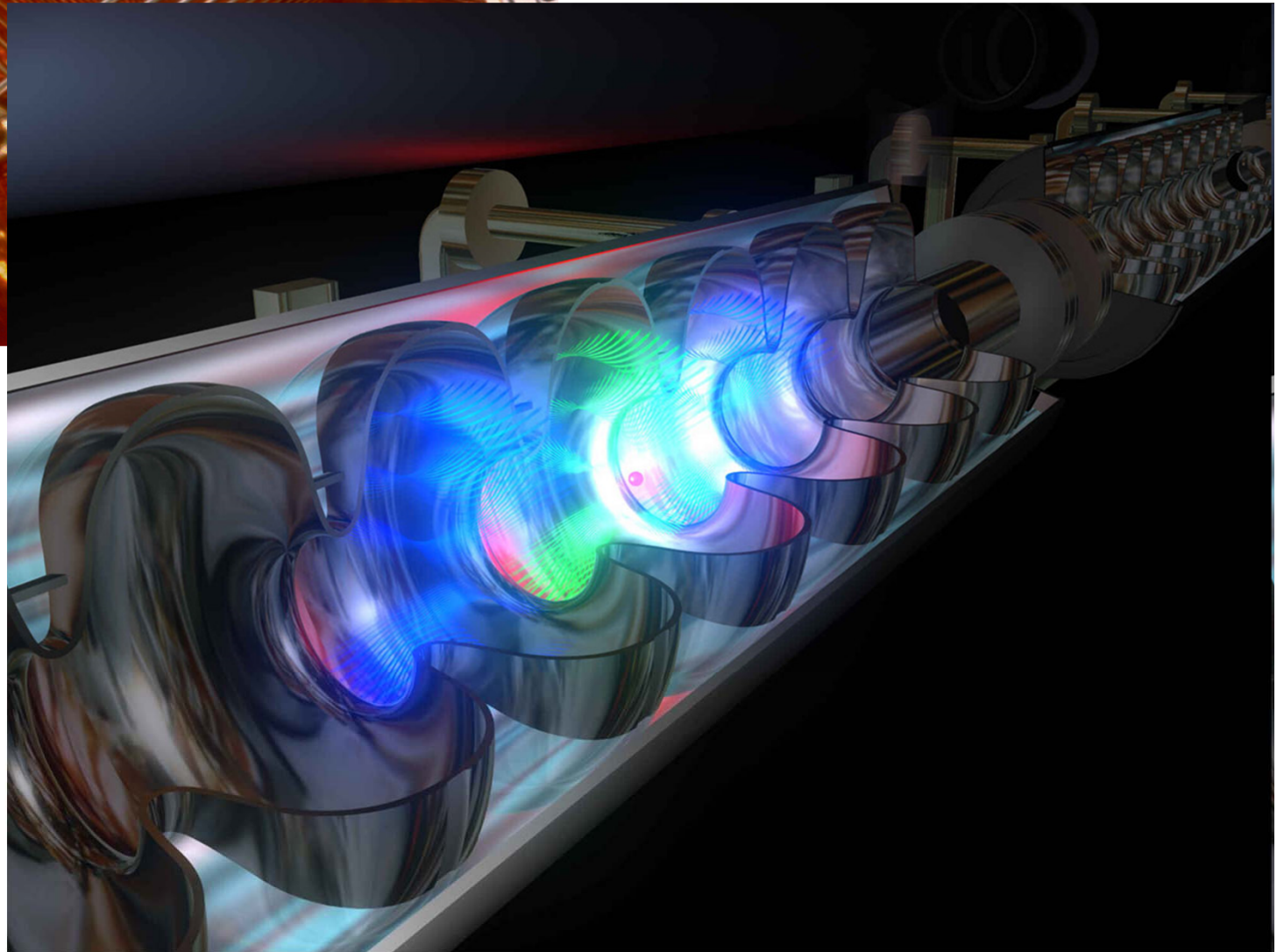
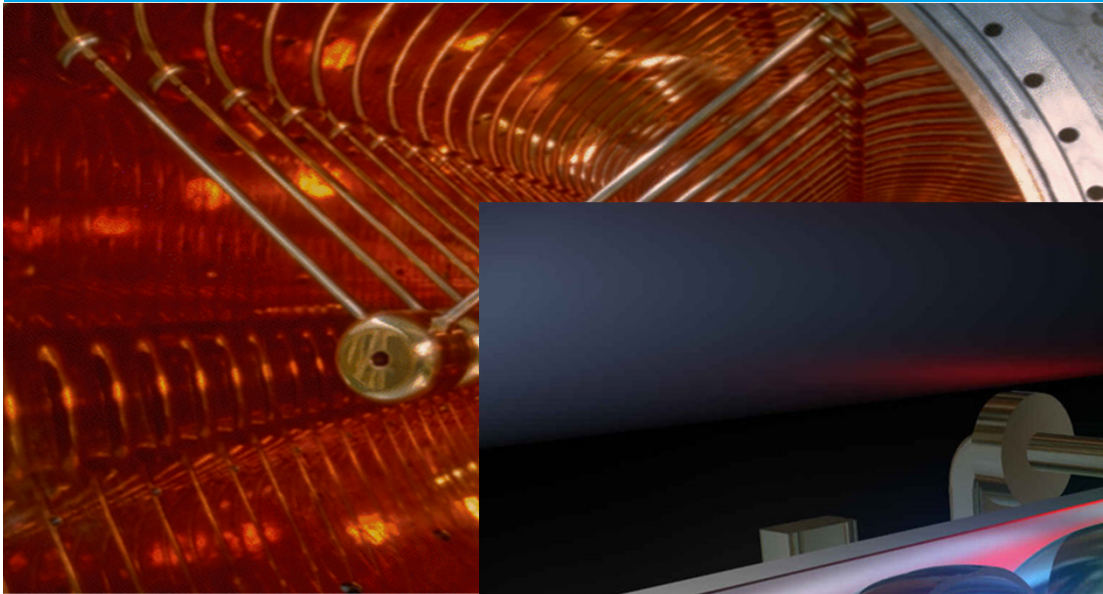


# Introduction to Accelerator Physics (part 1)

Scientific Tools for High Energy Physics, Synchrotron Radiation  
Research and Medicine Applications

Pedro Castro / Accelerator Physics Group (MPY)  
Introduction to Accelerator Physics (part 1)  
DESY, 5th August 2011

# How electromagnetic fields accelerate particles

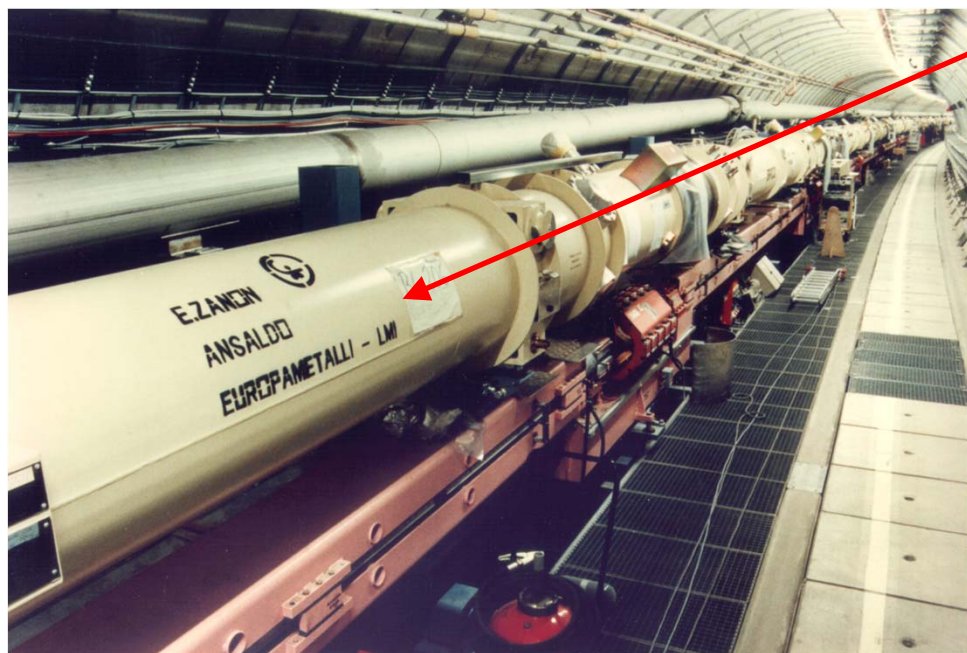


# Why we need superconducting magnets



LHC: Large Hadron Collider  
at CERN

p: 7 TeV



HERA: Hadron-Electron Ring Accelerator  
at DESY

p: 920 GeV  
e: 27.5 GeV

superconducting magnets



# Differences between proton and electron accelerators

HERA (Hadron Electron Ring Accelerator) tunnel:

proton  
accelerator  
920 GeV

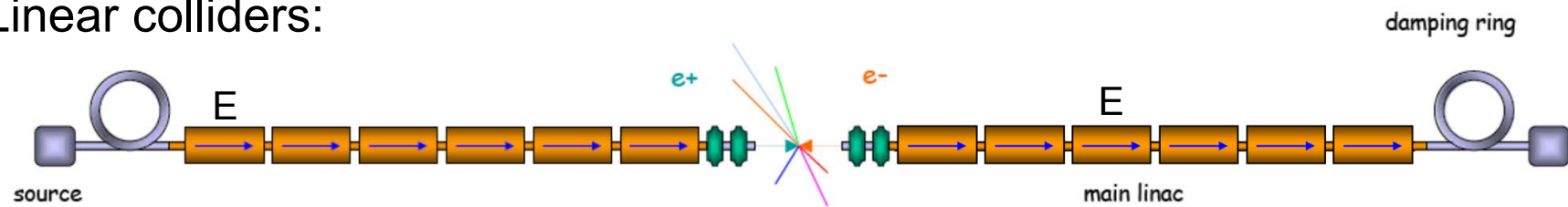


electron accelerator  
27.5 GeV

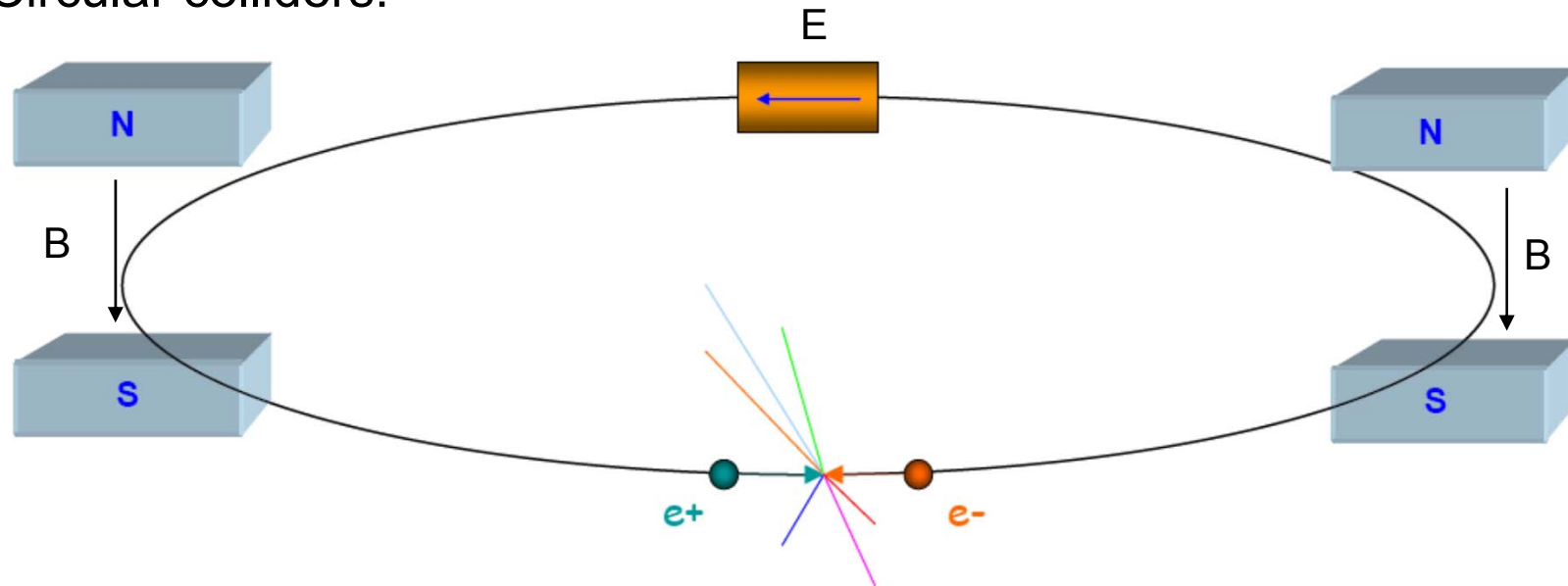


# Which collider is better?

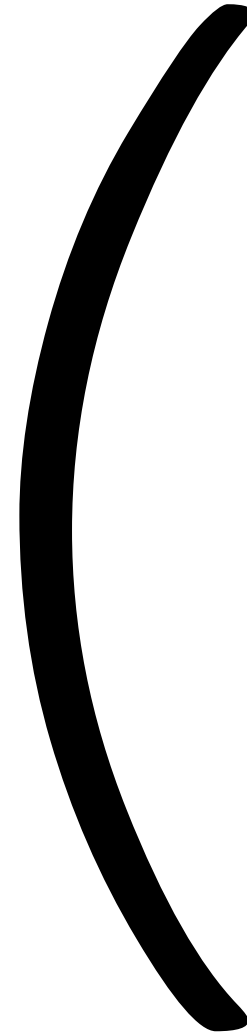
Linear colliders:



Circular colliders:



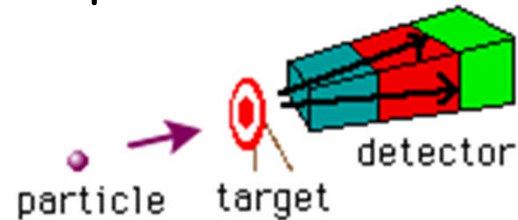
# Applications of accelerators



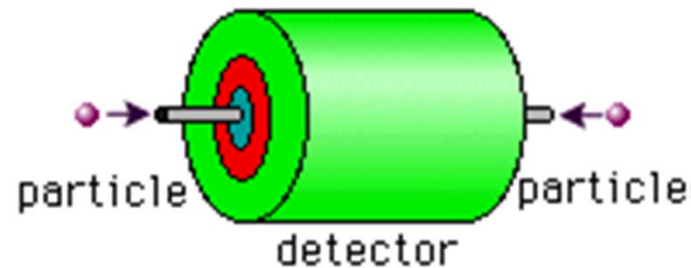
# Applications of Accelerators (1)

## Particle colliders for High Energy Physics (HEP) experiments

- fix target experiments:



- two beams collision experiments:

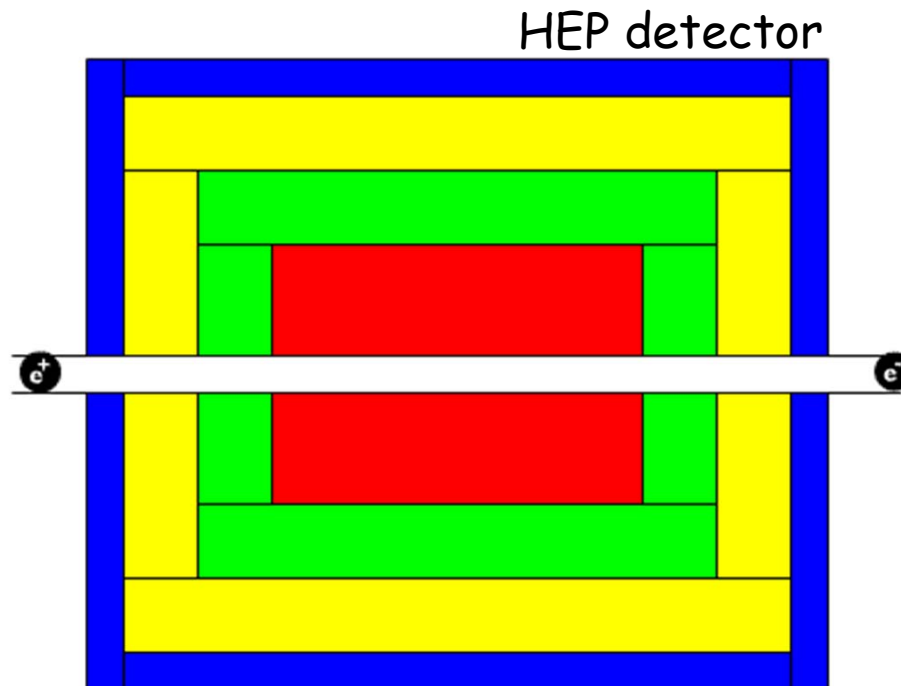
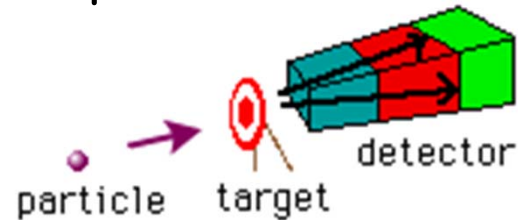




# Applications of Accelerators (1)

## Particle colliders for High Energy Physics (HEP) experiments

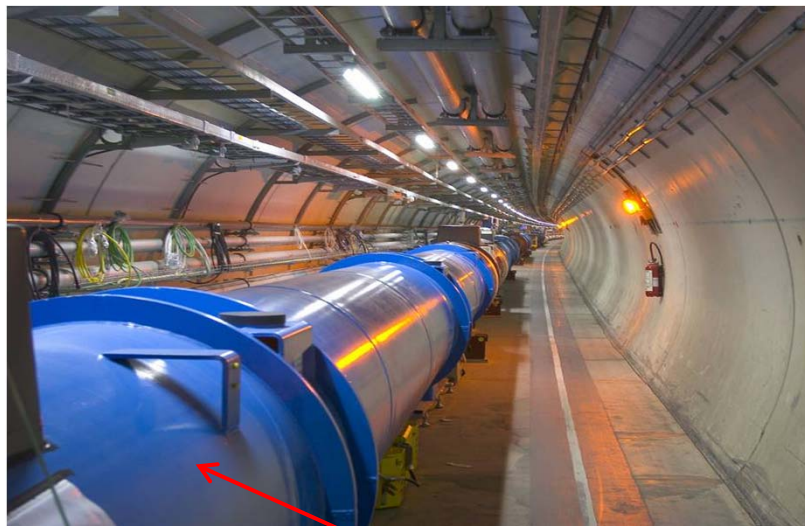
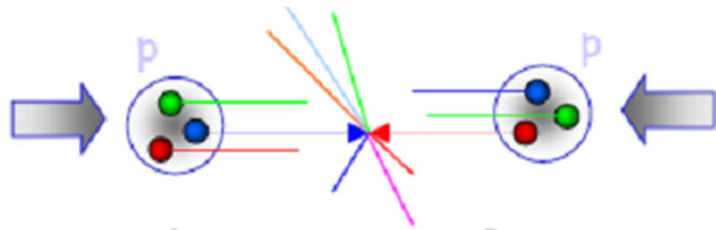
- fix target experiments:



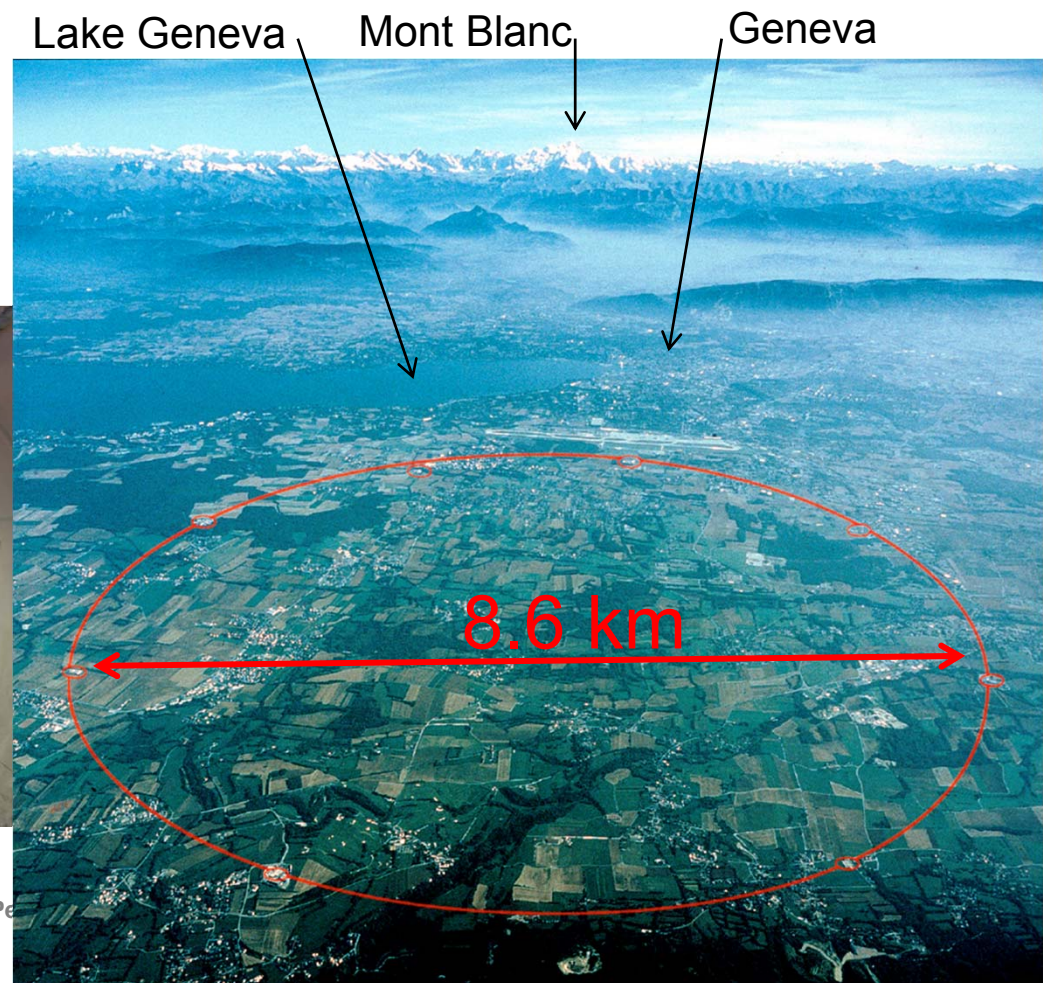
# Applications of Accelerators (1)

