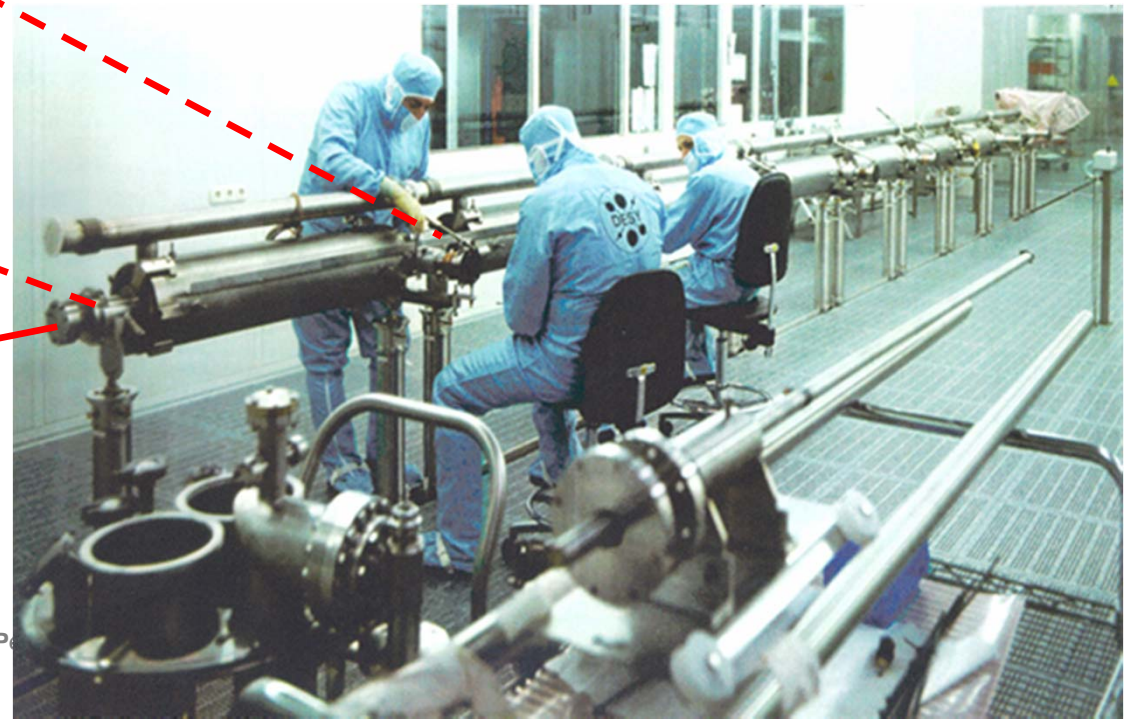
beam



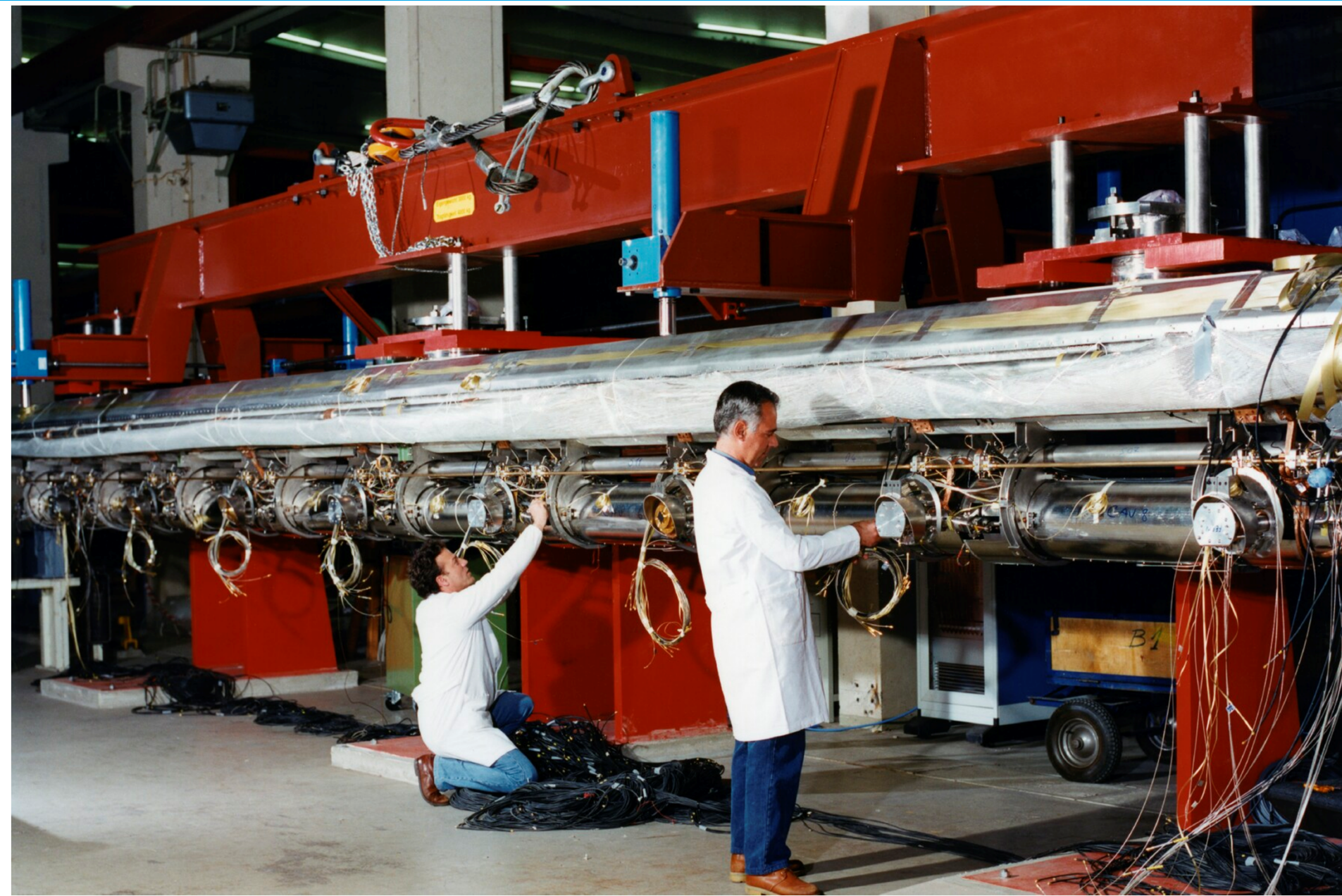


Number of cavities	8
Cavity length	1.038 m
Operating frequency	1.3 GHz
Operating temperature	2 K
Accelerating Gradient	23..35 MV/m

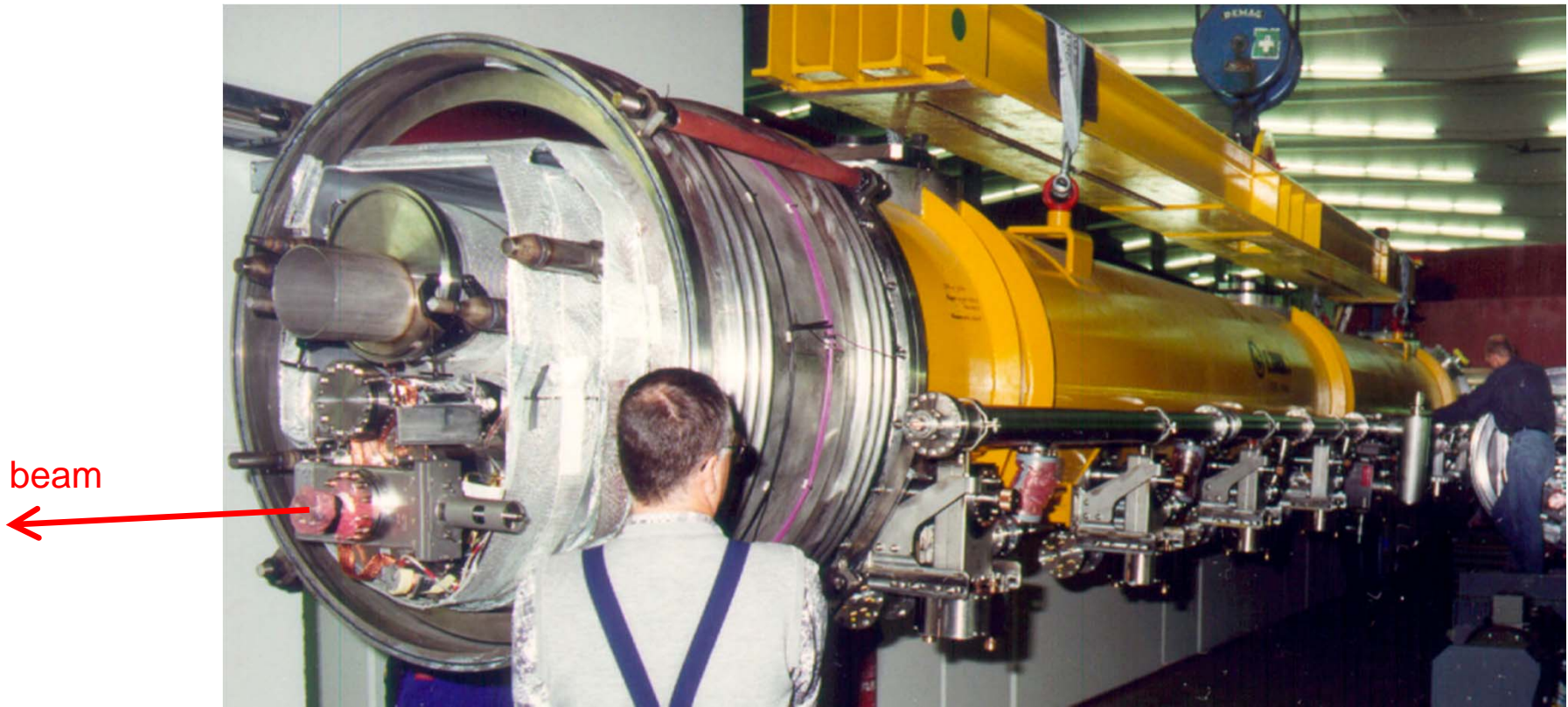
← beam



Cavities inside a cryostat

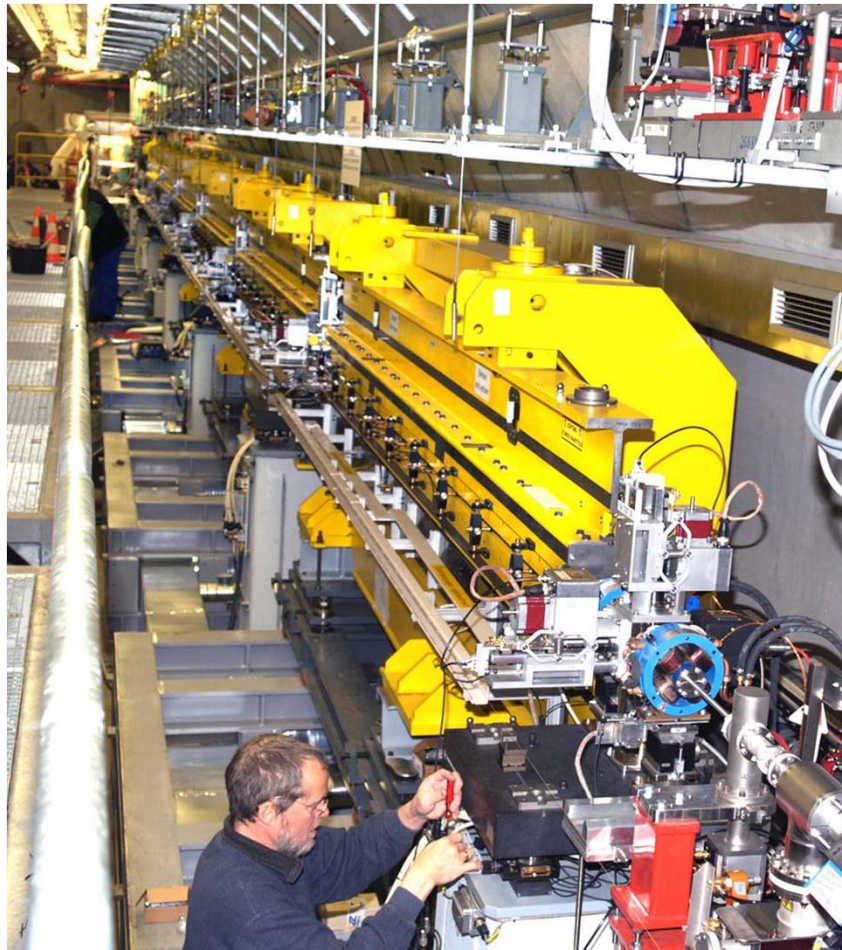


Cavities inside a cryostat



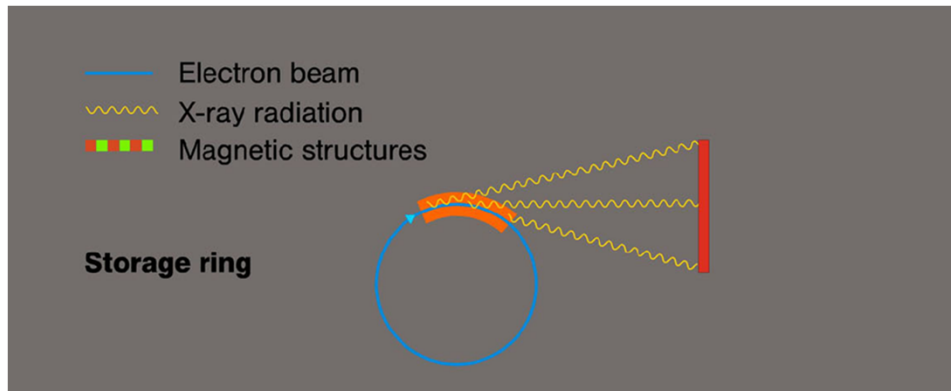
module installation in FLASH (2004)

Undulators for Free-Electron Laser



- International Linear Collider (ILC)