## Particle colliders for High Energy Physics experiments

Example: the Large Hadron Collider (LHC) at CERN

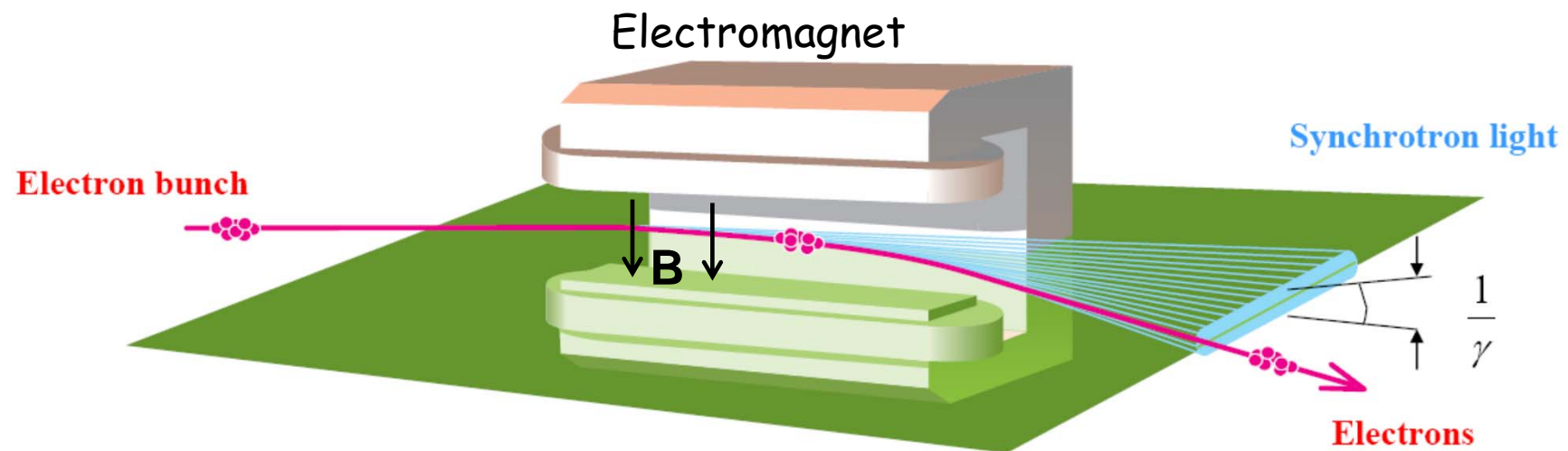


superconducting magnets  
(inside a cryostat)



## Applications of Accelerators (2)

Light sources for biology, physics, chemistry... experiments

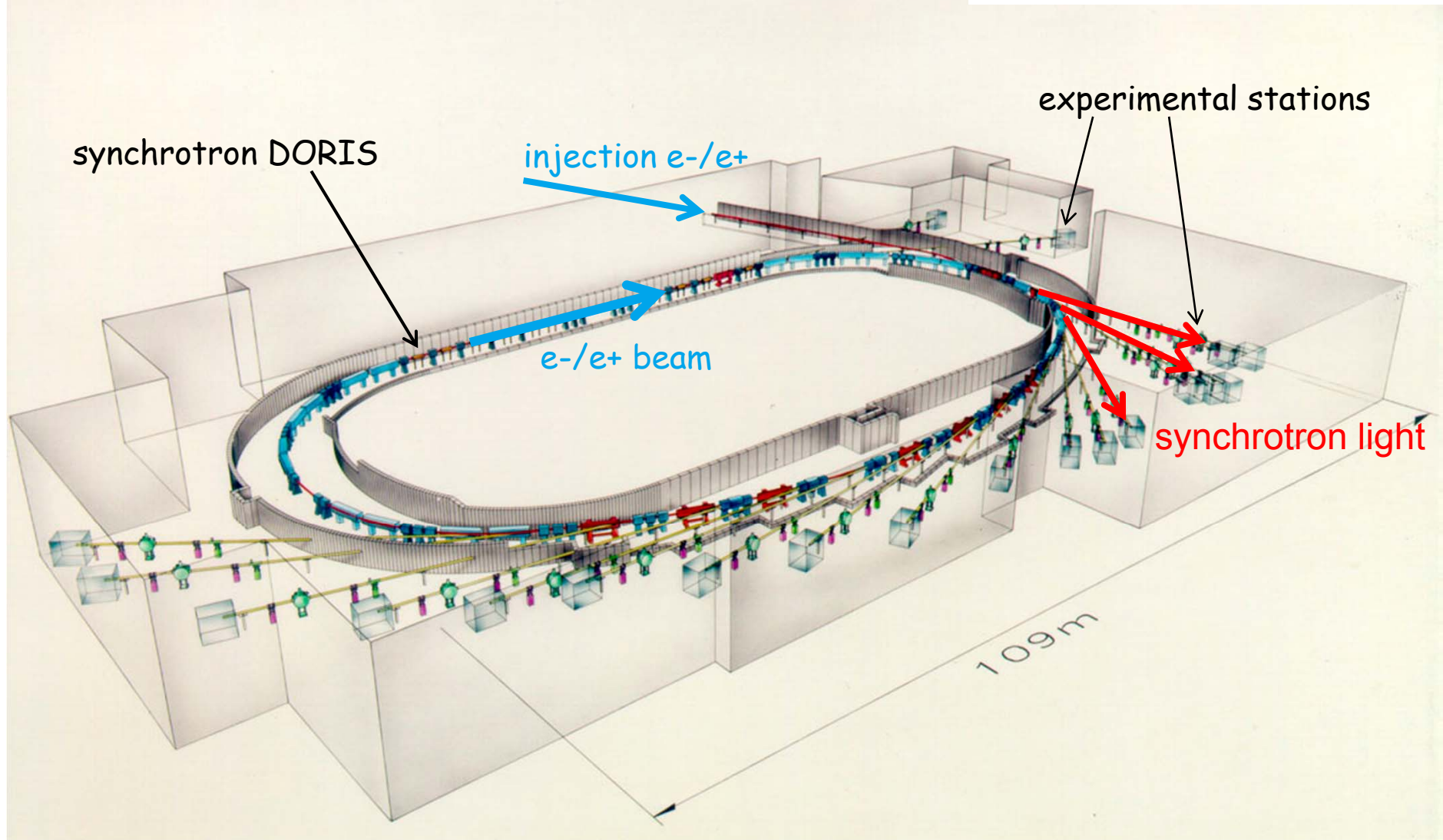


- structural analysis of crystalline materials
- X-ray crystallography (of proteins)
- X-ray microscopy
- X-ray absorption (or emission) spectroscopy
- ...



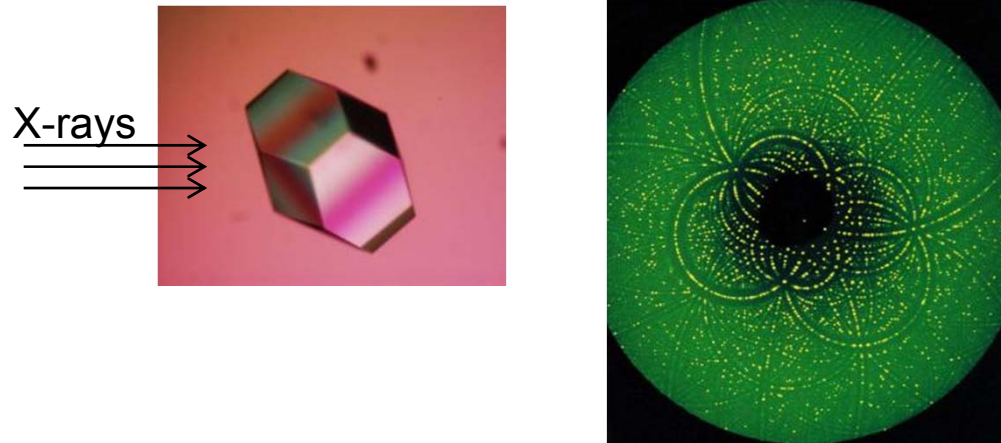
Example: Doppel-Ring-Speicher (DORIS)  
'double ring store' at DESY

built between 1969 and 1974  
HEP exp. until 1983  
synchrotron rad. since 1980

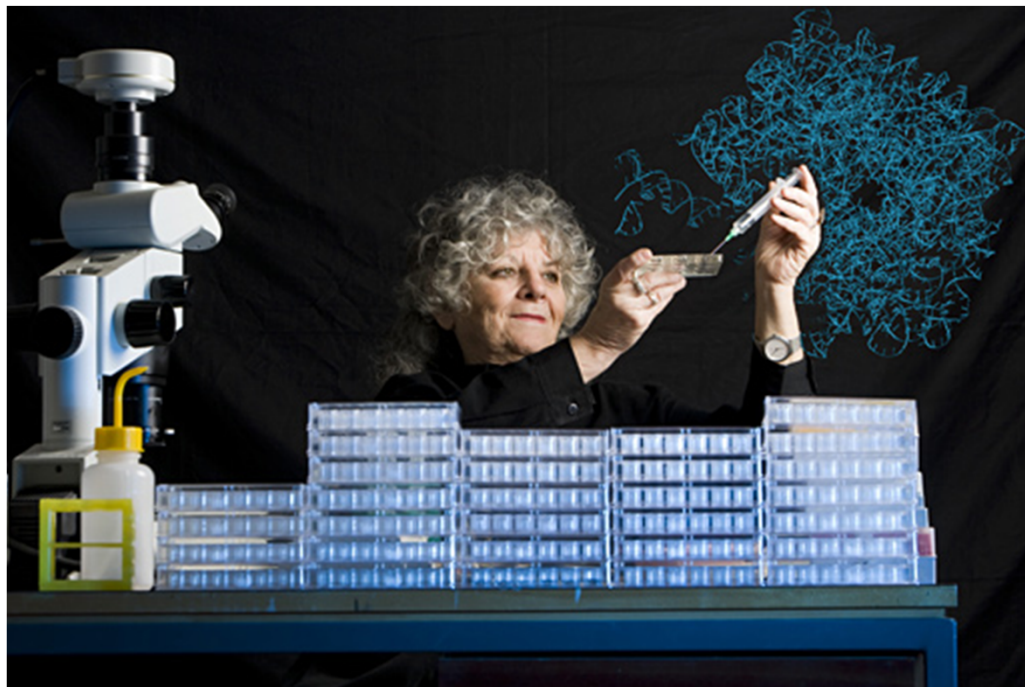
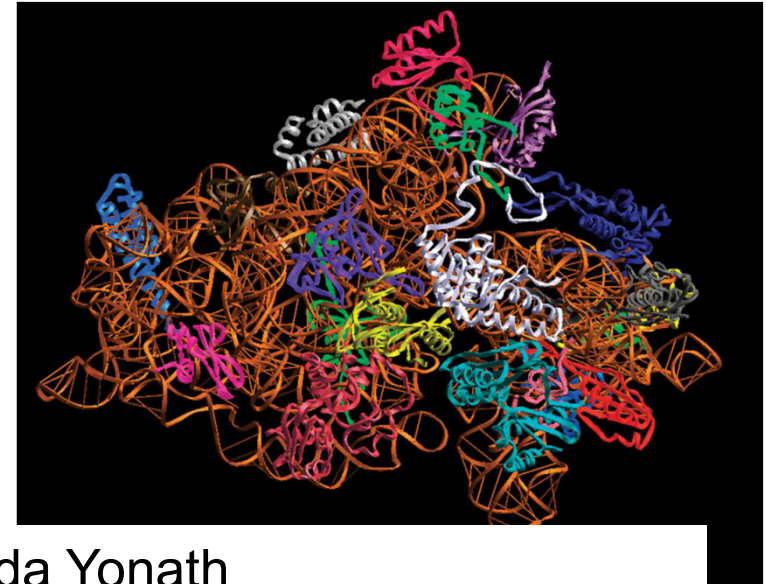


## Applications of Accelerators (2)

### X-ray crystallography



### Ribosome



Ada Yonath  
Leader of MPG Ribosome  
Structure Group at DESY  
1986-2004



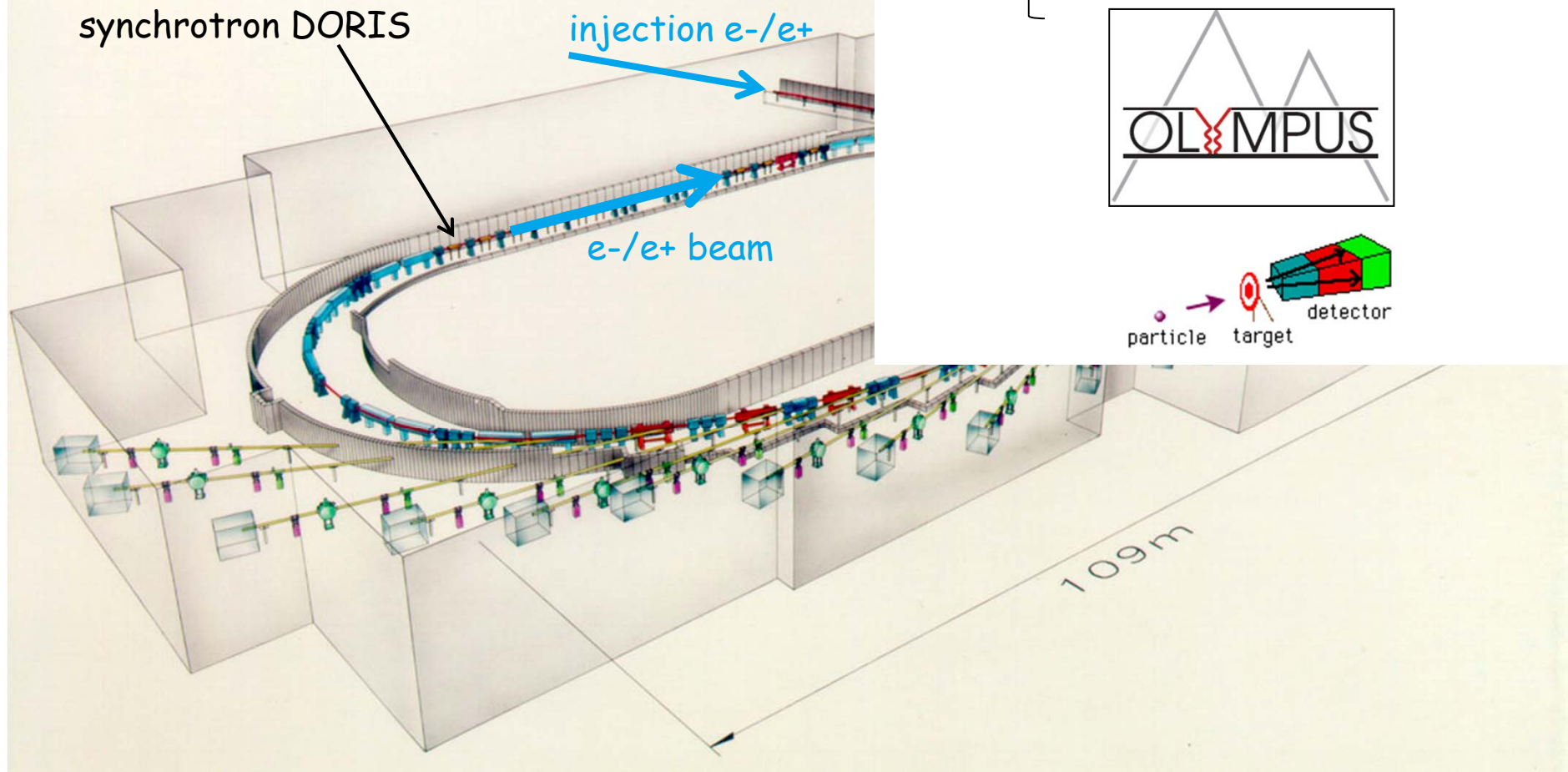
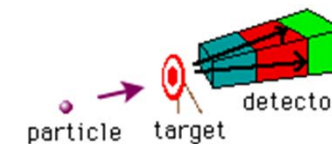
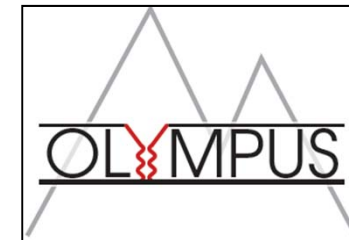
2009 Nobel Prize of Chemistry  
together with T. Steitz and  
V. Ramakrishnan



Example: Doppel-Ring-Speicher (DORIS)  
'double ring store' at DESY

history { built between 1969 and 1974  
HEP exp. until 1983  
synchrotron rad. since 1980

future { synchrotron rad. until 2012  
HEP exp. from 2012





- > About 120 accelerators for research in "nuclear and particle physics"
- > About 70 electron storage rings and electron linear accelerators used as light sources (so-called 'synchrotron radiation sources')

- 
- > More than 7,000 accelerators for medicine  
radiotherapy (>7,500), radioisotope production (200)
  - > More than 18,000 industrial accelerators  
ion implantation (>9,000) , electron cutting and welding (>4,000) ...

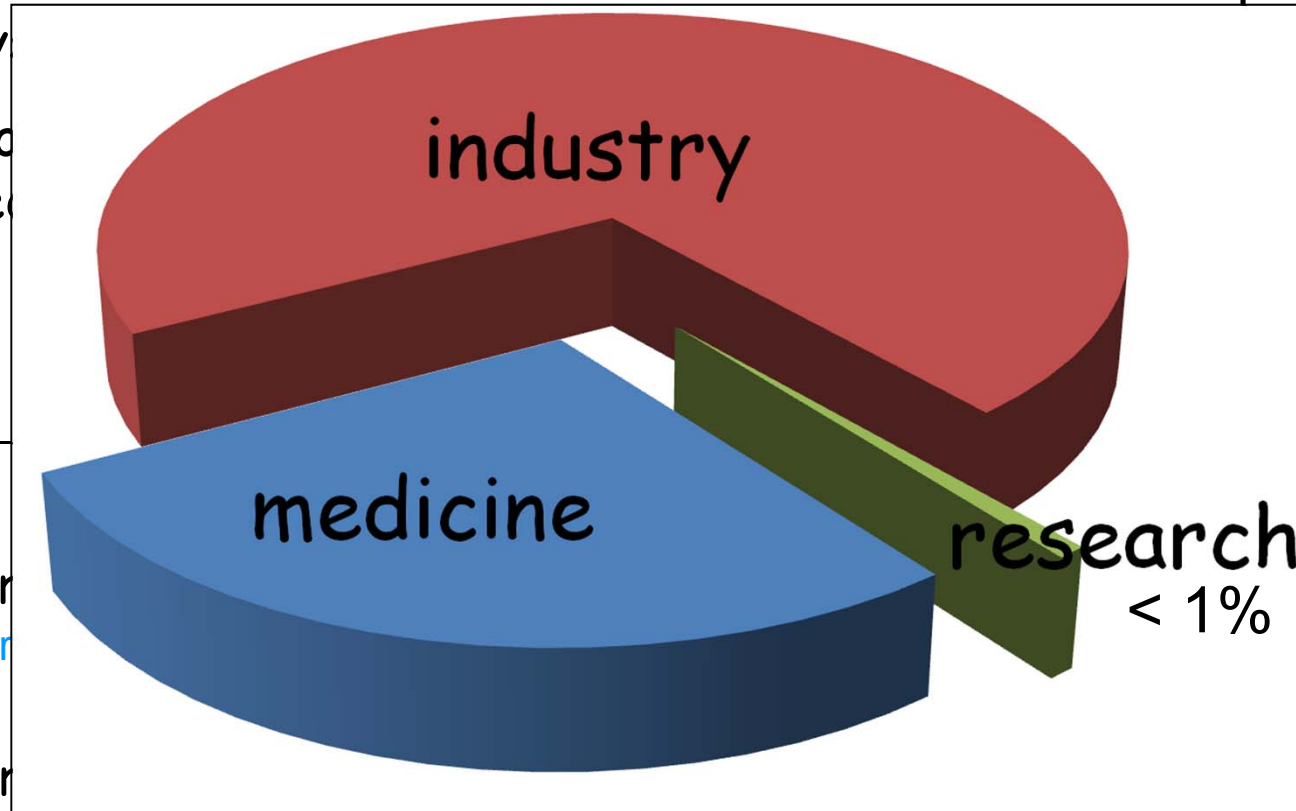


> About 120 accelerators for research in "nuclear and particle physics"

> About 100 accelerators used in medicine

> More than 100 accelerators used in industry

> More than 100 accelerators used in research



elerators  
'sources')

ion implantation (>9,000) , electron cutting and welding (>4,000) ...