(future project)
- European X-ray Free-Electron Laser (XFEL)
(in construction)
- Free-electron LASer in Hamburg (FLASH)
(in operation)

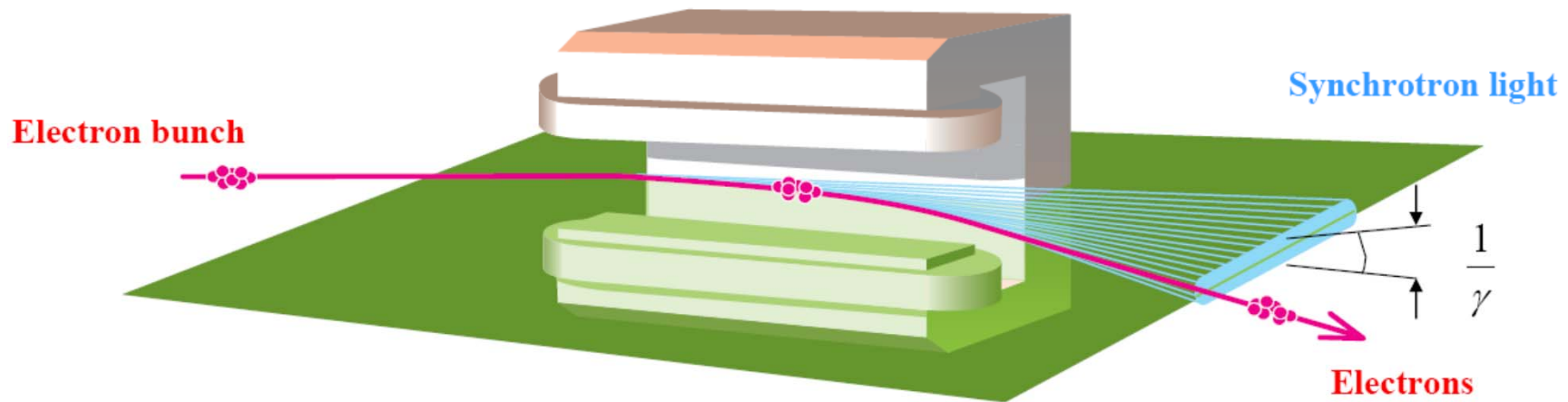
Increase of number of photons



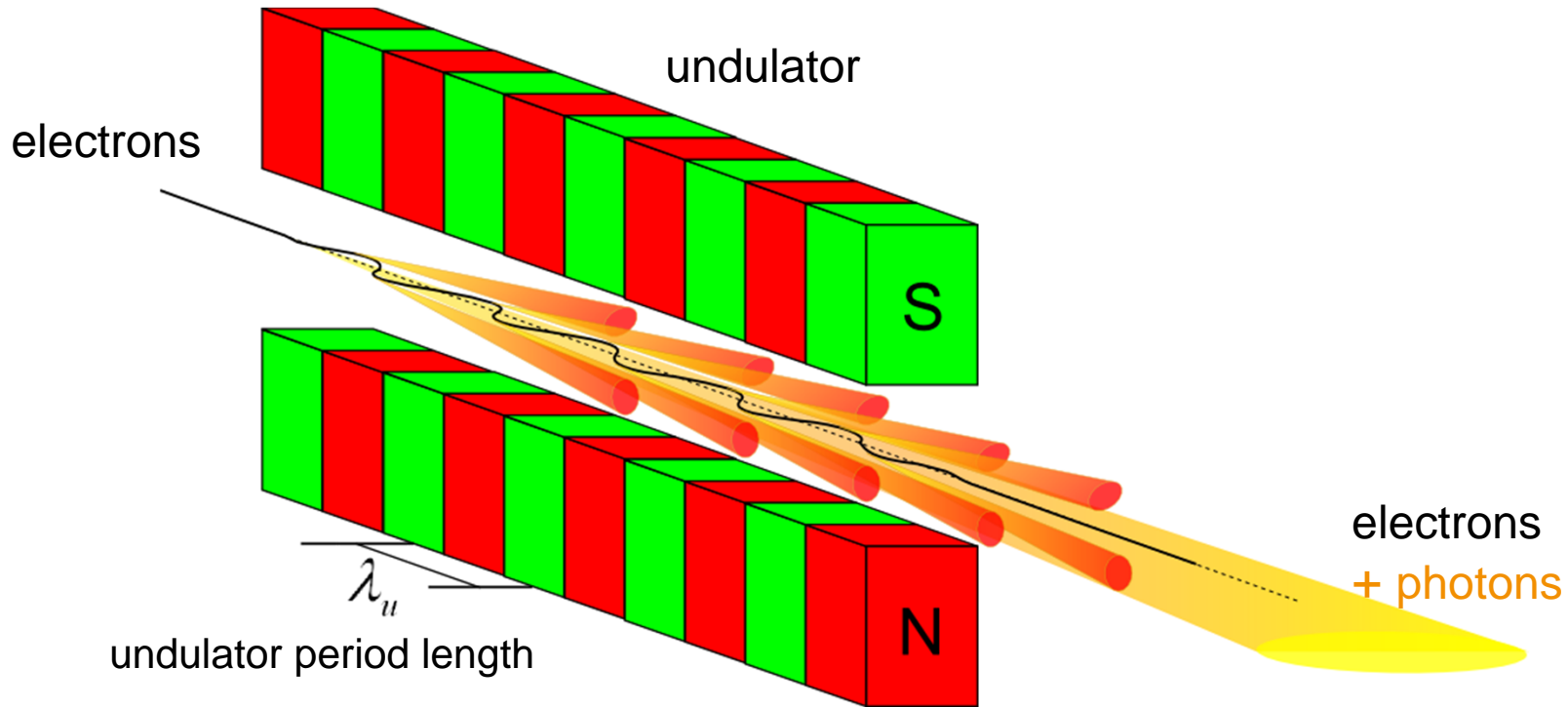
Power radiated by one electron
in a dipole field

$$P_{\text{ph}} = N_e \times P_{\text{dipole}}$$

Bending Magnet

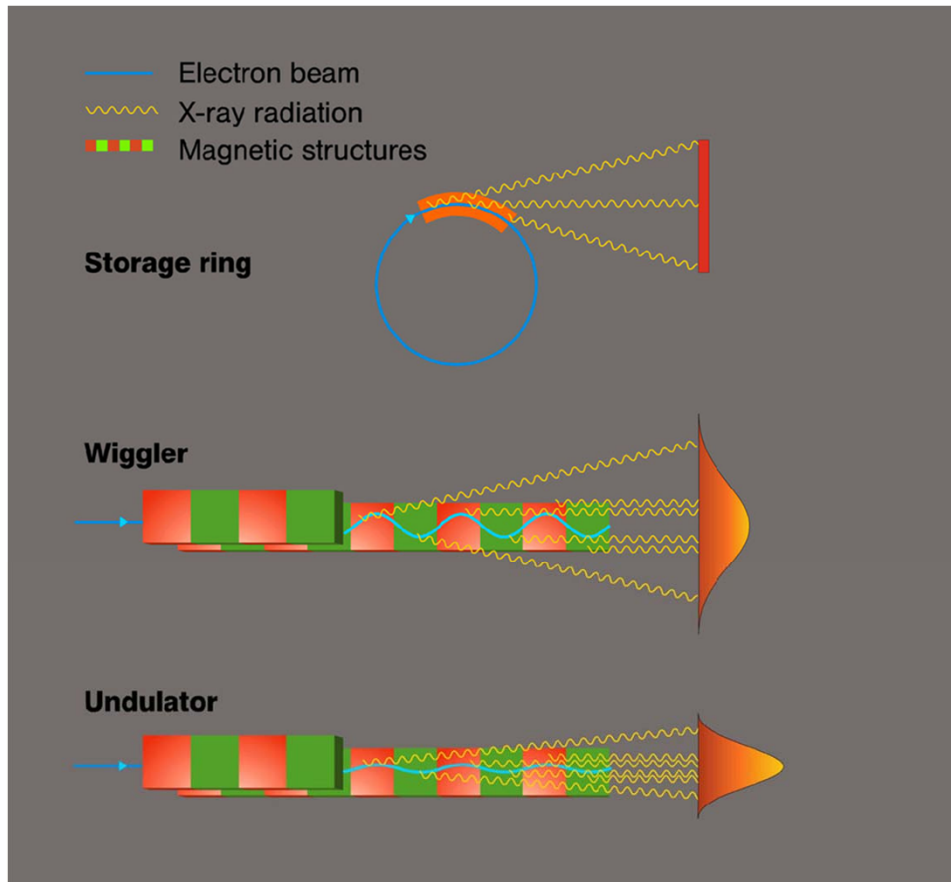


Motion of electrons inside an undulator magnet



Example: undulator at FLASH: $\lambda_u = 27 \text{ mm}$, $\hat{x} = 2.6 \mu\text{m}$

Increase of number of photons



Photon brilliance emitted by an electron bunch in a dipole field

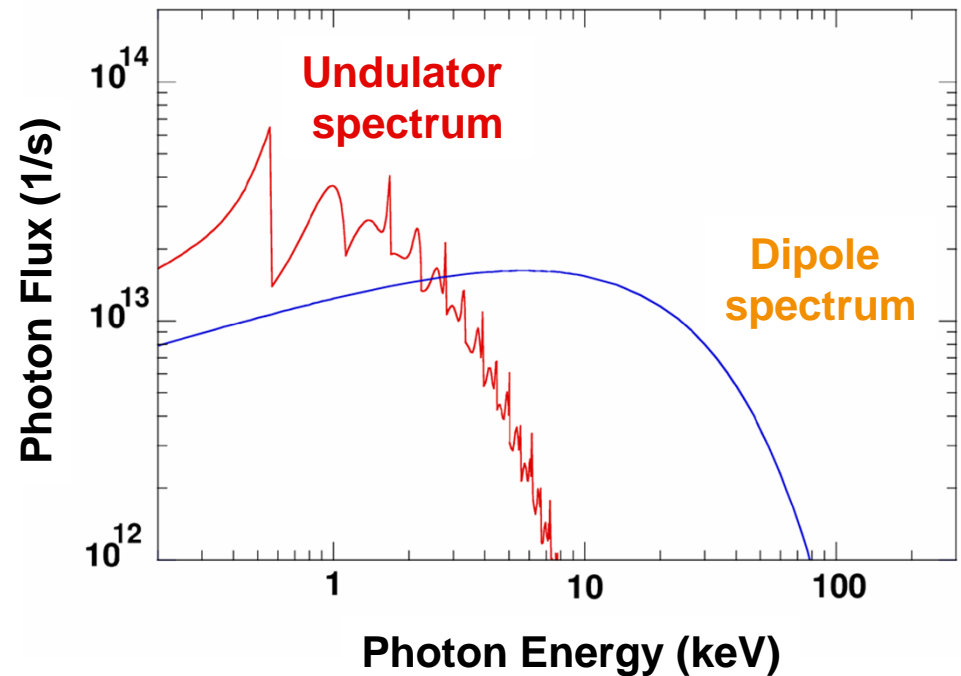
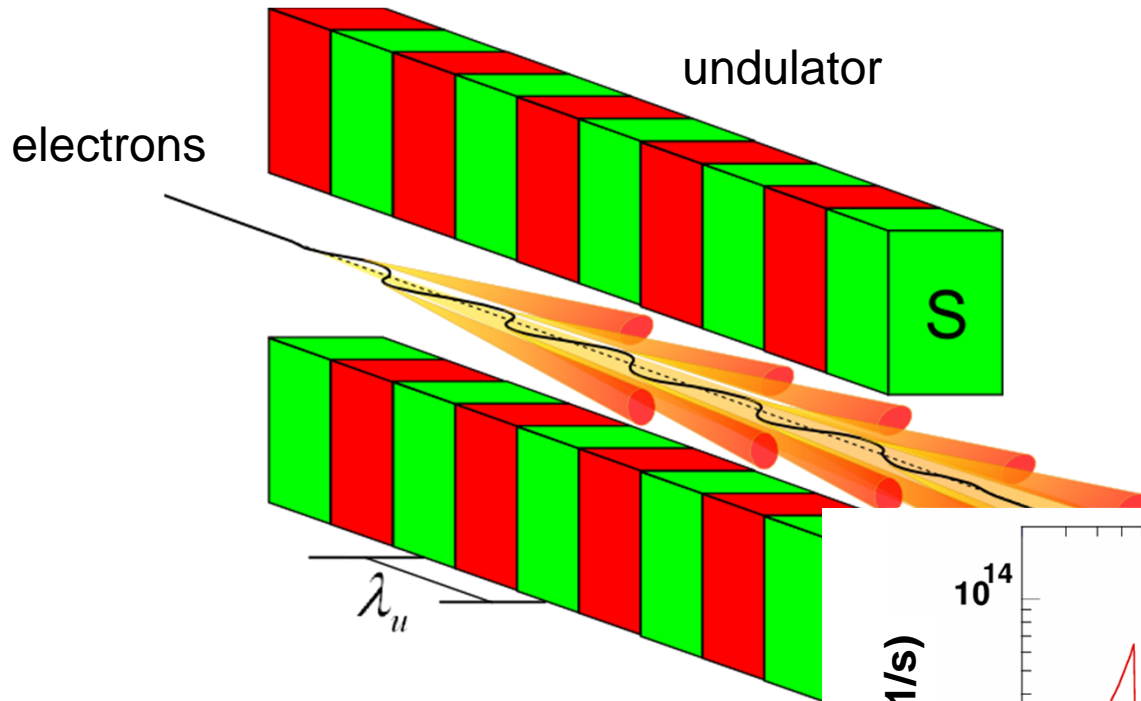
B_{dipole}