# Applications of Accelerators (3)

## Medical applications

For radioisotope production

proton beam + stable isotope  $\xrightarrow{\text{transmutation}}$  radioactive isotope

For radiotherapy and radiosurgery:

- x-rays and gamma-rays
- ions (from protons to atoms with atomic number up to 18, Argon)
- neutrons



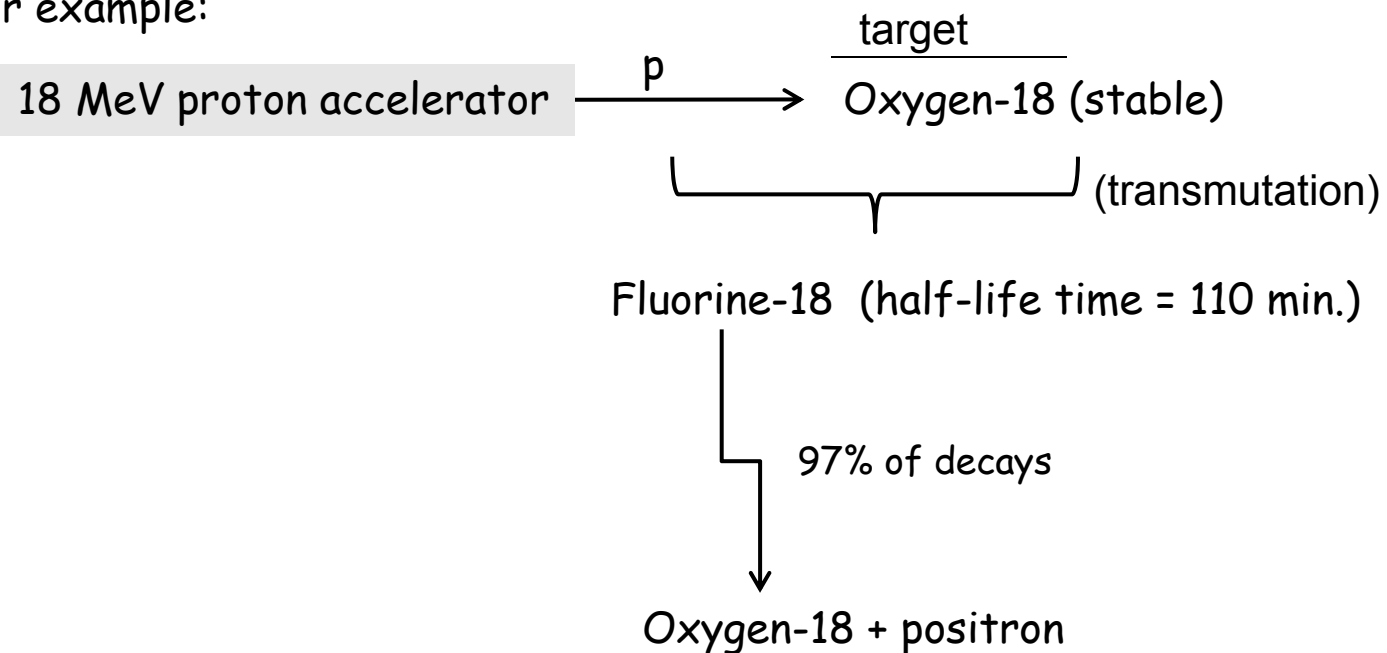


# Applications of Accelerators (3)

## Medical applications

For radioisotope production

For example:

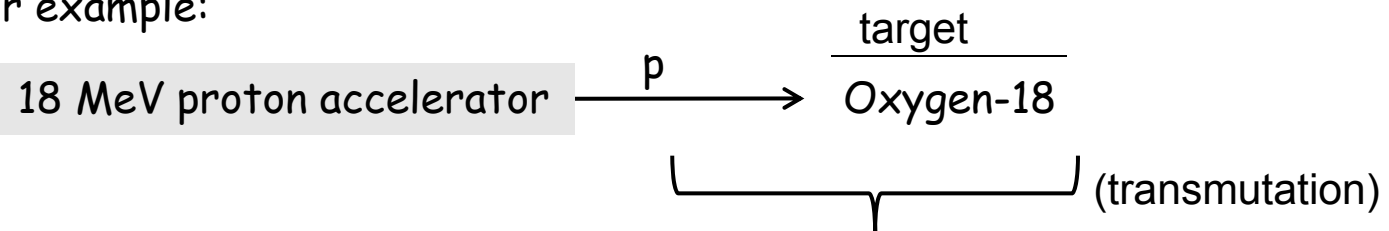


# Applications of Accelerators (3)

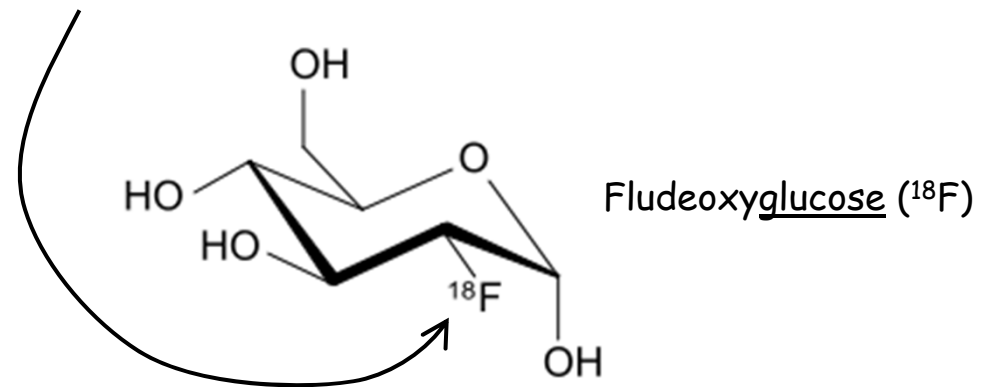
## Medical applications

For radioisotope production

For example:

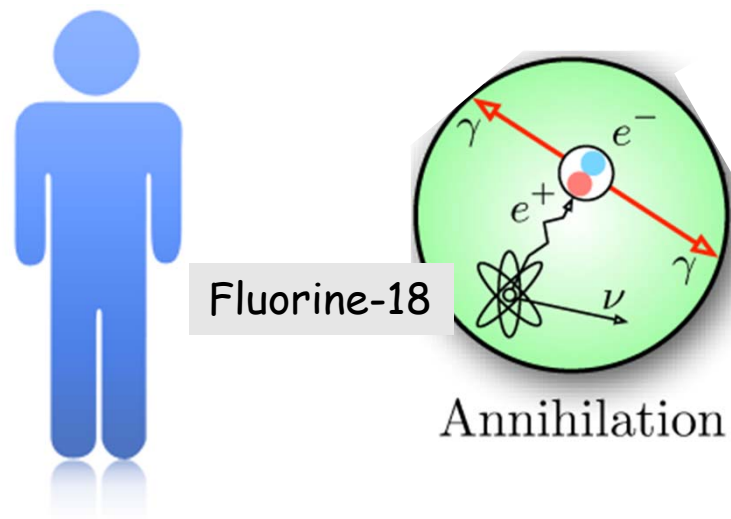


Fluorine-18 (half-life time = 110 min.)



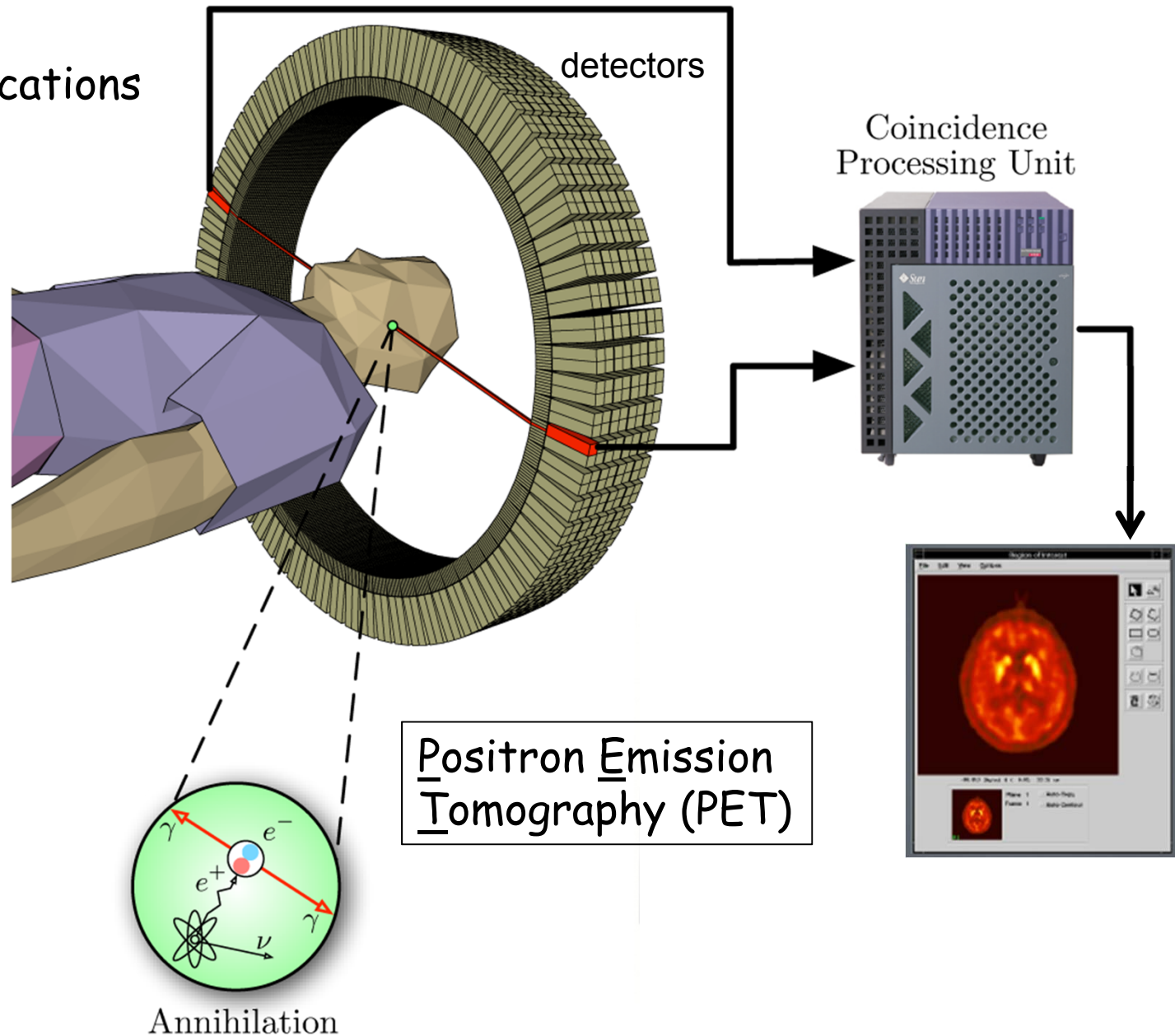
# Applications of Accelerators (3)

## Medical applications



# Applications of Accelerators (3)

Medical applications





# Applications of Accelerators (4)

For industrial applications:

Application	
Ion implantation	~ 9500
Electron cutting and welding	~ 4500
Electron beam and x-ray irradiators	~ 2000
Ion beam analysis (including AMS)	~ 200
Radioisotope production (including PET)	~ 900
Nondestructive testing (including security)	~ 650
Neutron generators (including sealed tubes)	~ 1000

approx. numbers from 2007 (worldwide)

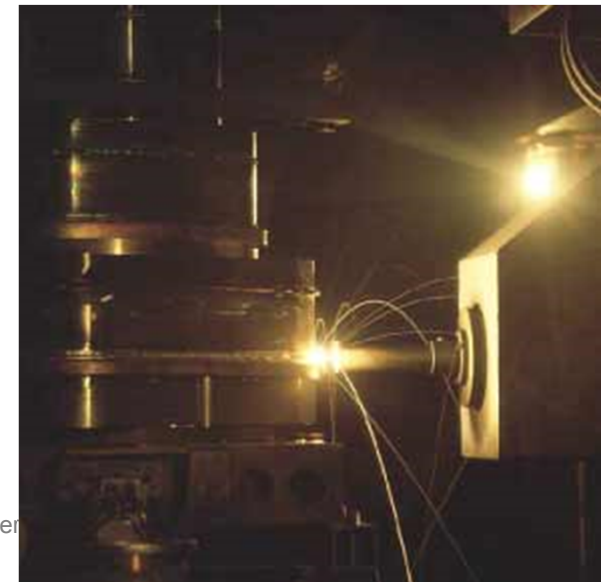
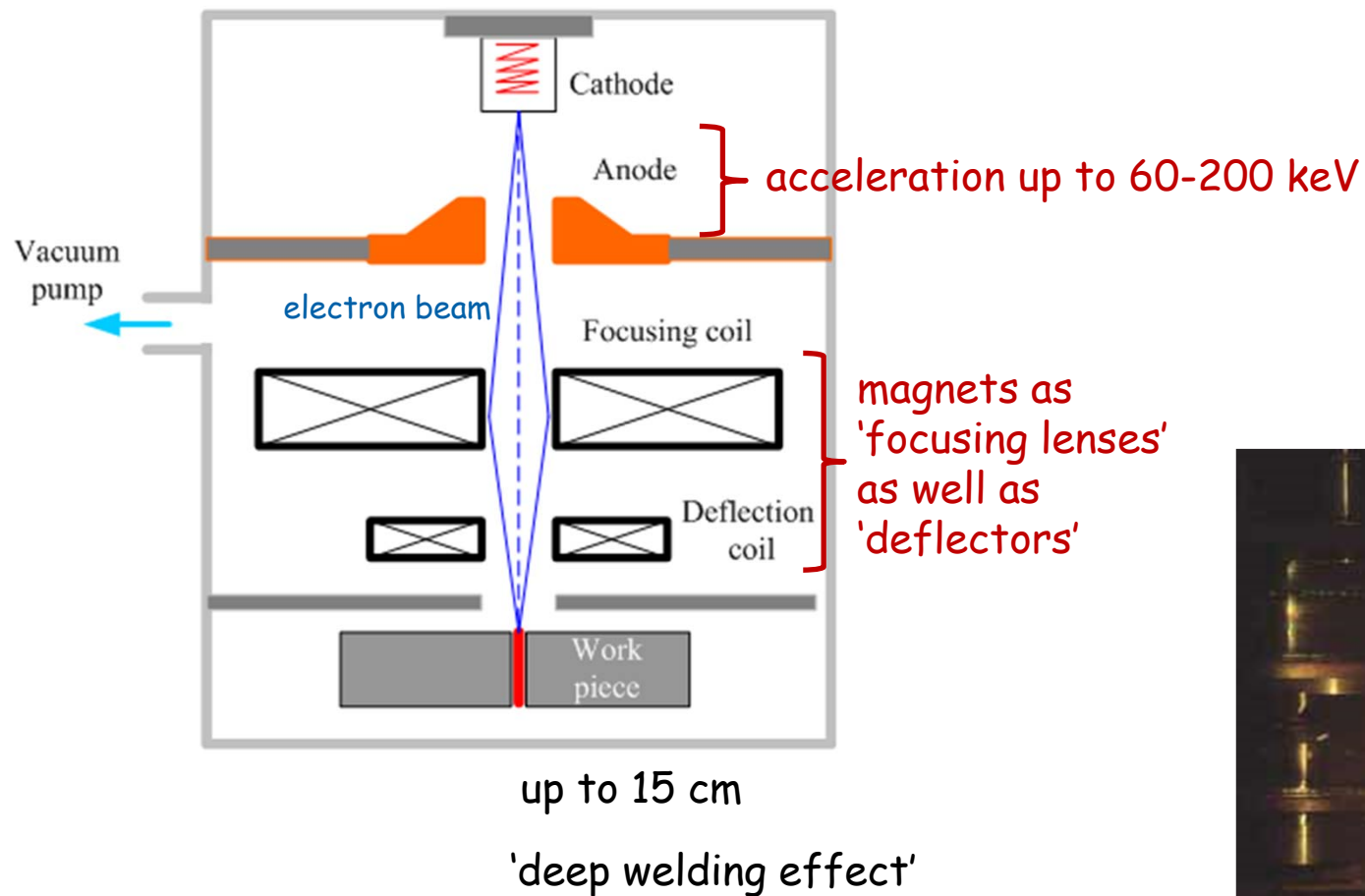
with energies up to 15 MeV



# Applications of Accelerators (4)

For industrial applications:

an example: electron beam welding



- > About 120 accelerators for research in “nuclear and particle physics”
- > About 70 electron storage rings and electron linear accelerators used as light sources (so-called ‘synchrotron radiation sources’)

---

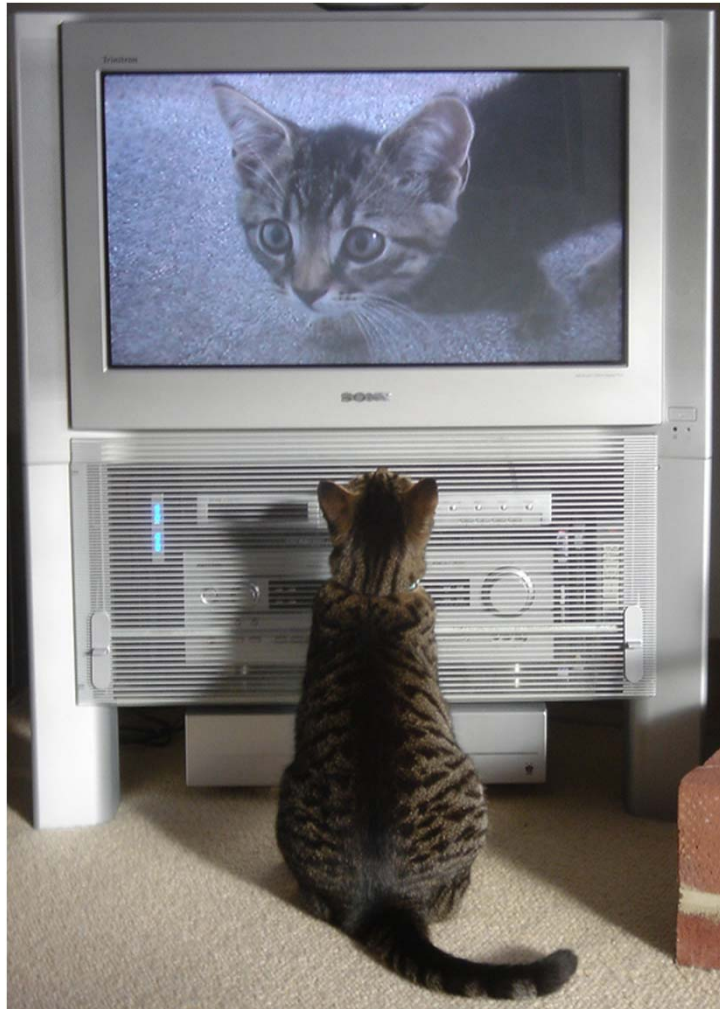
...and there is more !!!

- > More than 7,000 accelerators for medicine  
radiotherapy (>7,500), radioisotope production (200)
- > More than 18,000 industrial accelerators  
ion implantation (>9,000) , electron cutting and welding (>4,000) ...



# Applications of Accelerators (5)

Many millions of television sets, oscilloscopes using CRTs (Cathode Ray Tube)



TV

CRT (Cathode Ray Tube)



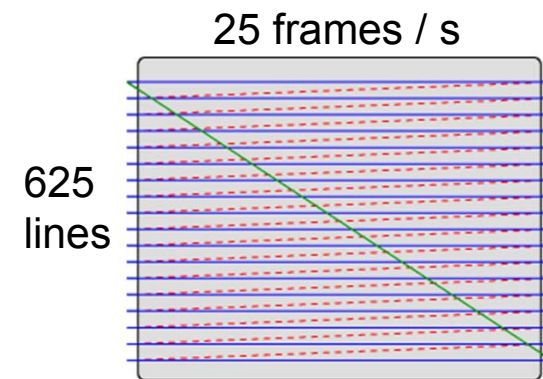
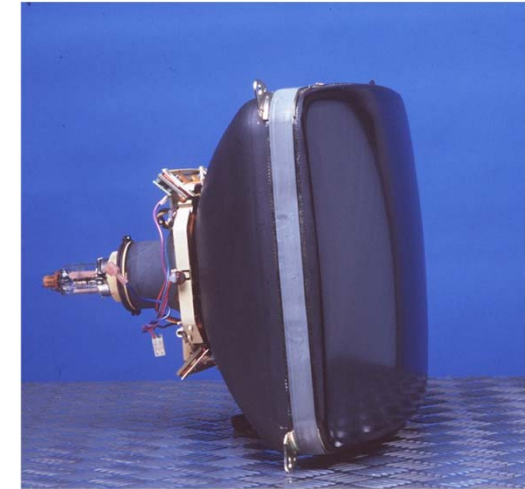
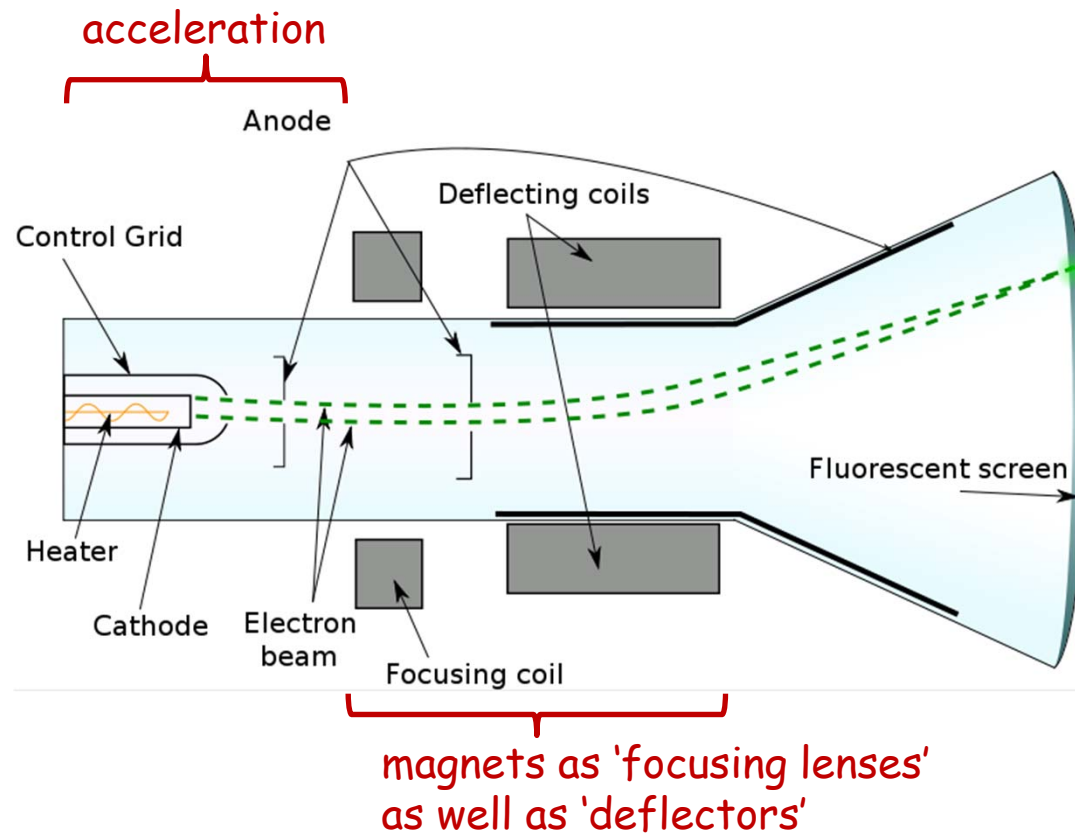
oscilloscope