$$B = B_{\text{dipole}} \times N_{\text{dipole}}$$

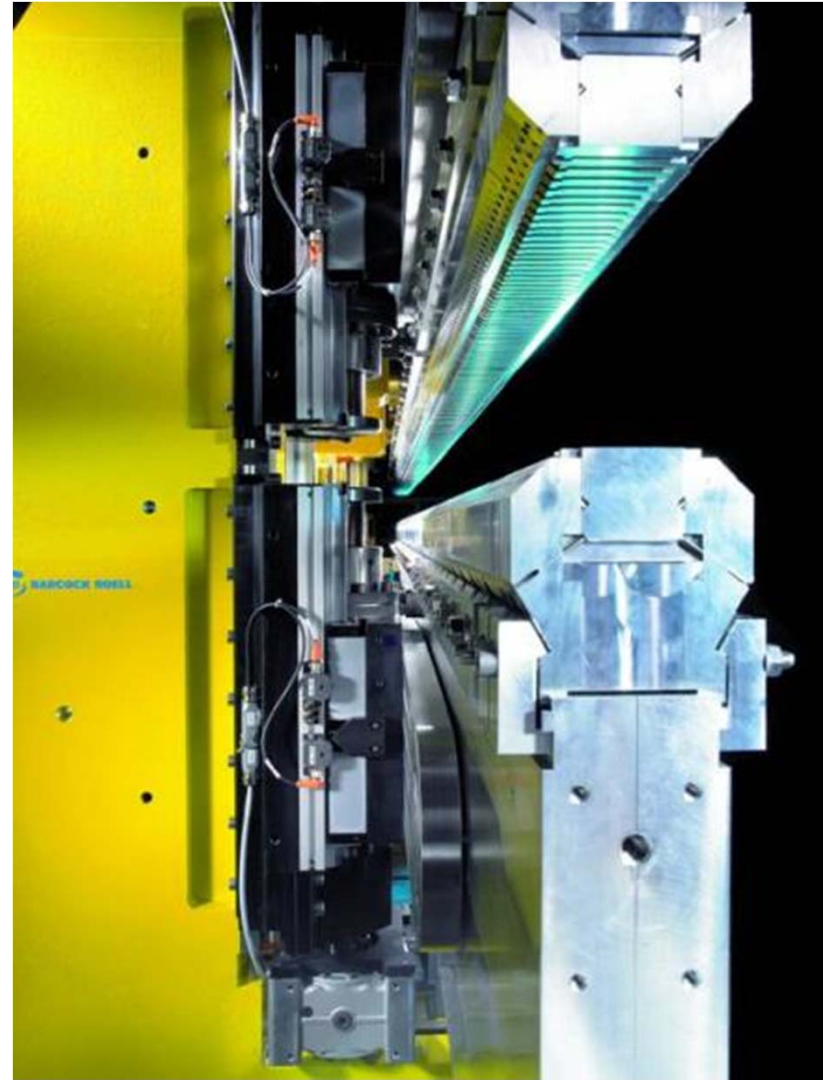
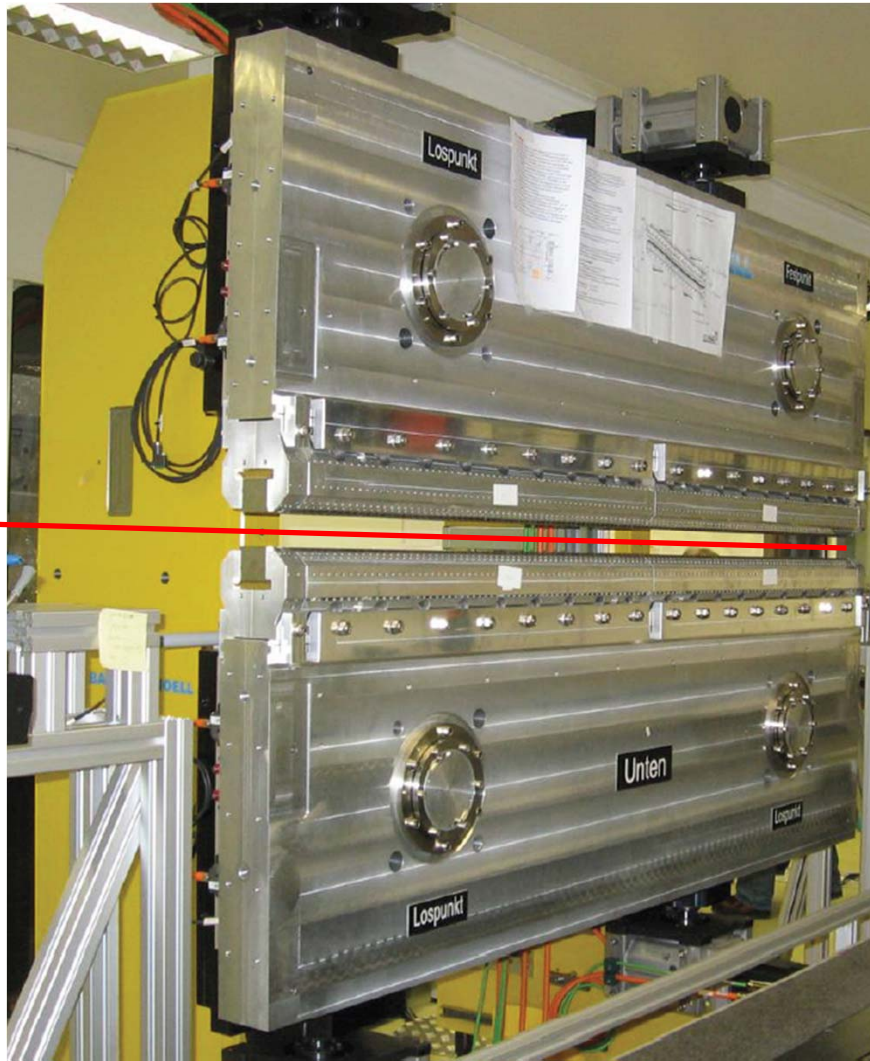
$$B \propto B_{\text{dipole}} \times N_{\text{dipole}}^2$$

$$\text{Brilliance} = \frac{\text{photons / s / 0.1\% bandwidth}}{\text{source area} \times \text{solid angle}} = \frac{\text{spectral flux}}{\text{source area} \times \text{solid angle}}$$

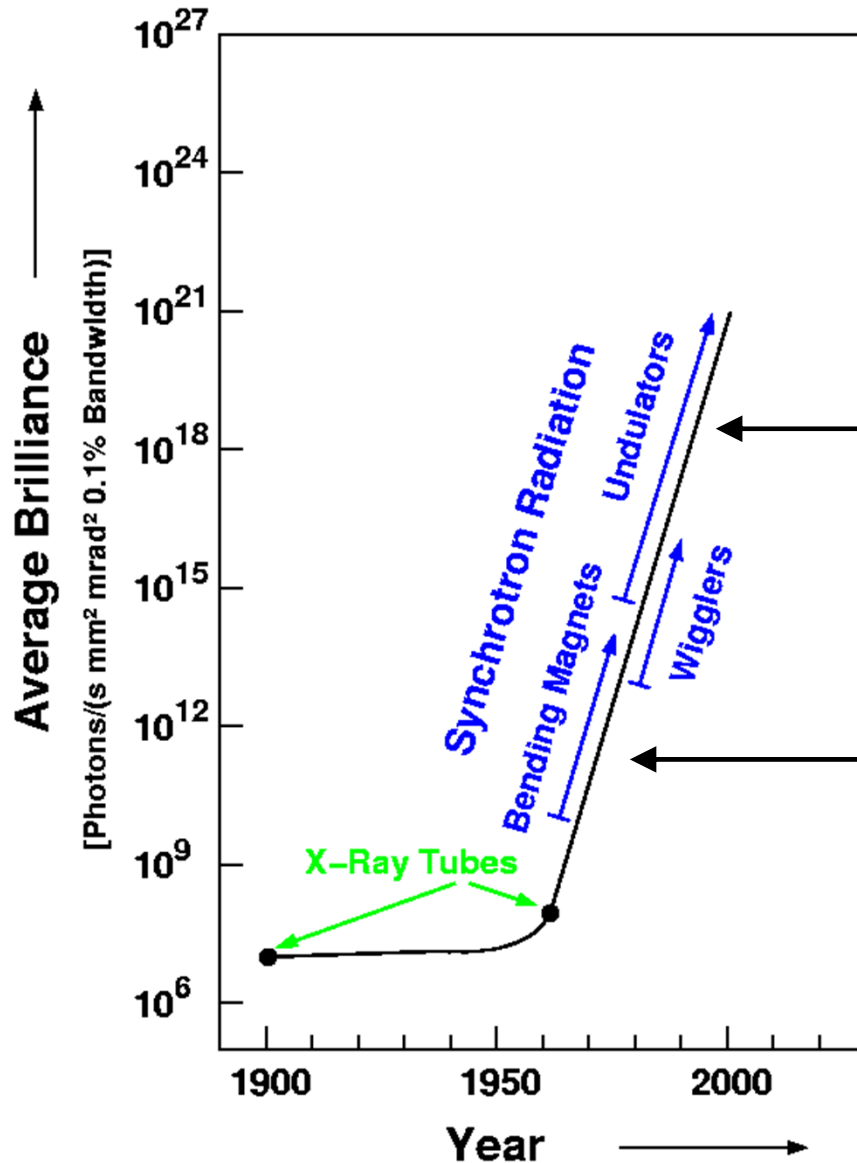
Motion of electrons inside an undulator magnet



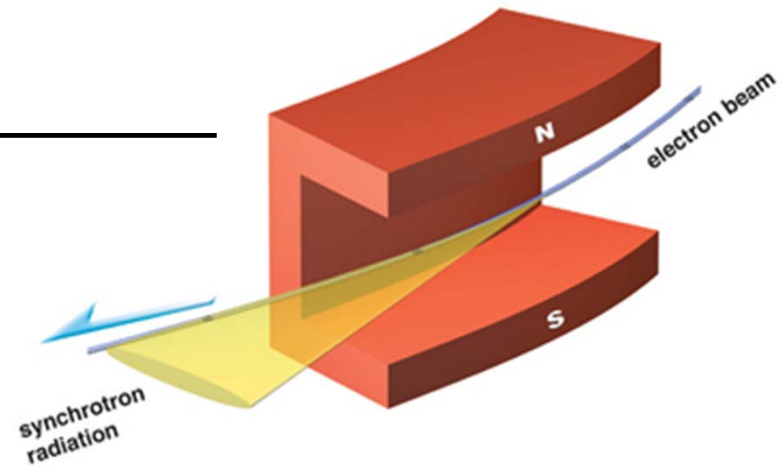
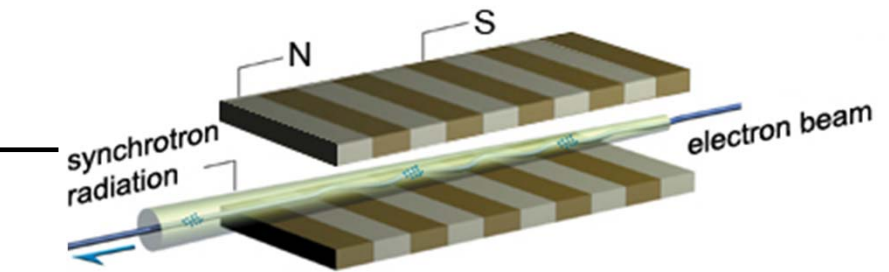
Undulators