# Applications of Accelerators (5)

Many millions of television sets, oscilloscopes using CRTs (Cathode Ray Tube)



# Applications of Accelerators (5)

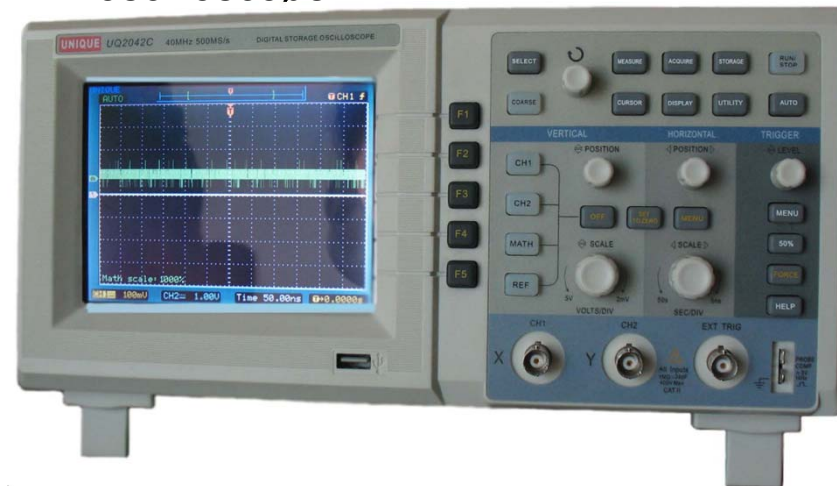
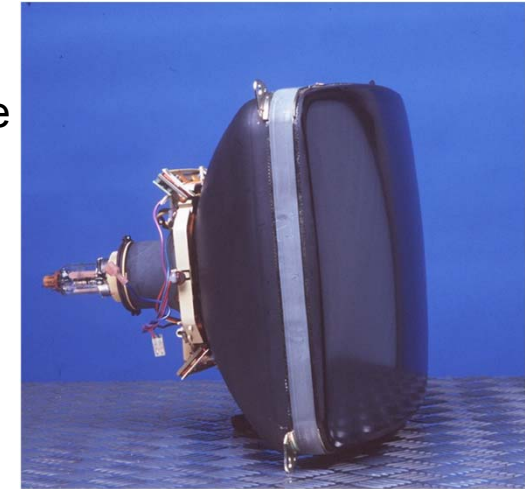
Many millions of television sets, oscilloscopes using CRTs (Cathode Ray Tube)  
(tending to disappear, replaced by LCD and plasma screens)



CRT (Cathode Ray Tube)

TV

oscilloscope

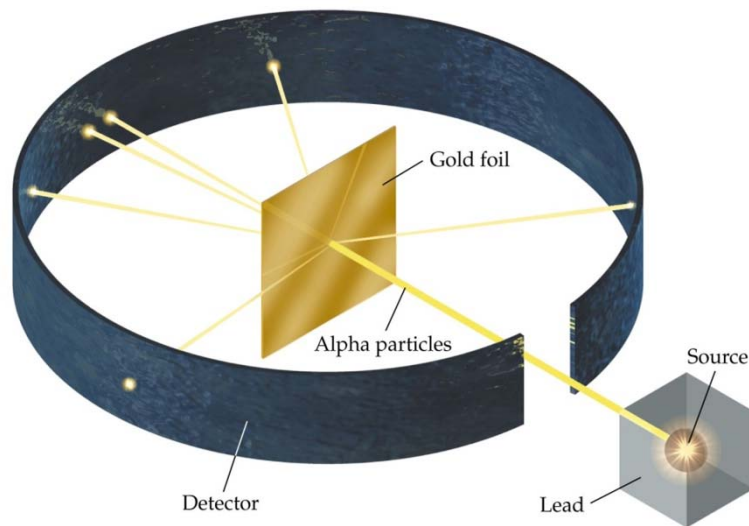




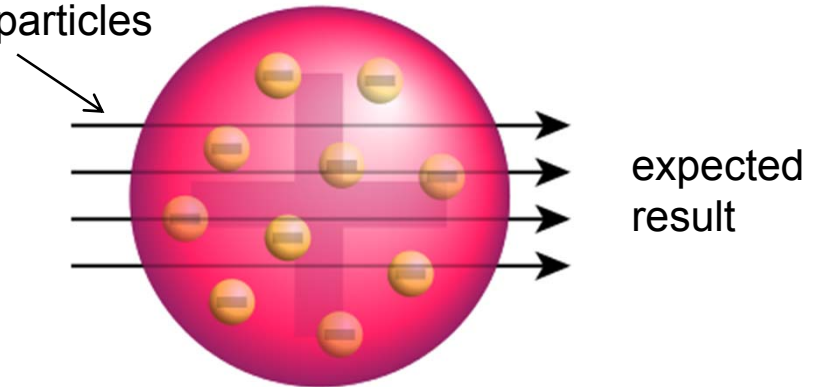
# Applications of accelerators



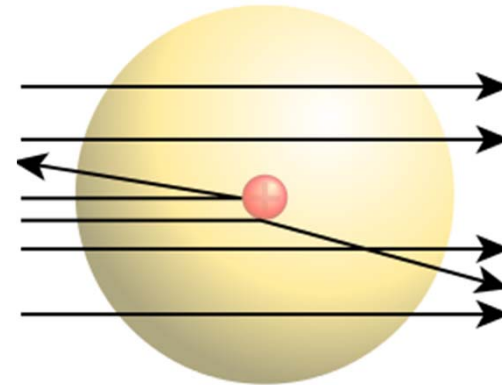
Geiger-Marsden experiment:  
the gold foil experiment (1909)



Thomson model of the atom (1904)  
alpha particles



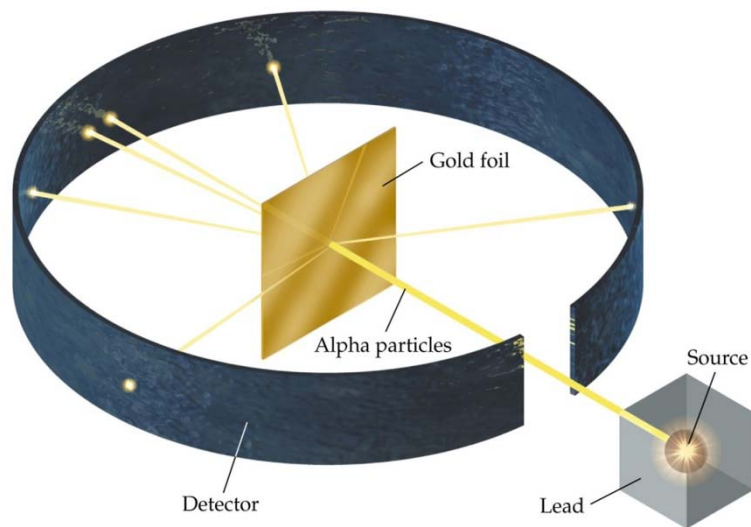
1 in 8000 reflected with  $\theta > 90^\circ$   
shooting with 10000 km/s, a few coming back !



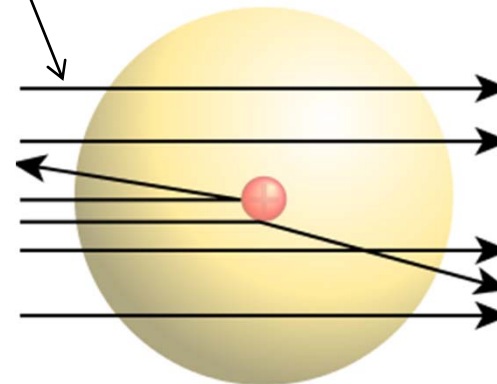
Rutherford model of the atom (1911)



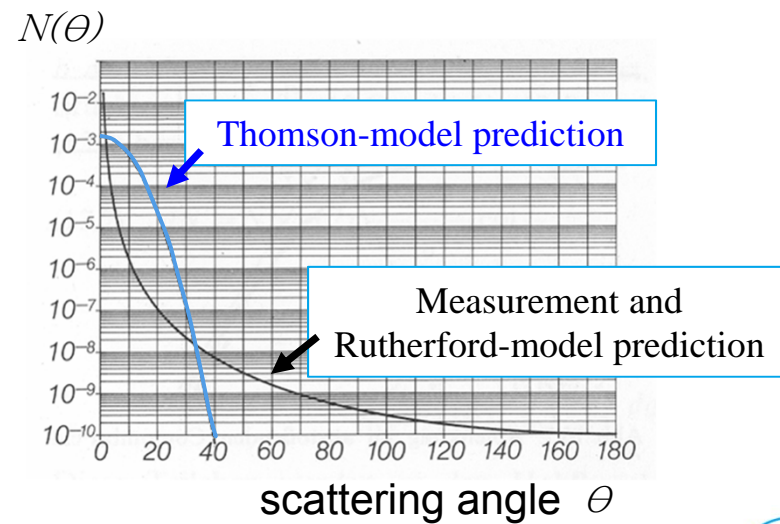
## Geiger-Marsden experiment: the gold foil experiment (1909)



alpha particles



Rutherford model of the atom (1911)



# Acceleration with an electrostatic field

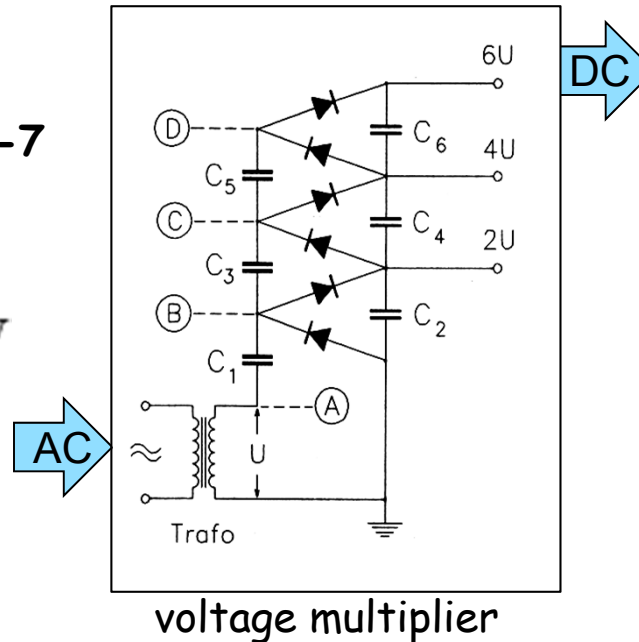
## Cockcroft-Walton generator

(1932)