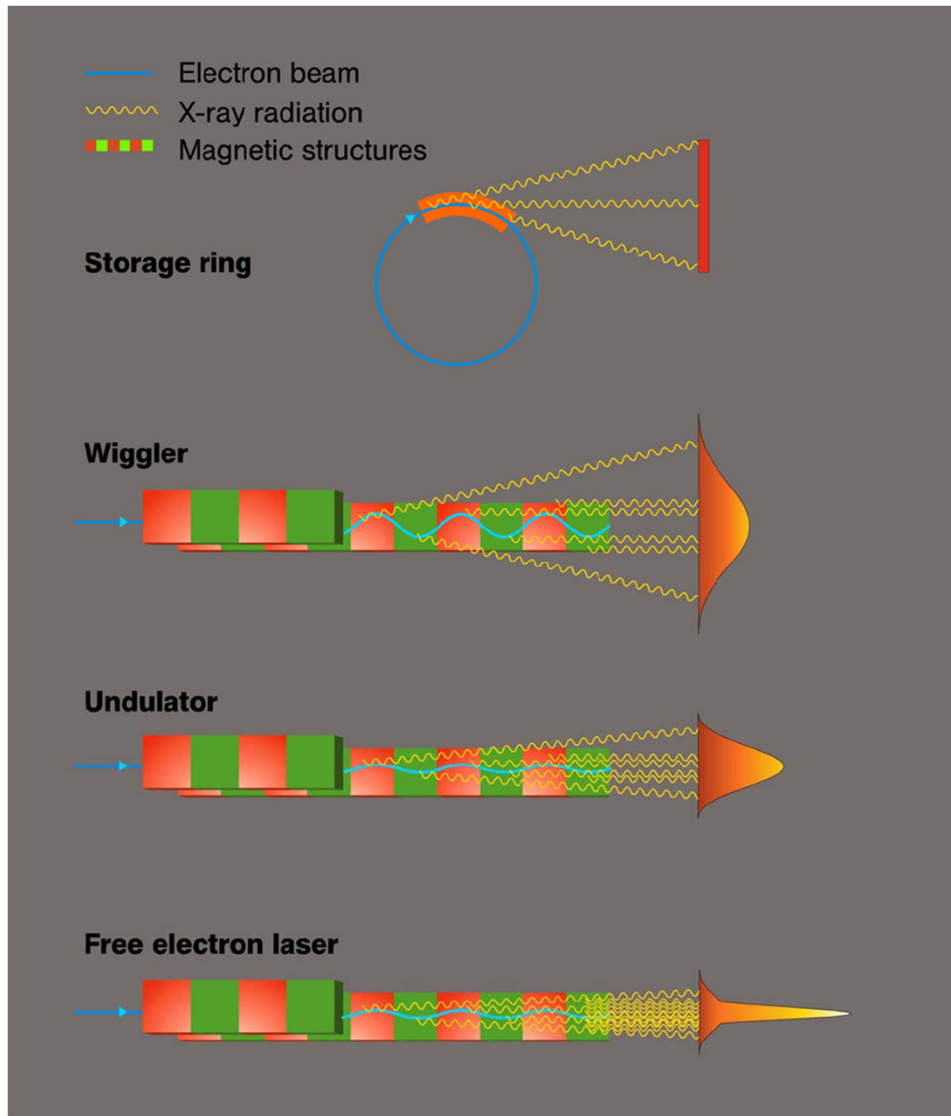
Development of synchrotron light sources



$$\text{Brilliance} = \frac{\text{photons / s / 0.1\% bandwidth}}{\text{source area} \times \text{solid angle}}$$



Increase of number of photons



Photon brilliance emitted by an electron bunch in a dipole field

$$B_{\text{dipole}}$$

$$B = B_{\text{dipole}} \times N_{\text{dipole}}$$

$$B \propto B_{\text{dipole}} \times N_{\text{dipole}}^2$$

$$B \propto N_e \times B_{\text{dipole}} \times N_{\text{dipole}}^2$$

... and you need a very long undulator



6 undulators (4.5 m long) at FLASH

- European X-ray Free-Electron Laser (XFEL)
(in construction)

3.4 km, 18 GeV, 0.1 nm

- Free-electron LASer in Hamburg (FLASH)
(in operation)

300 m, 1.2 GeV, 4.1 nm

<http://xfel.desy.de>

<http://flash.desy.de>

Free-electron LASer in Hamburg (FLASH)

300 m, 1.2 GeV, 4.1 nm

accelerator control room



- 01-01f Laborgebäude 1
- 01,01a Bibliothek
- 01c Direktorium
- 02a Laborgebäude 2a
- 02b Rechenzentrum, UCO
- 02g Laborgebäude
- 03 Laborgebäude 3
- 03a Hausmeister
- 14 Vakuumlabor
- 15a Gästehaus 6
- 15b Gästehaus 7

50 HERA Halle West



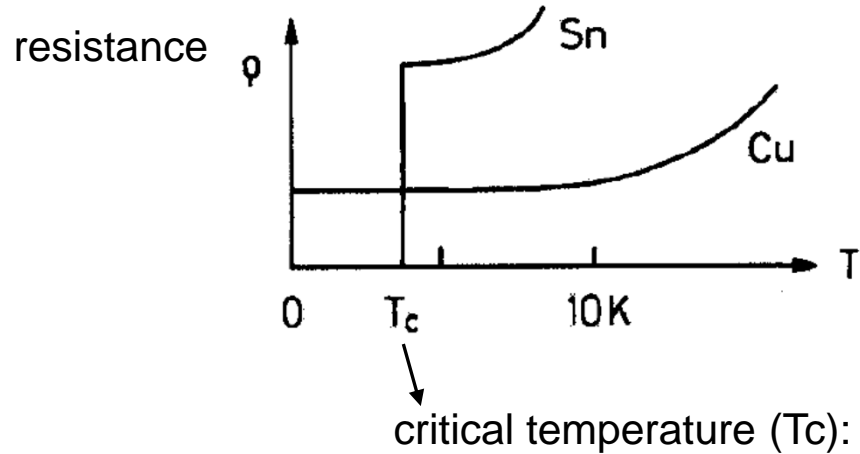
Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