400 keV p  $\rightarrow$  Lithium-7



$^4\text{He} + ^4\text{He} + 17,35 \text{ MeV}$



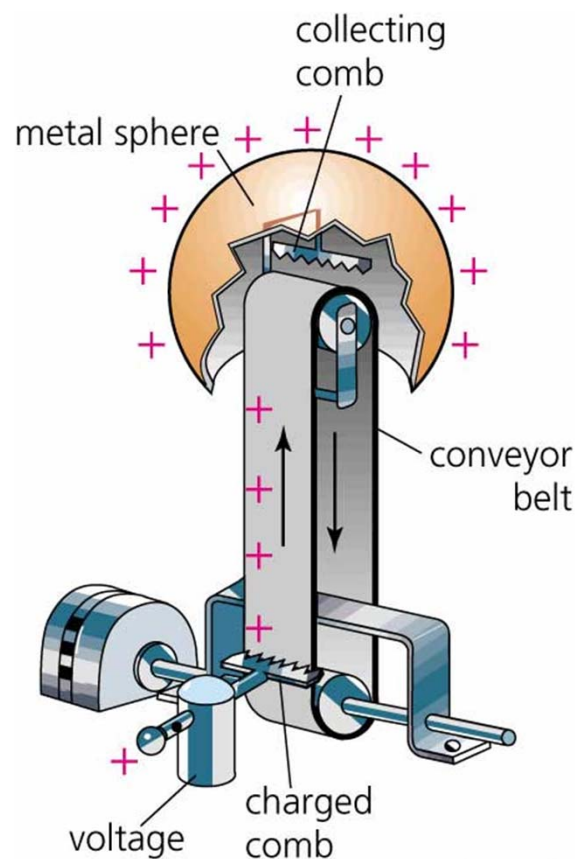
maximum voltage < 1 MV

maximum voltage  $\sim$  25 MV

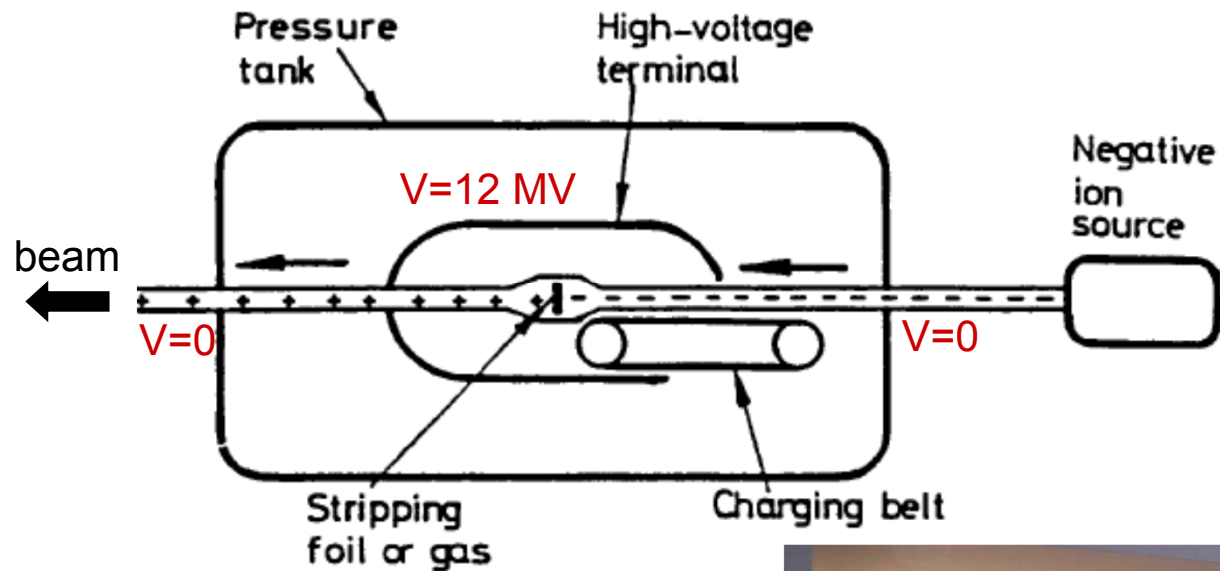
$\rightarrow$  Van de Graaff generator

# Acceleration with an electrostatic field

Van der Graaff generator: invented in 1929



# Acceleration with an electrostatic field



12 MV-Tandem Van de Graaff Accelerator  
at MPI Heidelberg, GE





# Acceleration with an electrostatic field

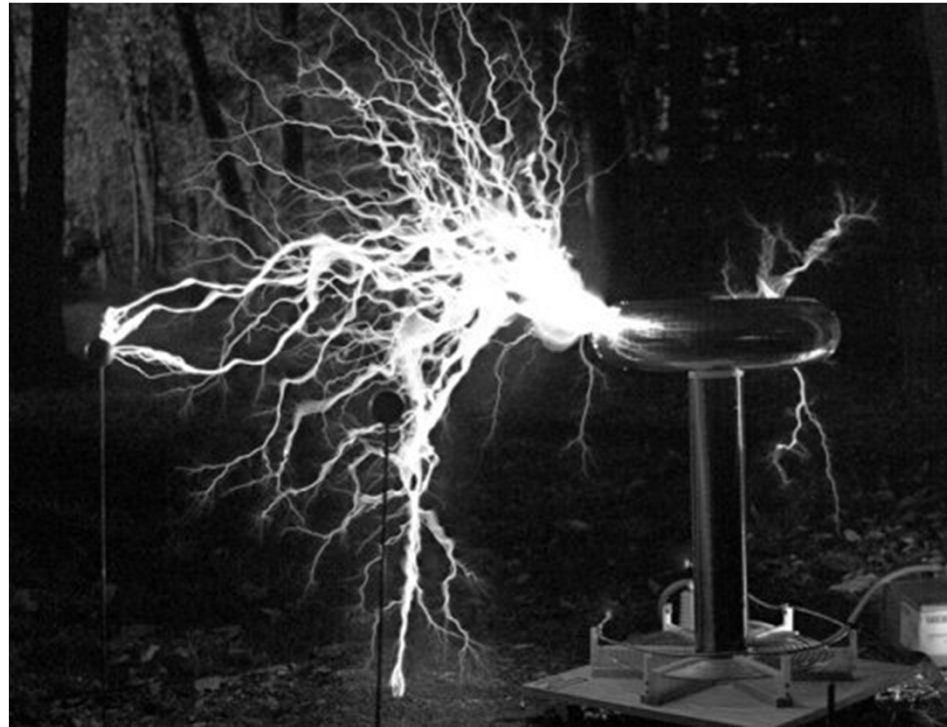
20 MV-Tandem  
at Daresbury, UK



12 MV-Tandem Van de Graaff Accelerator  
at MPI Heidelberg, GE



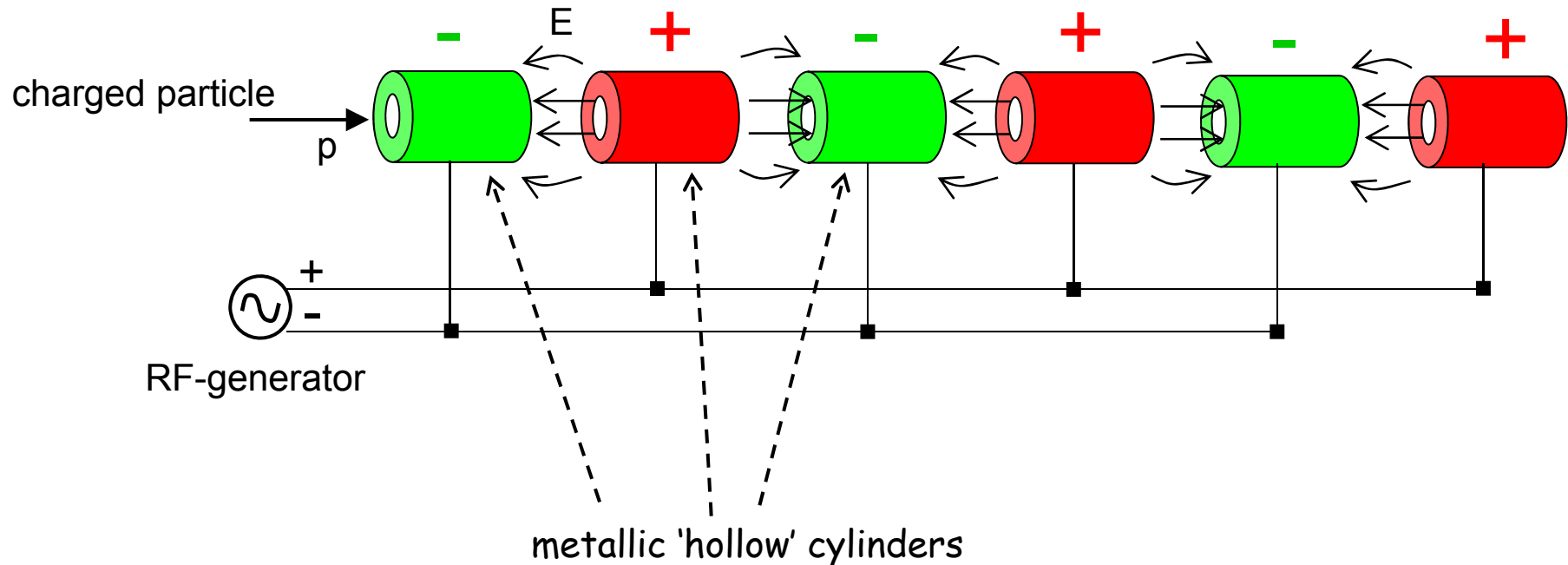
# Limitation of electrostatic fields



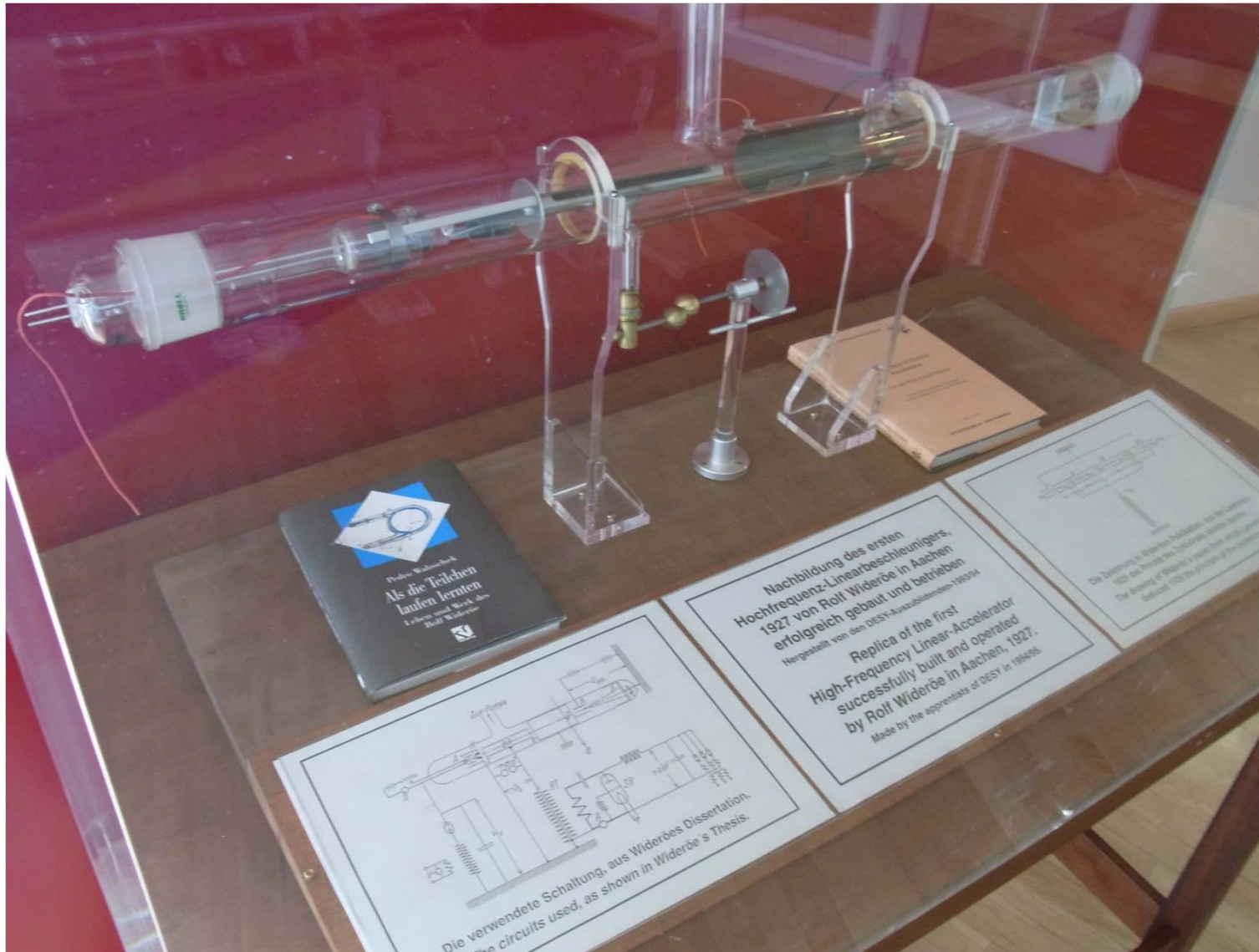
breakdown

# Acceleration using Radio-Frequency (RF) generators

Widerøe (1928): apply acceleration voltage several times to particle beam

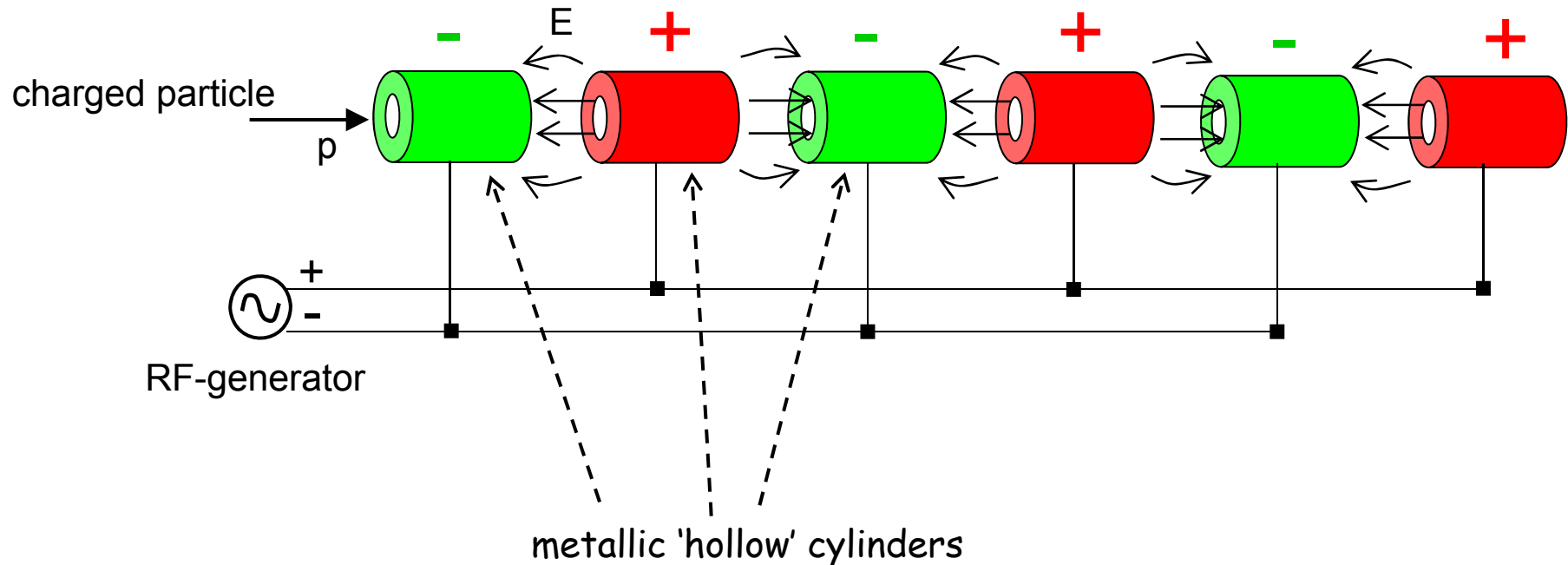


## Replica of the Widerøe accelerator



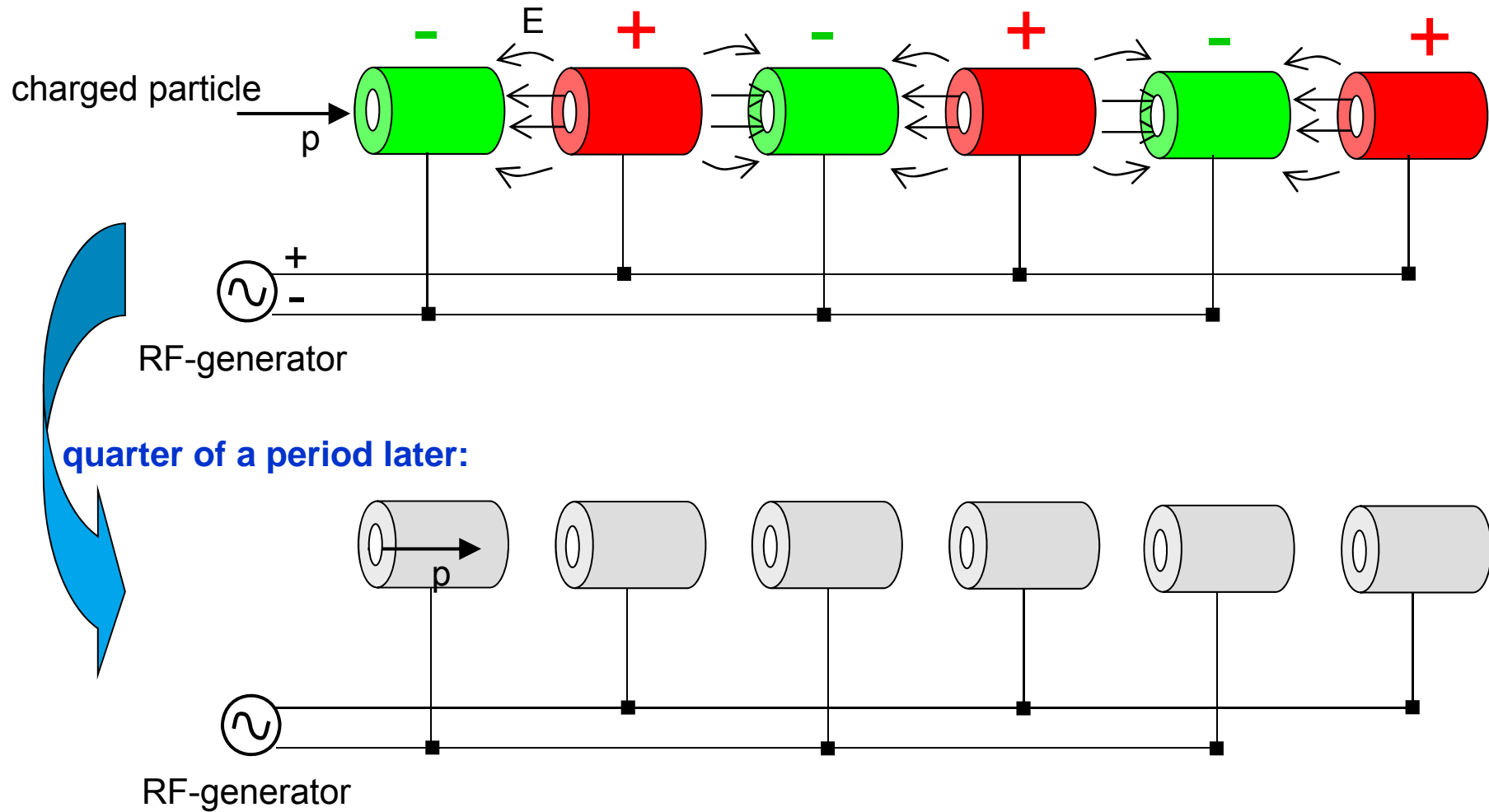
# Acceleration using Radio-Frequency (RF) generators

Widerøe (1928): apply acceleration voltage several times to particle beam



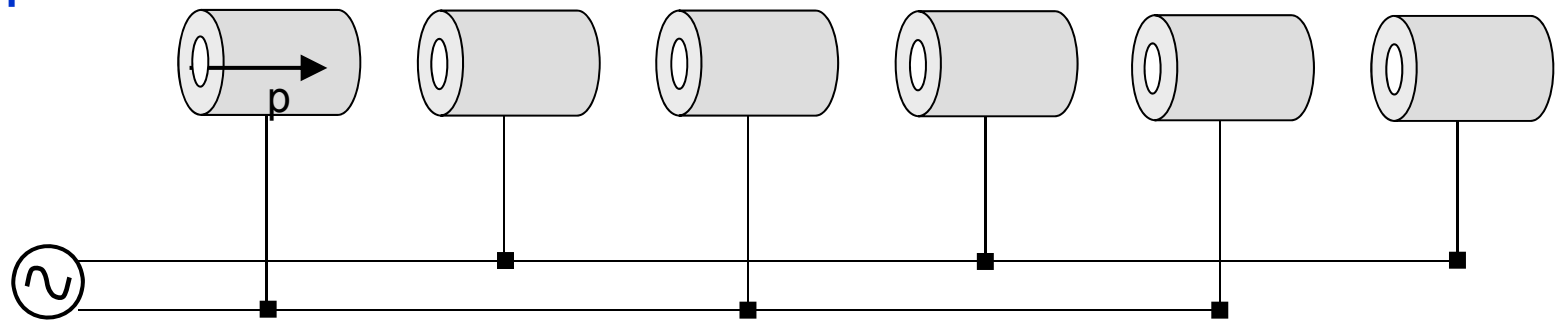


# Acceleration using Radio-Frequency (RF) generators

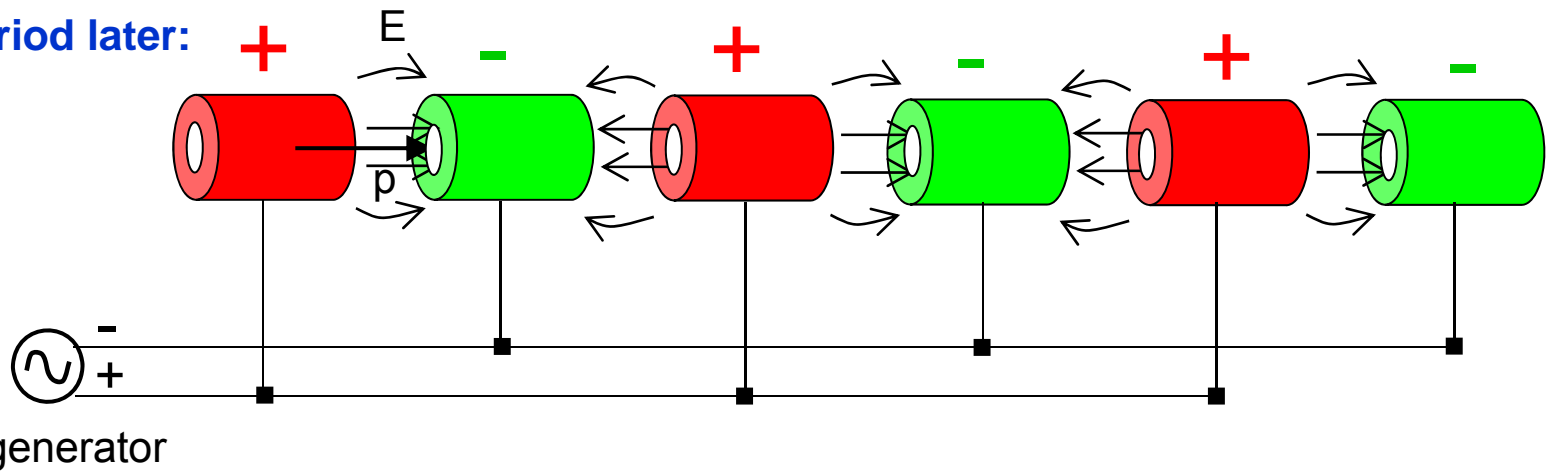


# Acceleration using Radio-Frequency (RF) generators

quarter of a period later:



half a period later:



# Restrictions of RF

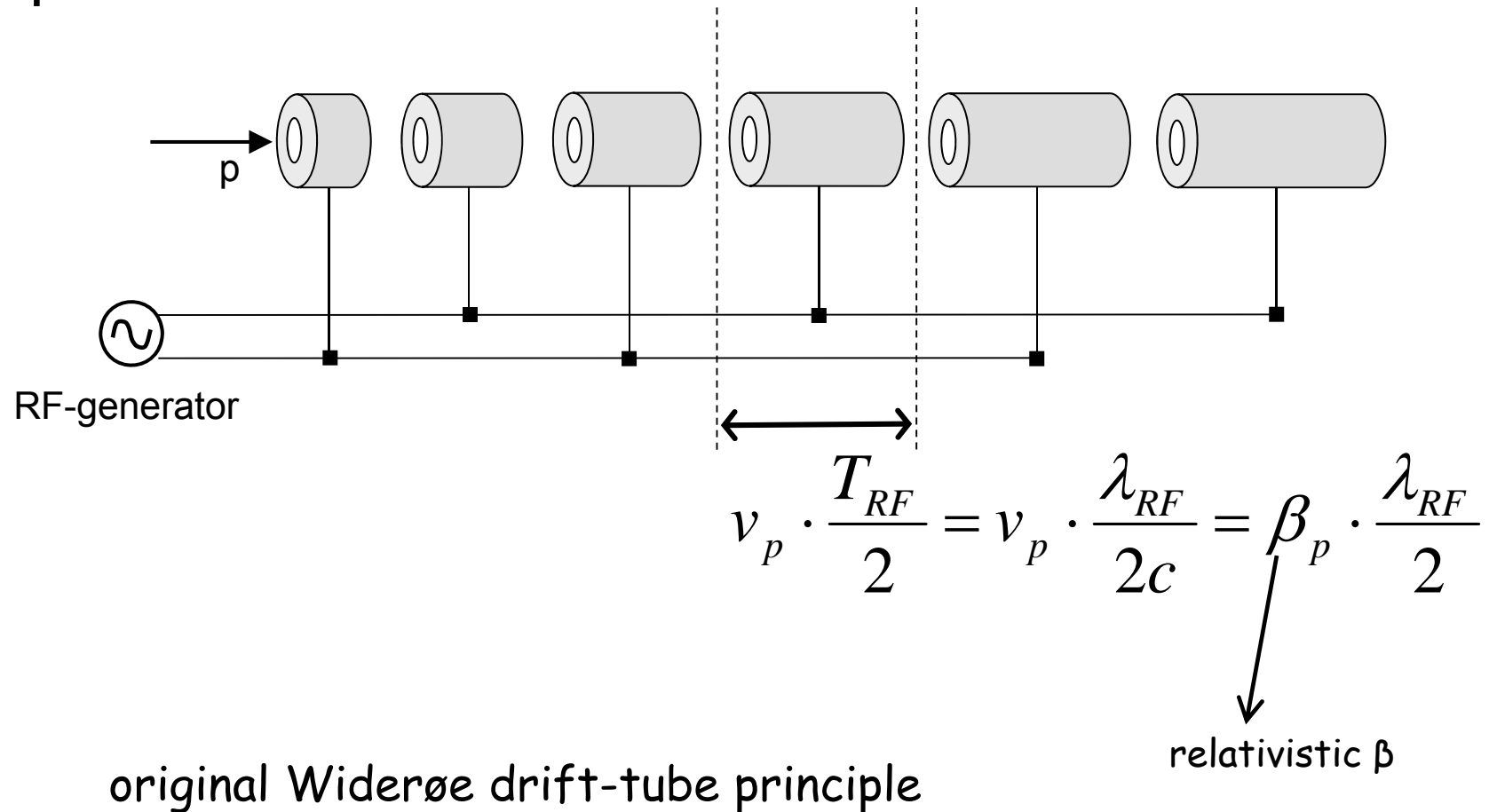
- > particles travel in groups → called bunches
- > bunches are travelling synchronous with RF cycles

>  $\Delta E \rightarrow \Delta v$



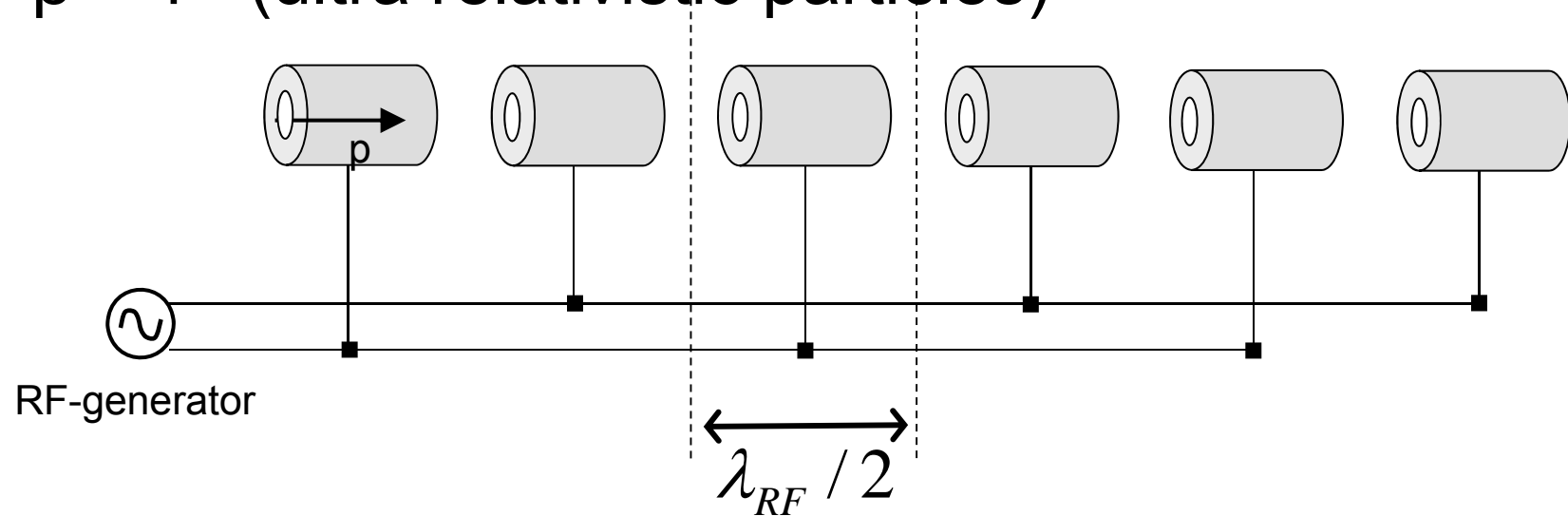
# Acceleration using Radio-Frequency (RF) generators

$$\beta < 1$$



# Acceleration using Radio-Frequency (RF) generators

$\beta \approx 1$  (ultra relativistic particles)



Limitations of drift tube accelerators:

> only low freq. (<10 MHz) can be used

$$L_{tube} = \beta \frac{\lambda_{RF}}{2} = \beta \frac{c}{2f_{RF}} \rightarrow 30 \text{ m for } \beta=1 \text{ and } f=10 \text{ MHz}$$

→ drift tubes are impracticable for ultra-relativistic particles ( $\beta=1$ )

→ only for very low  $\beta$  particles



# First summing-up

## Applications:

- HEP (example: LHC)
- light source (example: DORIS, Ribosome)
- medicine (example: PET)
- industry (example: electron beam welding)
- cathode ray tubes (example: TV)

## Electrostatic accelerators:

- Cockcroft-Walton generator
- Tandem Van der Graaff accelerator

## Radio-frequency accelerators:

- Widerøe drift-tube



Widerøe drift-tube  
principle

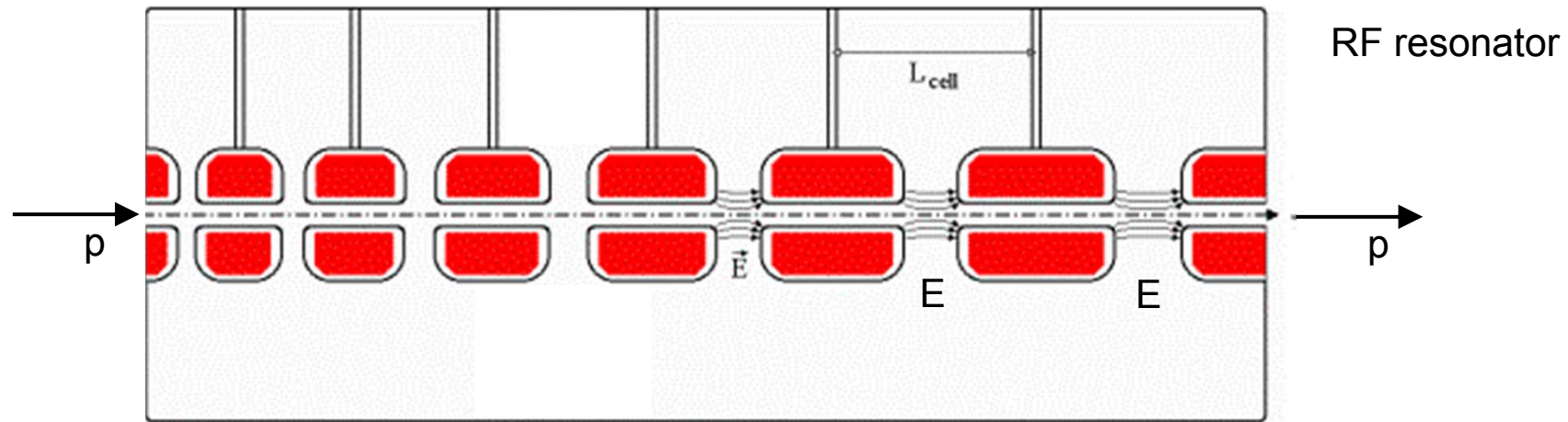
Alvarez drift-tube (1946) structure

Cyclotron (1929), E. Lawrence



# Resonant cavities

Alvarez drift-tube (1946) structure:

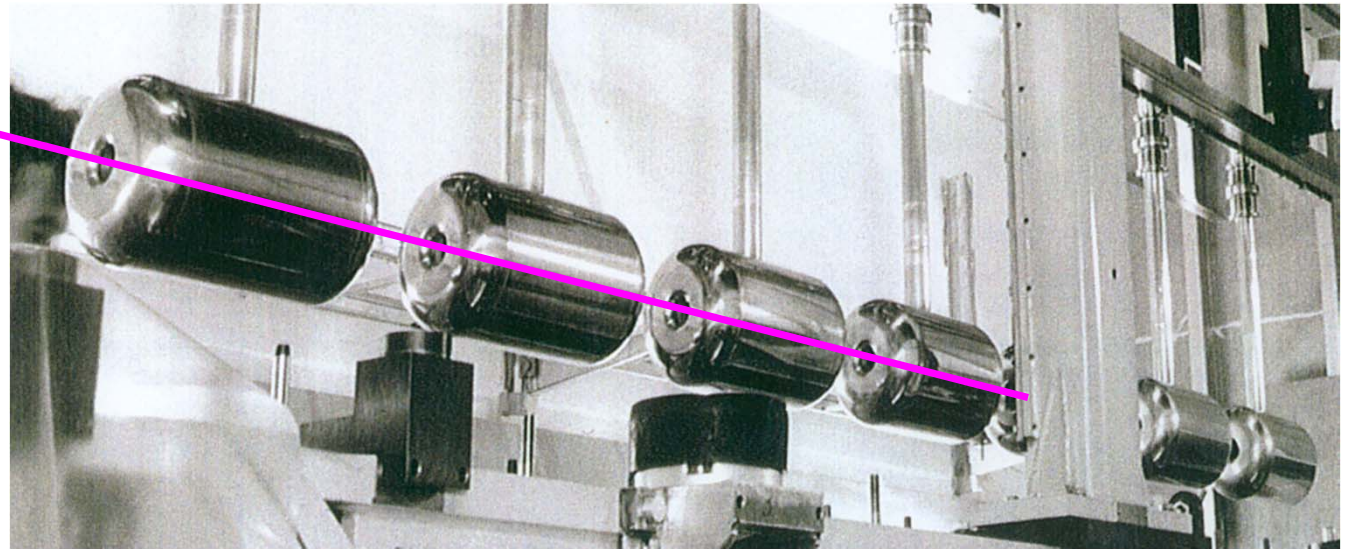


# Examples

## DESY proton linac (LINAC III)

$$E_{kin} = 50 \text{ MeV}$$

$$\beta \approx 0.3$$



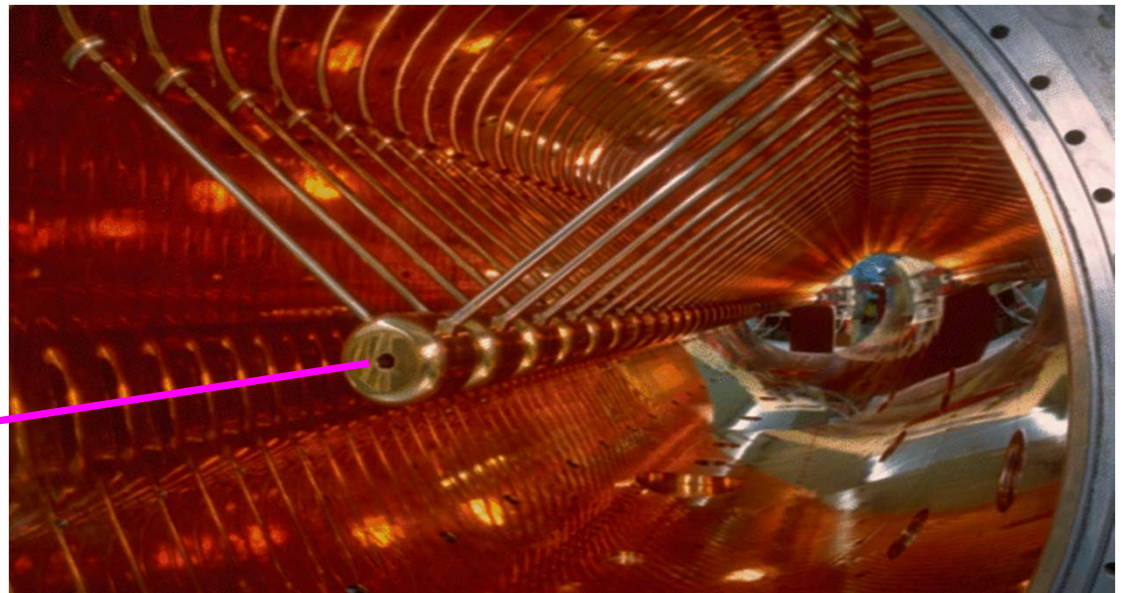
## GSI Unilac

(GSI: Heavy Ion Research Center)  
Darmstadt, Germany

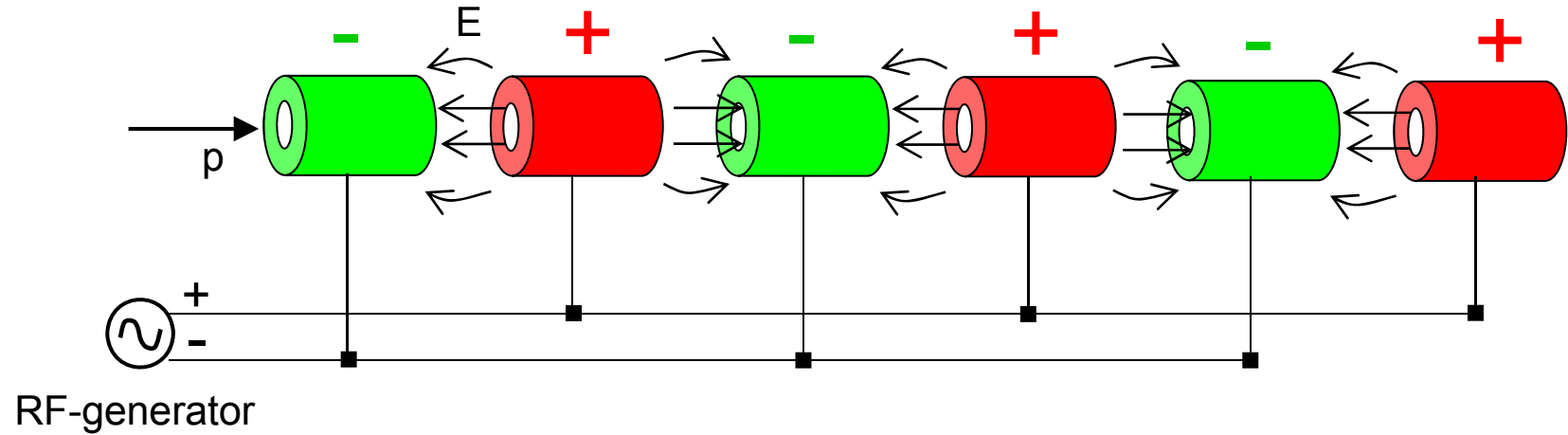
Protons/Ions

$$E \approx 20 \text{ MeV per nucleon}$$

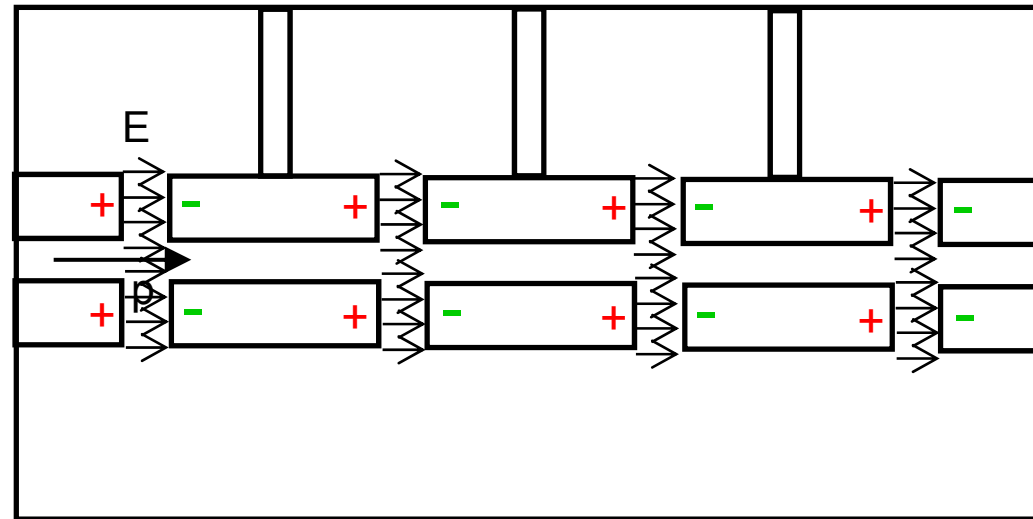
$$\beta \approx 0.04 \dots 0.2$$



## Widerøe drift-tube



## Alvarez drift-tube

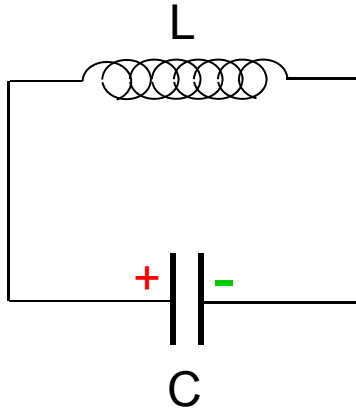




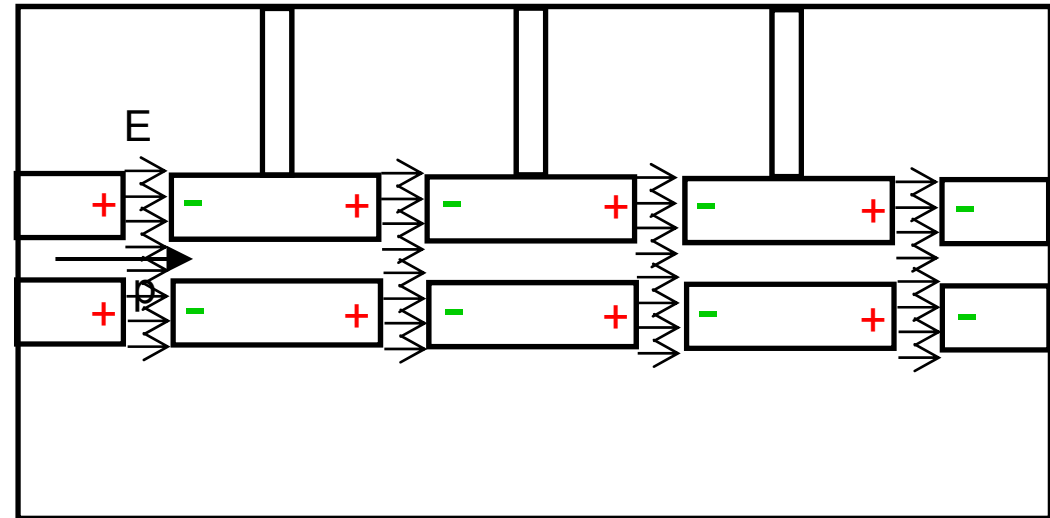
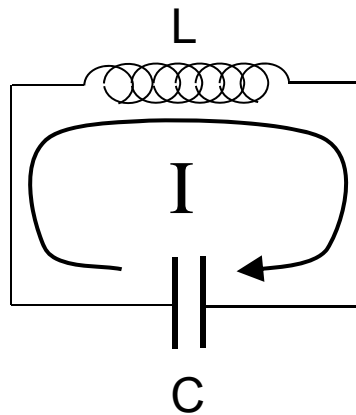
# Charges, currents and electromagnetic fields

Alvarez drift-tube

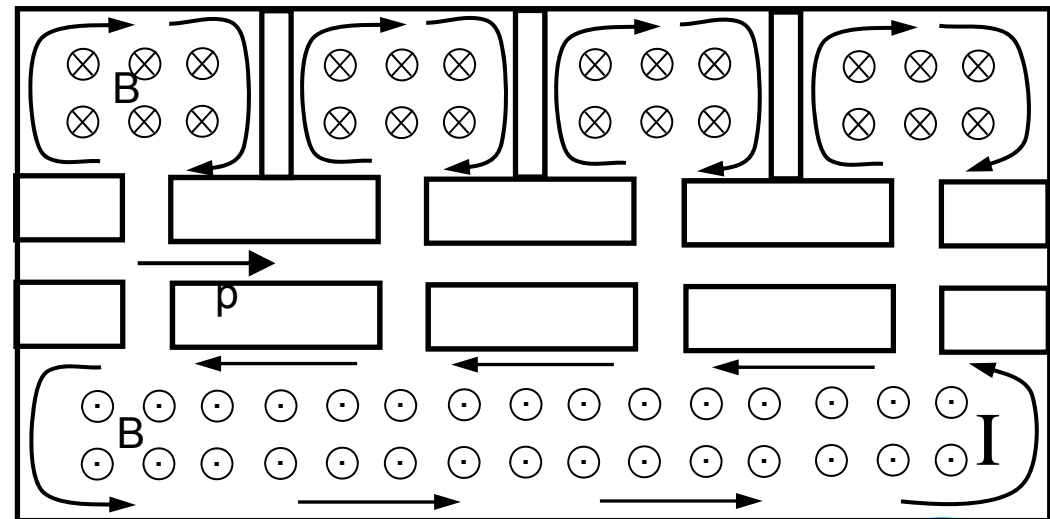
LC circuit (or resonant circuit) analogy:



a quarter of a period later:



a quarter of a period later:

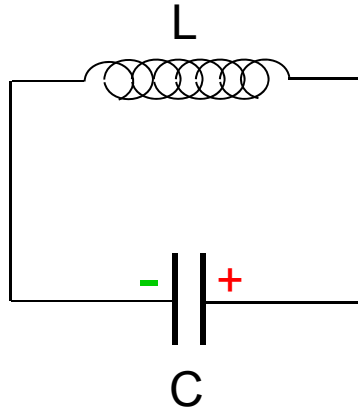


# Charges, currents and electromagnetic fields

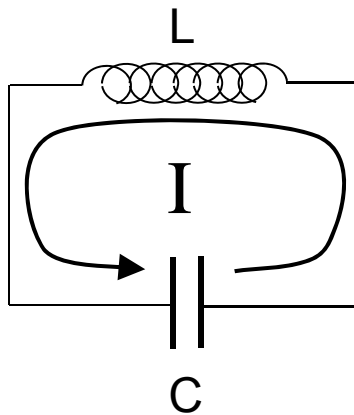
half a period later:

Alvarez drift-tube

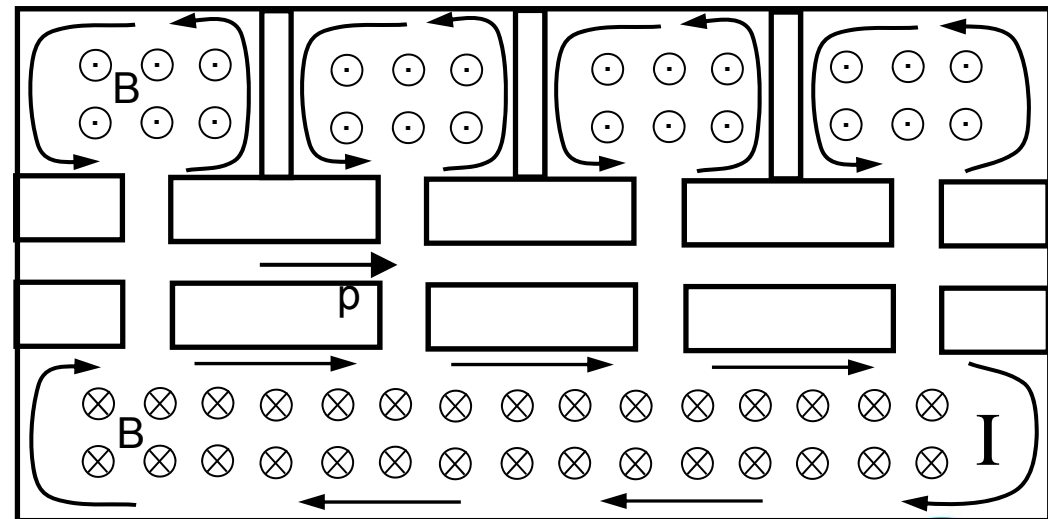
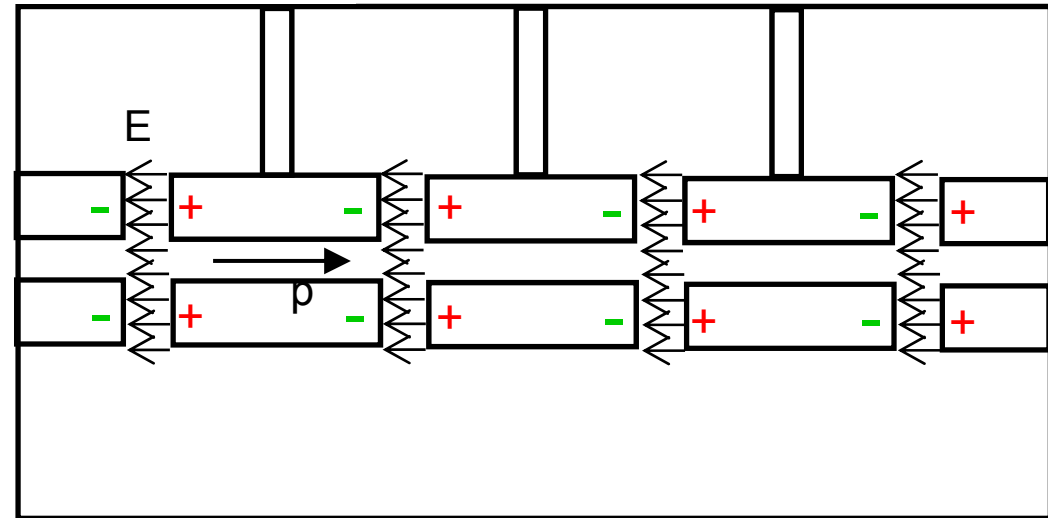
half a period later:



3 quarters of a period later:



3 quarters of a period later:

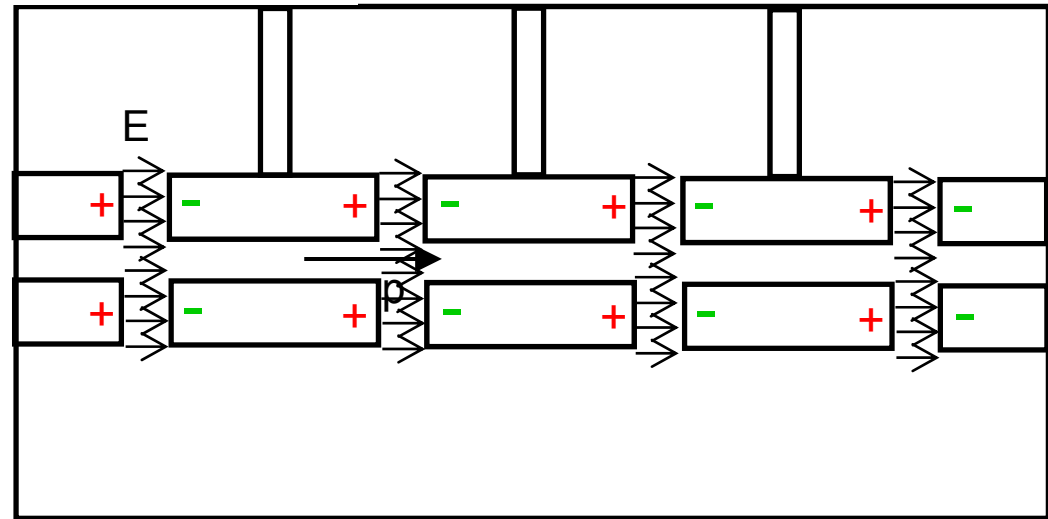
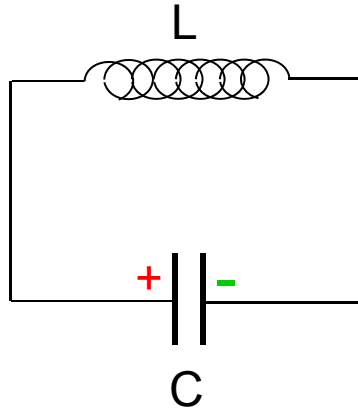


# Charges, currents and electromagnetic fields

a full period later:

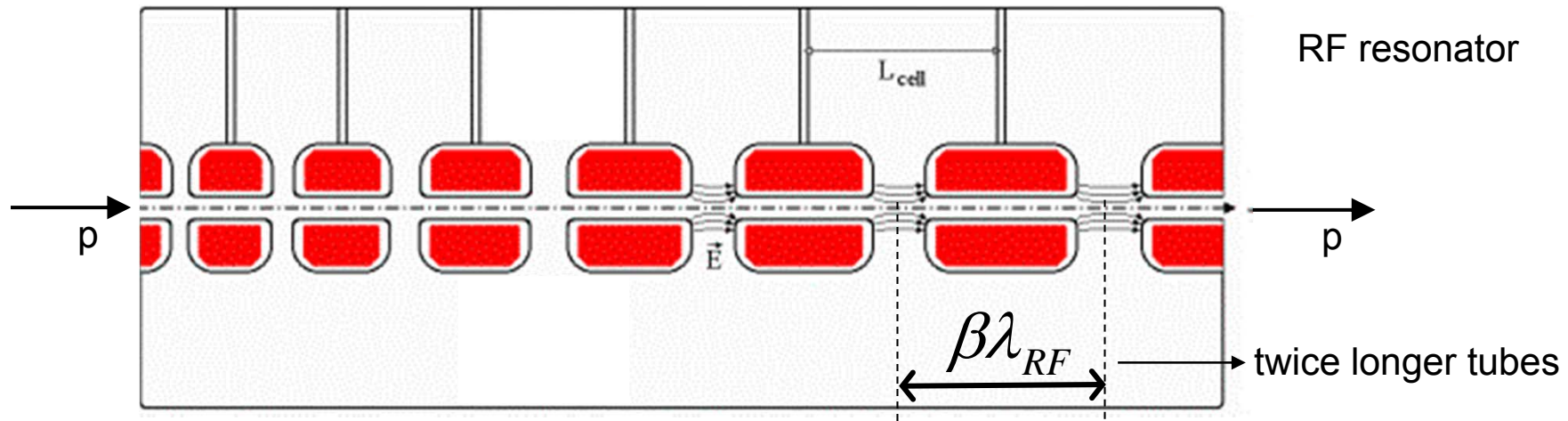
Alvarez drift-tube

a full period later:



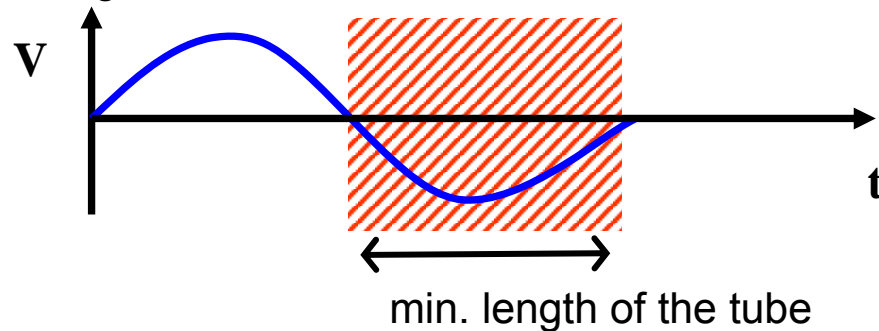
# Resonant cavities

Alvarez drift-tube structure:



higher frequencies possible  $\rightarrow$  shorter accelerator

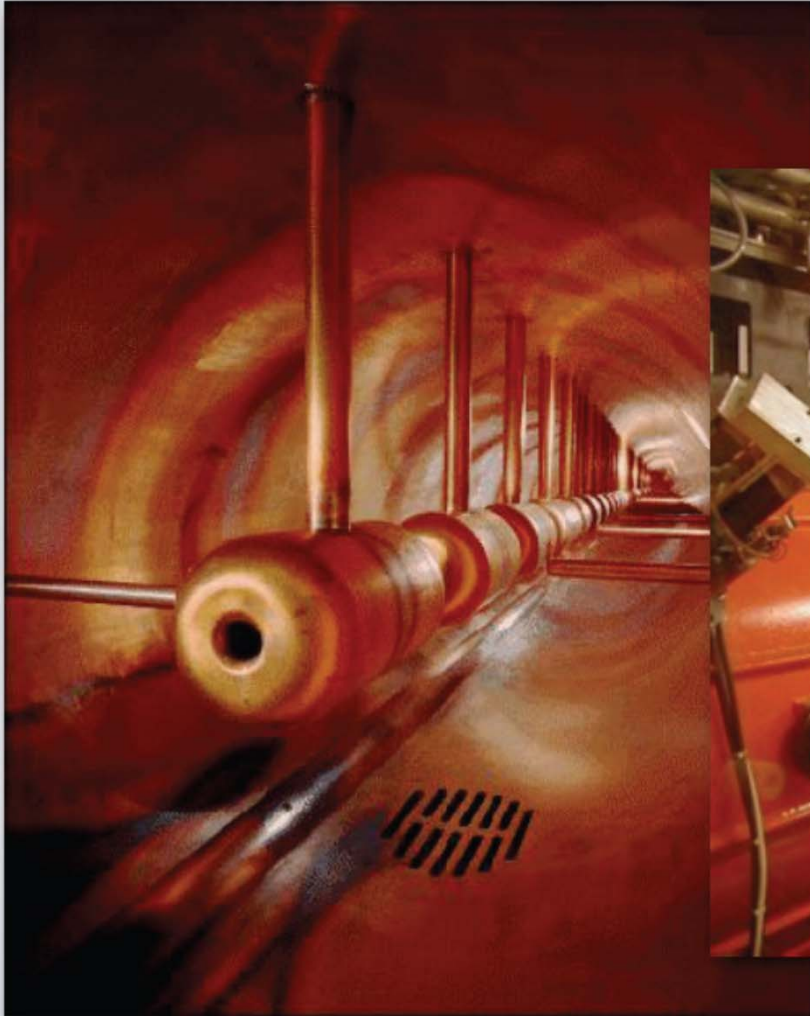
voltage between tubes



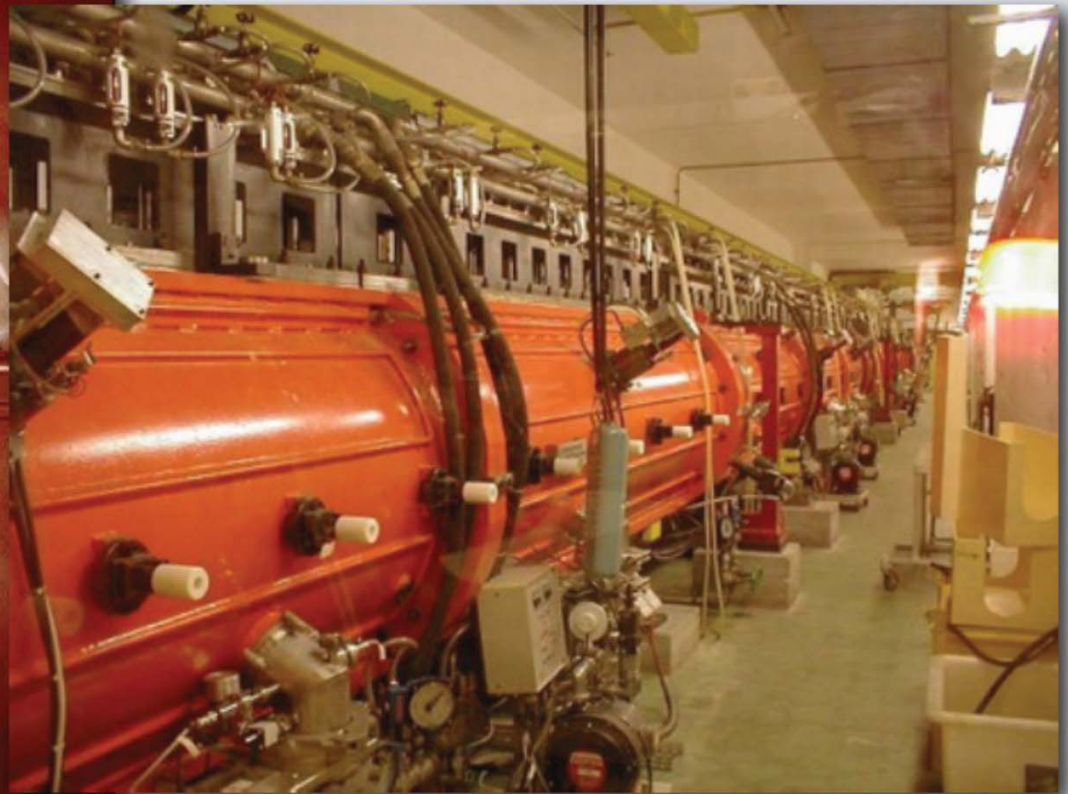
preferred solution  
for ions and protons  
up to few hundred MeV

# Examples

inside a drift tube linac



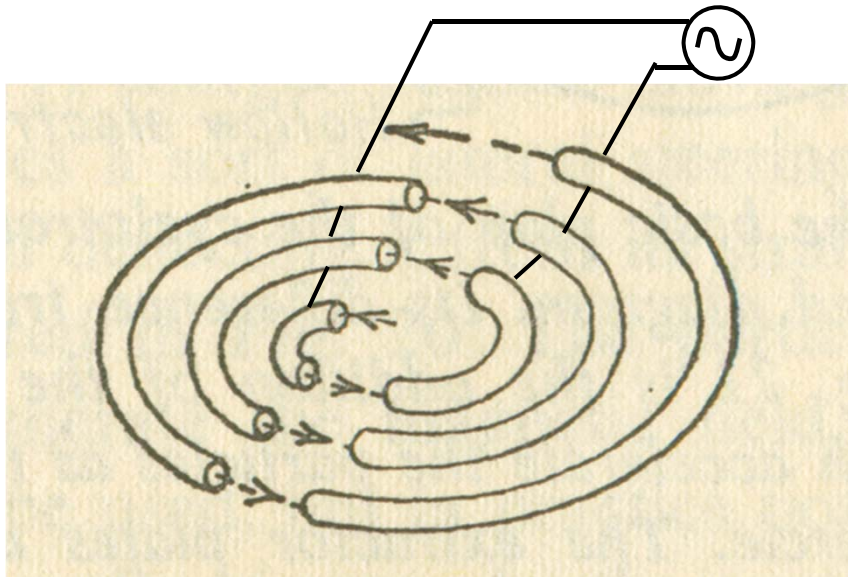
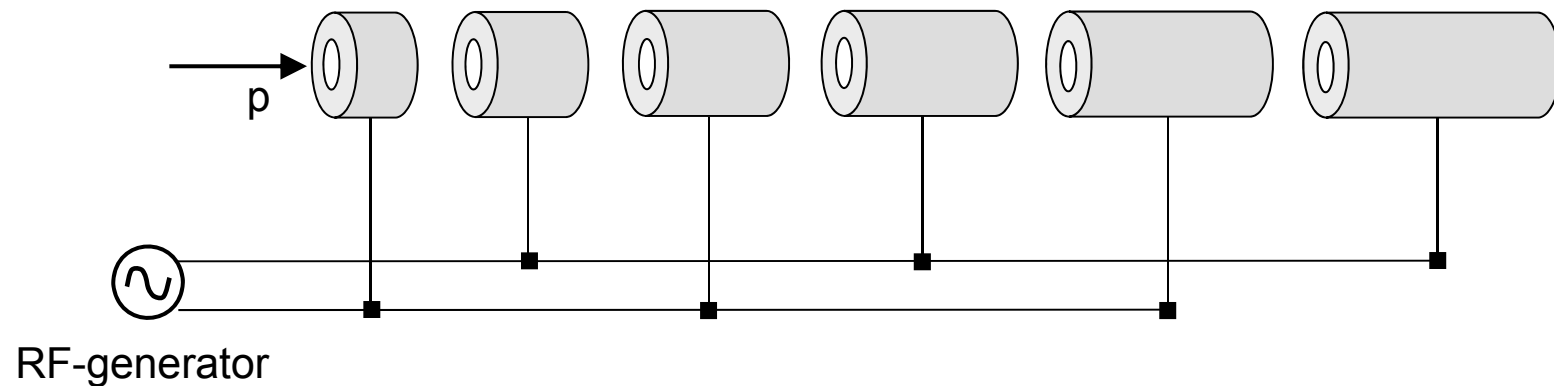
Linac2 at CERN, 50 MeV





# Acceleration using Radio-Frequency (RF) generators

original Widerøe drift-tube principle

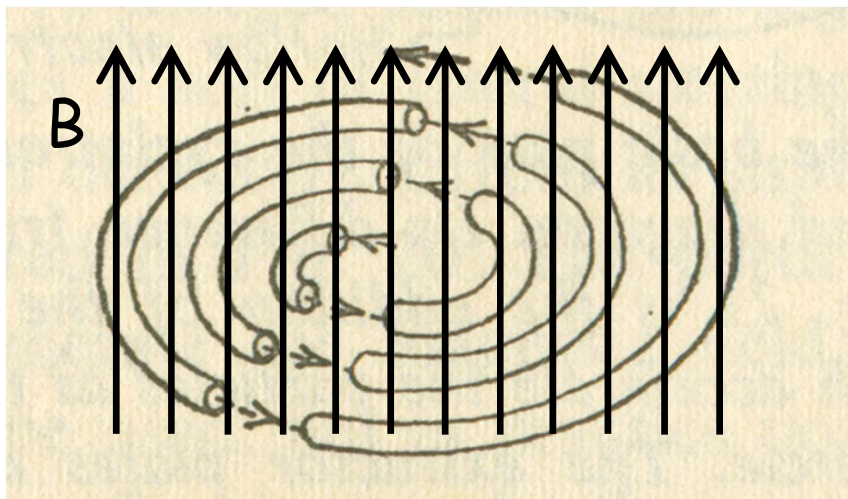
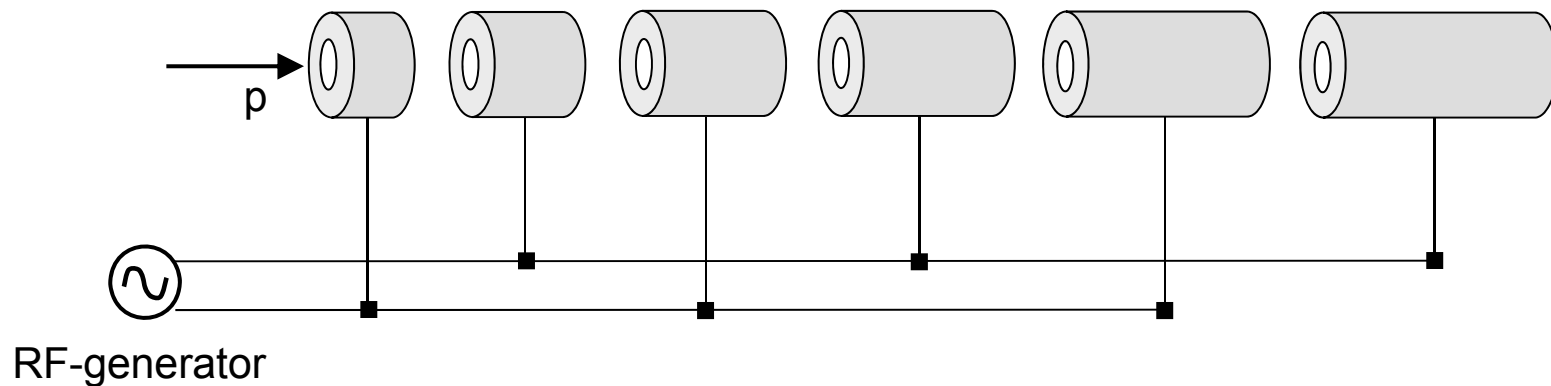


first concept of the 'cyclotron' (1929)  
(from E. Lawrence)

drift-tube linac "rolled up"

# Acceleration using Radio-Frequency (RF) generators

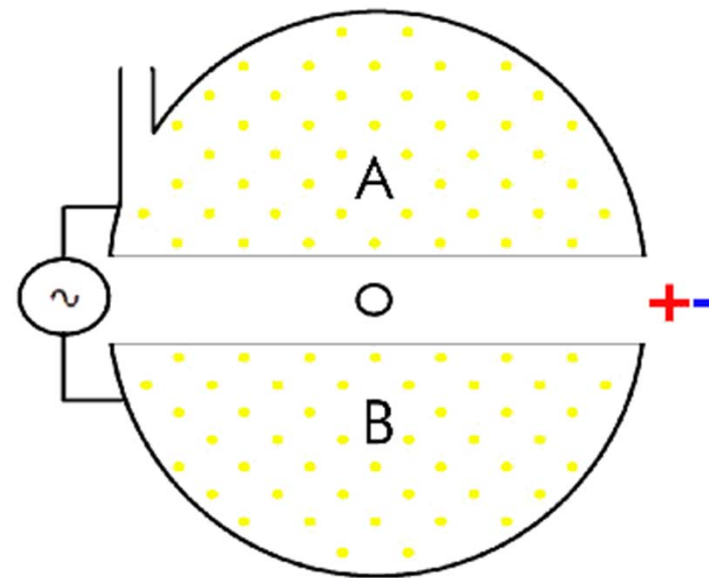
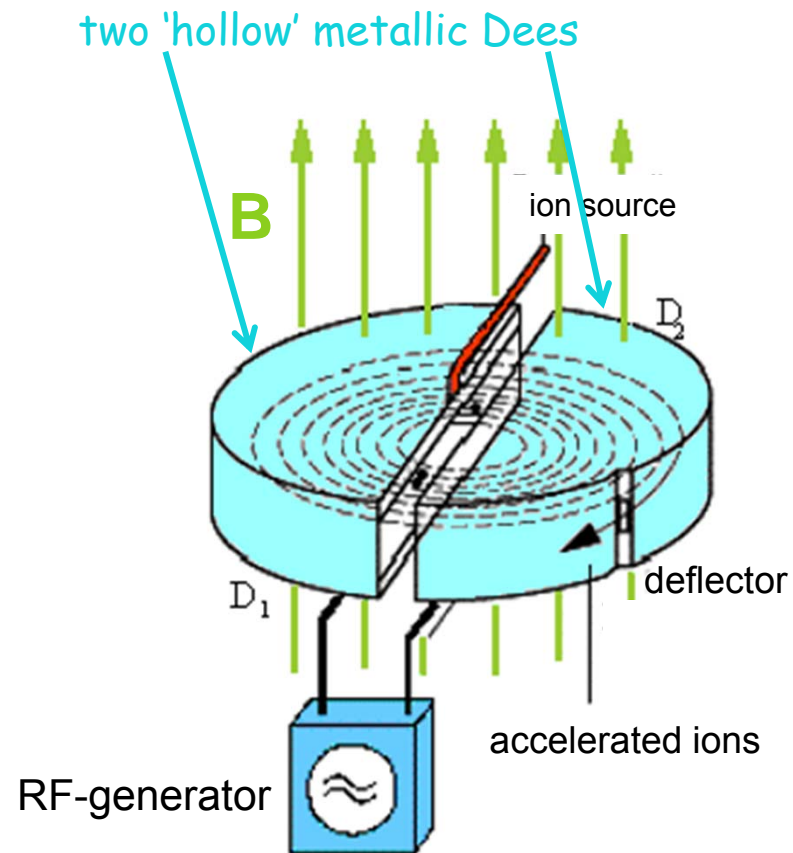
original Widerøe drift-tube principle

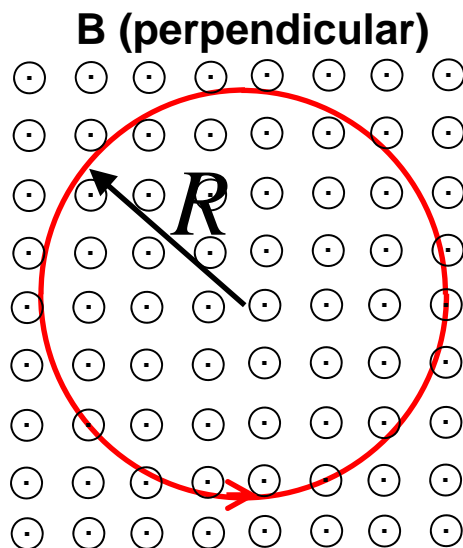


first concept of the 'cyclotron' (1929)  
(from E. Lawrence)

drift-tube linac "rolled up"

# Cyclotron





$$\vec{F} = \frac{d\vec{p}}{dt} = q \vec{v} \times \vec{B}$$

momentum      charge      velocity      magnetic field  
 of the particle

circular motion:

$$\vec{B} \perp \vec{v} \rightarrow F = q v B = m \frac{v^2}{R} \Rightarrow R = \frac{m v}{q B}$$

time for one revolution:  $T = \frac{2\pi R}{v} = 2\pi \frac{m}{q B} = \text{const.}$

# Cyclotron

... in a uniform constant magnetic field:

$$T = 2\pi \frac{m}{q B} = \text{const.} \quad (\text{for non-relativistic velocities})$$

$$\text{cyclotron frequency: } \omega = \frac{2\pi}{T} = \frac{q}{m} B = \text{const.}$$

→ protons up to 15 MeV ( $\beta = 0.1$ )