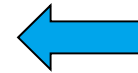
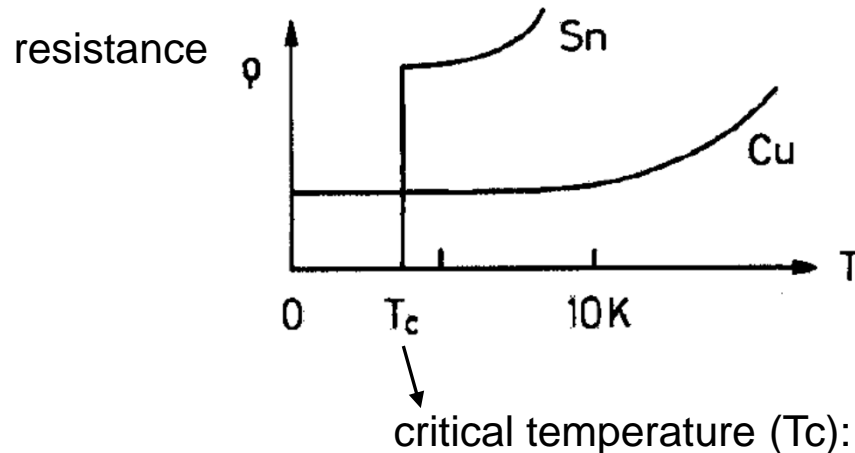
	superconducting cavity	normal conducting cavity	
for $E = 1 \text{ MV/m}$	0 ??	56 kW / m	dissipated at the cavity walls



Advantages of RF superconductivity



Advantages of RF superconductivity



for DC currents !

at radio-frequencies, there is a "microwave surface resistance"
which typically is 5 orders of magnitude lower than R of copper

Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

	superconducting cavity	normal conducting cavity	
for $E = 1 \text{ MV/m}$	1.5 W / m	56 kW / m	dissipated at the cavity walls



Advantages of RF superconductivity

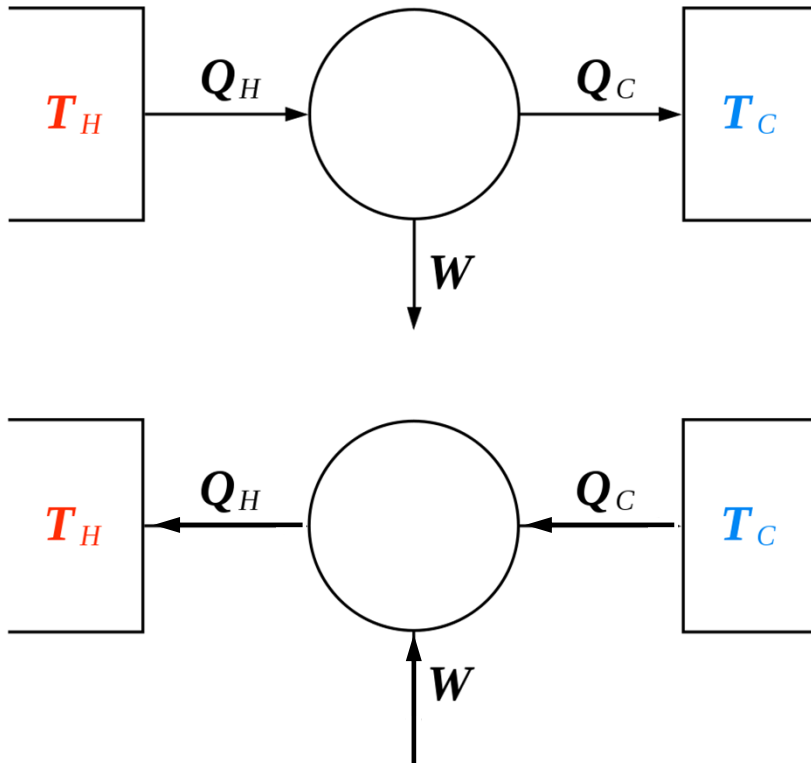
Example: comparison of 500 MHz cavities:

	superconducting cavity	normal conducting cavity	
for $E = 1 \text{ MV/m}$	1.5 W / m at 2 K	56 kW / m	dissipated at the cavity walls



2nd law of Thermodynamics

“Heat cannot spontaneously flow from a colder location to a hotter location”



max. efficiency

$$\eta_c = \frac{T_H - T_C}{T_H}$$

Carnot efficiency:

$$\eta_c = \frac{T_C}{T_H - T_C}$$

most common applications

thermal power stations,
cars, ...

air conditioners,
refrigerators, ...



Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

	superconducting cavity	normal conducting cavity	
for E = 1 MV/m	1.5 W / m at 2 K	56 kW / m	dissipated at the cavity walls
Carnot efficiency:	$\eta_c = \frac{T}{300 - T} = 0.007$		x cryogenics efficiency 20-30%



Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

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for E = 1 MV/m	1 kW / m	56 kW / m	



Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

	superconducting cavity	normal conducting cavity	
for E = 1 MV/m	1.5 W / m at 2 K	56 kW / m	dissipated at the cavity walls
Carnot efficiency: $\eta_c = \frac{T}{300 - T} = 0.007$ x			cryogenics efficiency 20-30%
for E = 1 MV/m	1 kW / m	56 kW / m	
for E = 1 MV/m	1 kW / m	112 kW / m	including RF generation efficiency (50%)



Advantages of RF superconductivity

Example: comparison of 500 MHz cavities:

	superconducting cavity	normal conducting cavity	
for E = 1 MV/m	1.5 W / m at 2 K	56 kW / m	dissipated at the cavity walls
Carnot efficiency: $\eta_c = \frac{T}{300 - T} = 0.007$ x			cryogenics efficiency 20-30%
for E = 1 MV/m	1 kW / m	56 kW / m	
for E = 1 MV/m	1 kW / m	112 kW / m	including RF generation efficiency (50%)

>100 (electrical) power reduction factor



Third summing-up

Beam focusing in synchrotrons: quadrupole magnets

Circular colliders (synchrotrons with $R=\text{const.}$):

	limitation
• proton synchrotrons	dipole magnet
• electron synchrotrons	synchrotron radiation

Linear accelerators:

- International Linear Collider (ILC)
 - European X-ray Free-Electron Laser (XFEL)
 - Free-electron LASer in Hamburg (FLASH)
- } based on S.C. cavities



Thank you for your attention

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