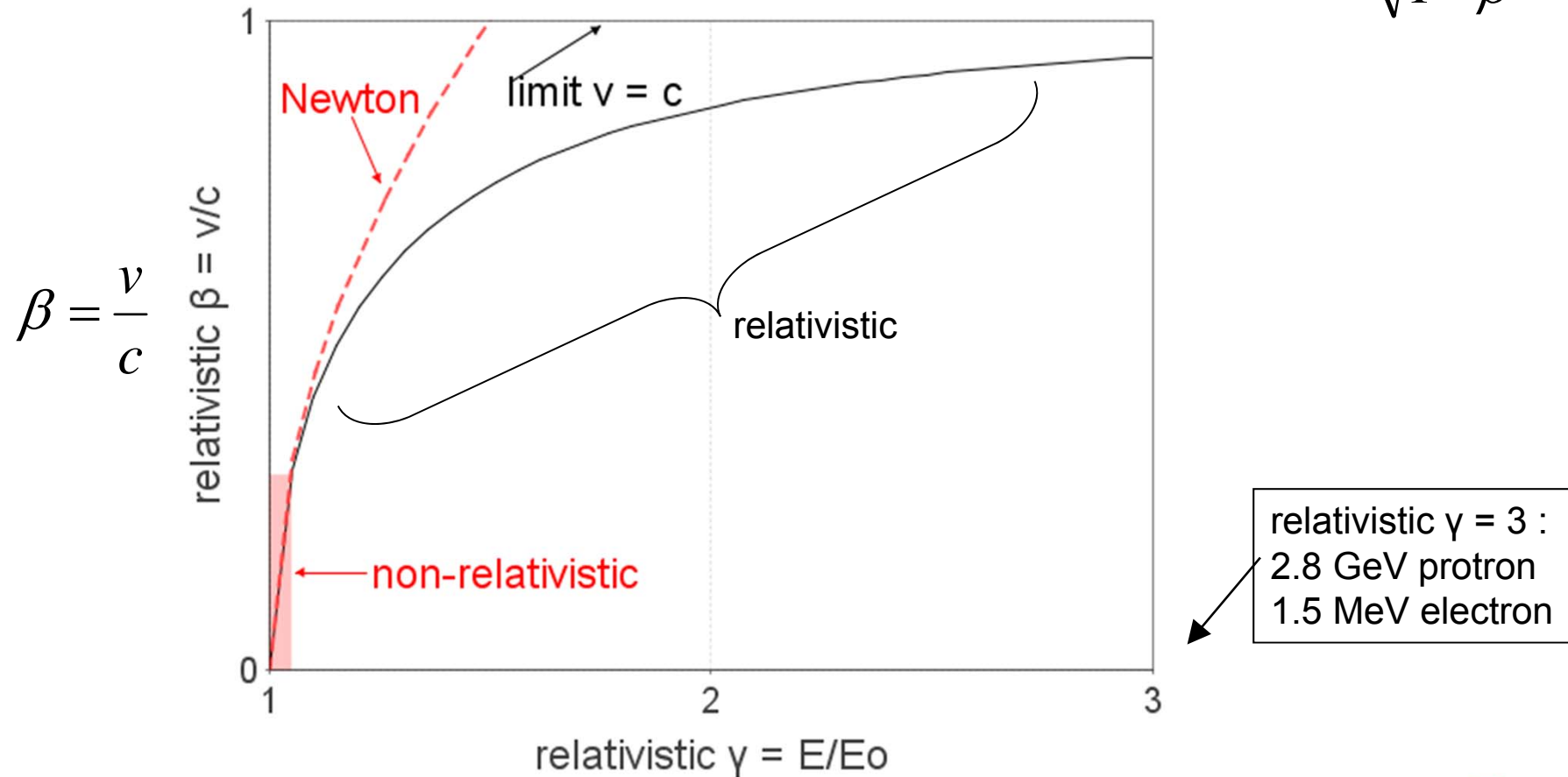


# Velocity as function of energy $\rightarrow \beta$ as function of $\gamma$

Newton:  $E_{kin} = \frac{1}{2}mv^2$

Einstein:

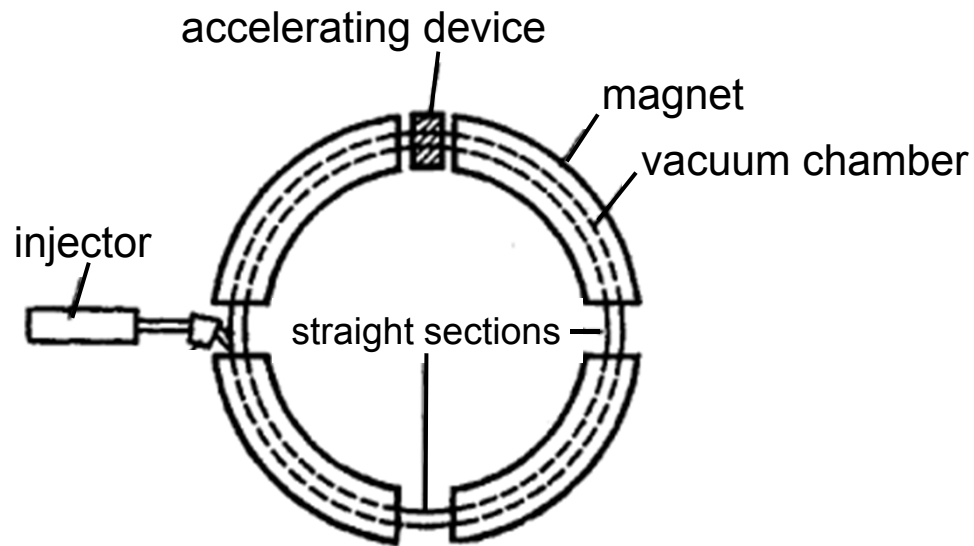
$$E = E_o + E_{kin} = \gamma mc^2 = \frac{mc^2}{\sqrt{1-\beta^2}}$$





Cyclotron at Fermilab, Chicago IL, USA

# Circular accelerators



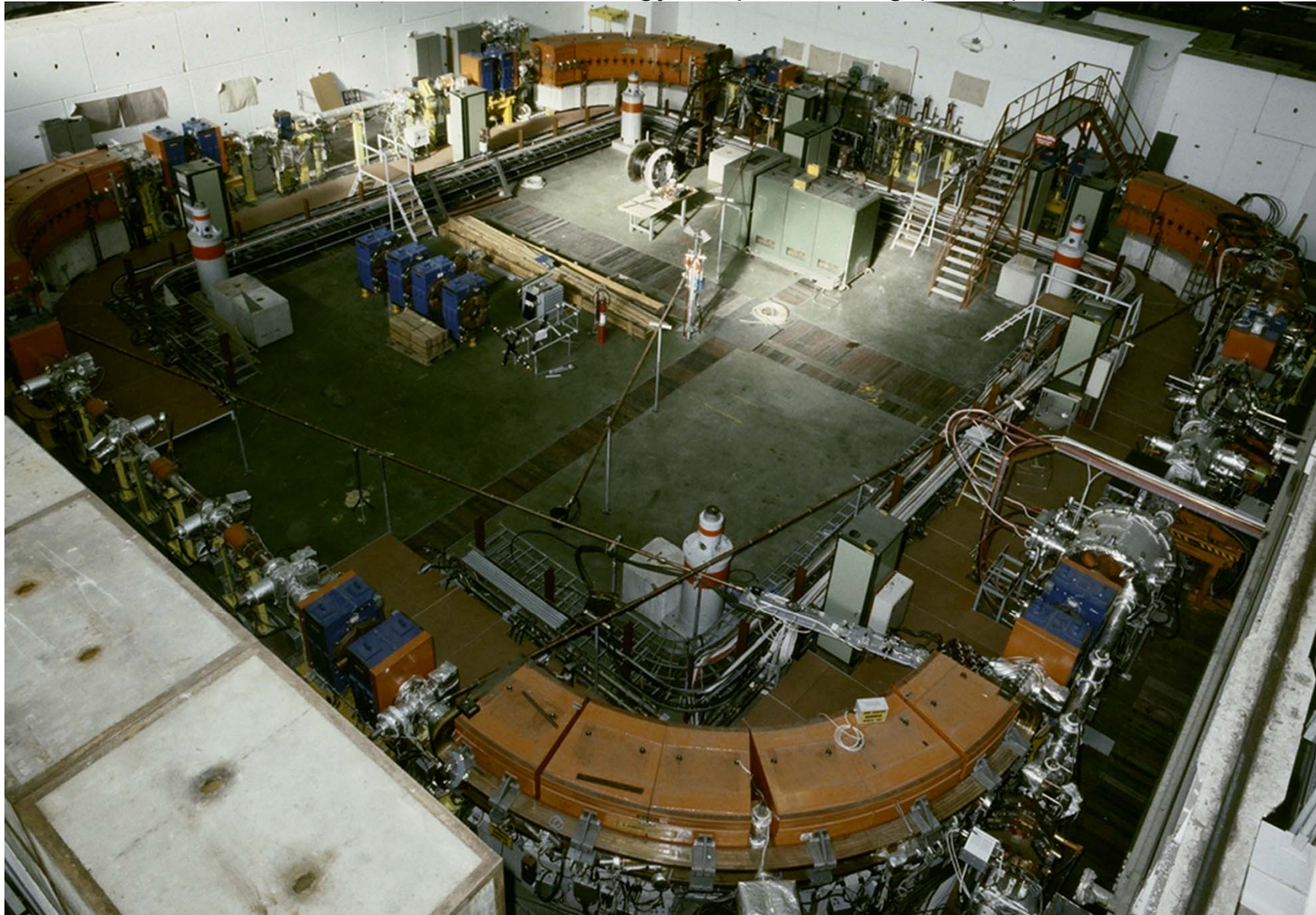
$$\vec{B} \perp \vec{v} \rightarrow F = q v B = m \frac{v^2}{R} \Rightarrow R = \frac{m v}{q B}$$

synchrotron:  $R$  is constant,  
→ increase  $B$  synchronously with  $E$  of particle



# Circular accelerators

Low Energy Antiproton Ring (LEAR) at CERN





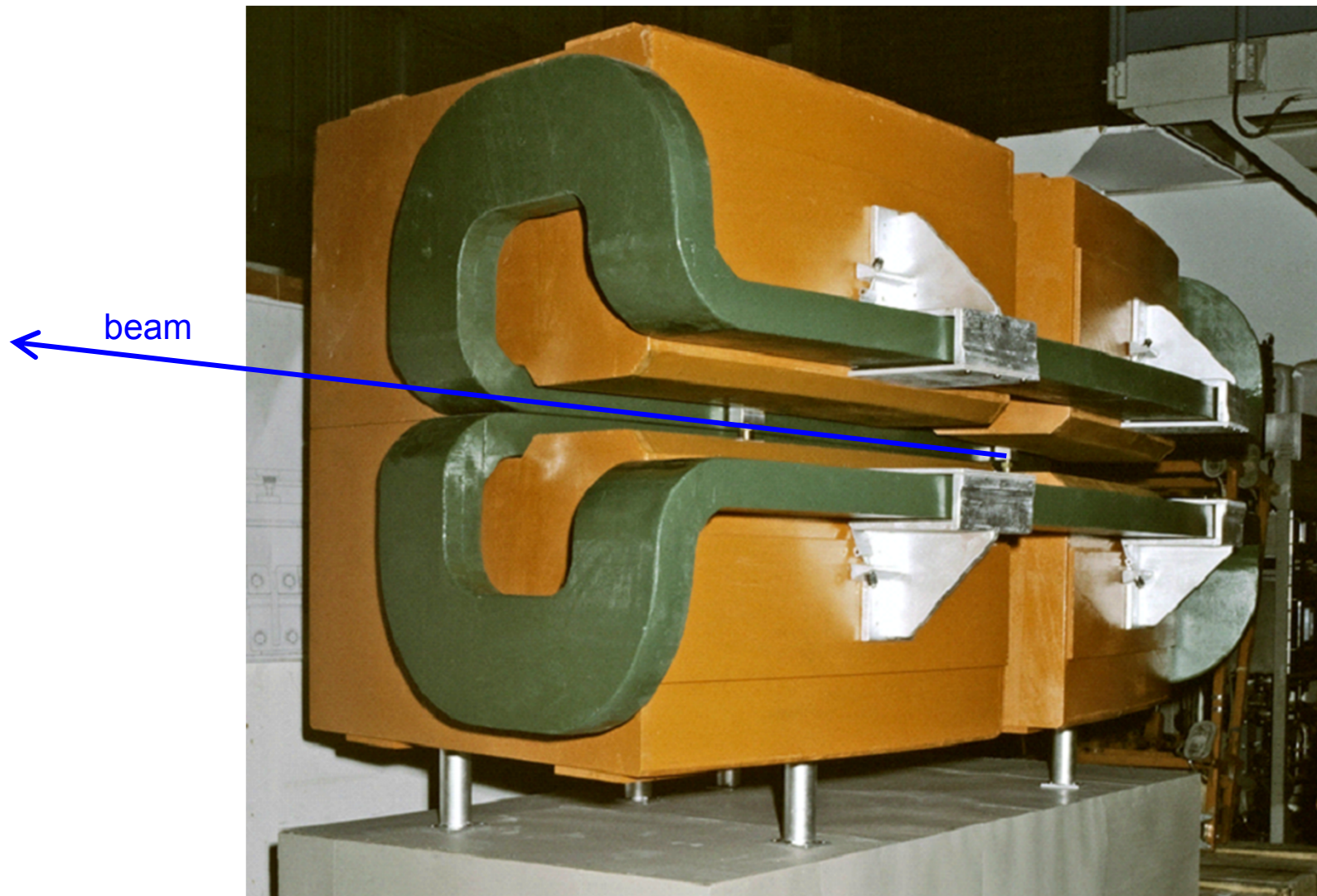
# DESY (Deutsches Elektronen Synchrotron)

DESY: German electron synchrotron, 1964, 7.4 GeV

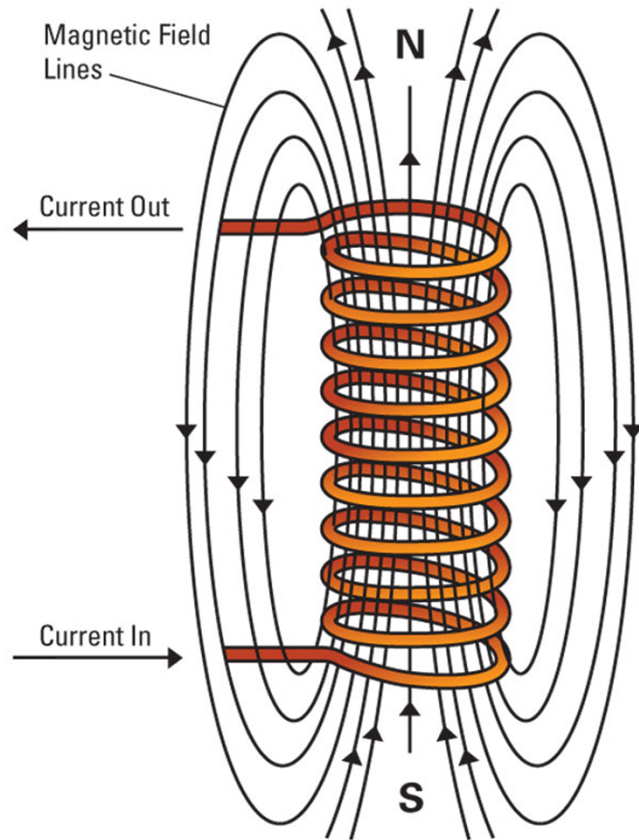




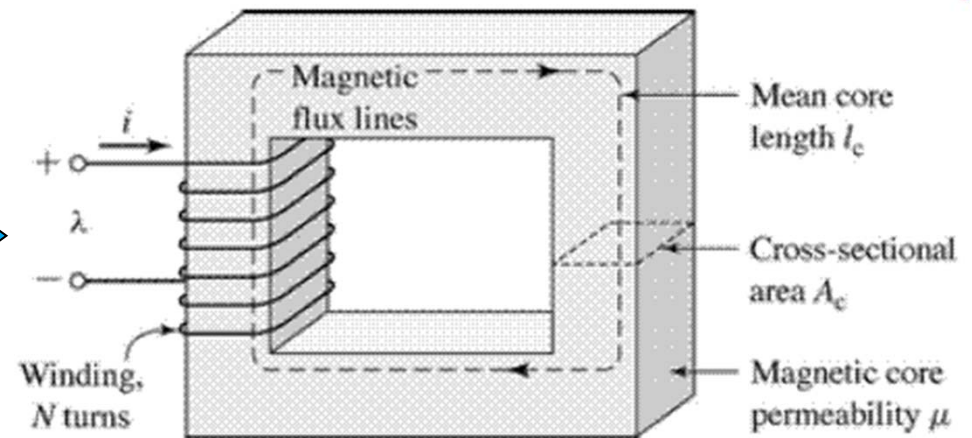
# Dipole magnet



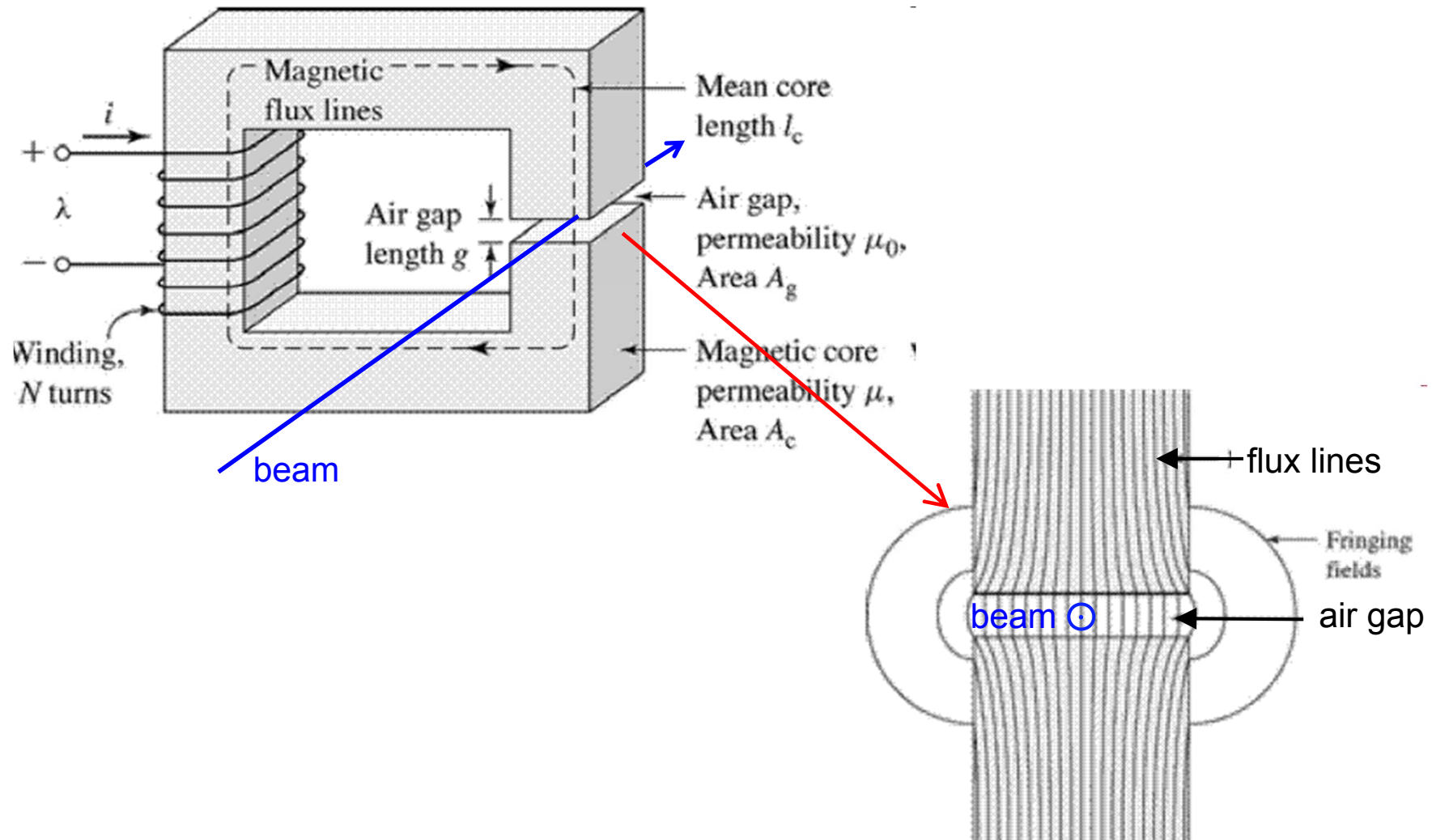
# Electromagnet



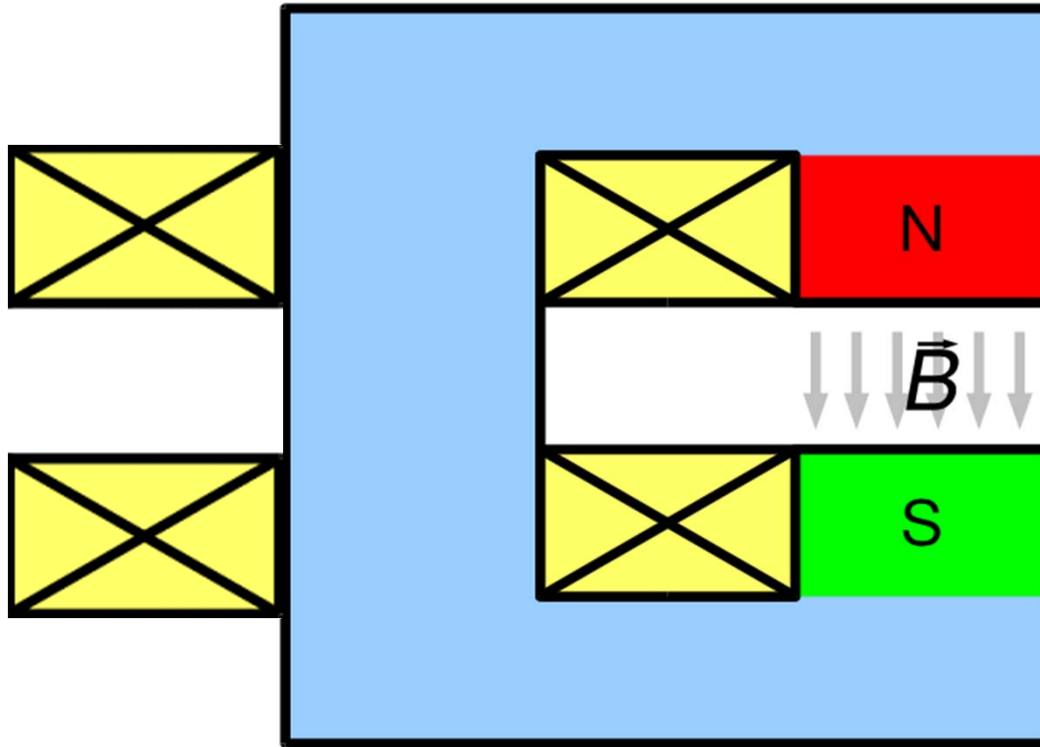
permeability of iron = 300...10000 larger than air



# Dipole magnet



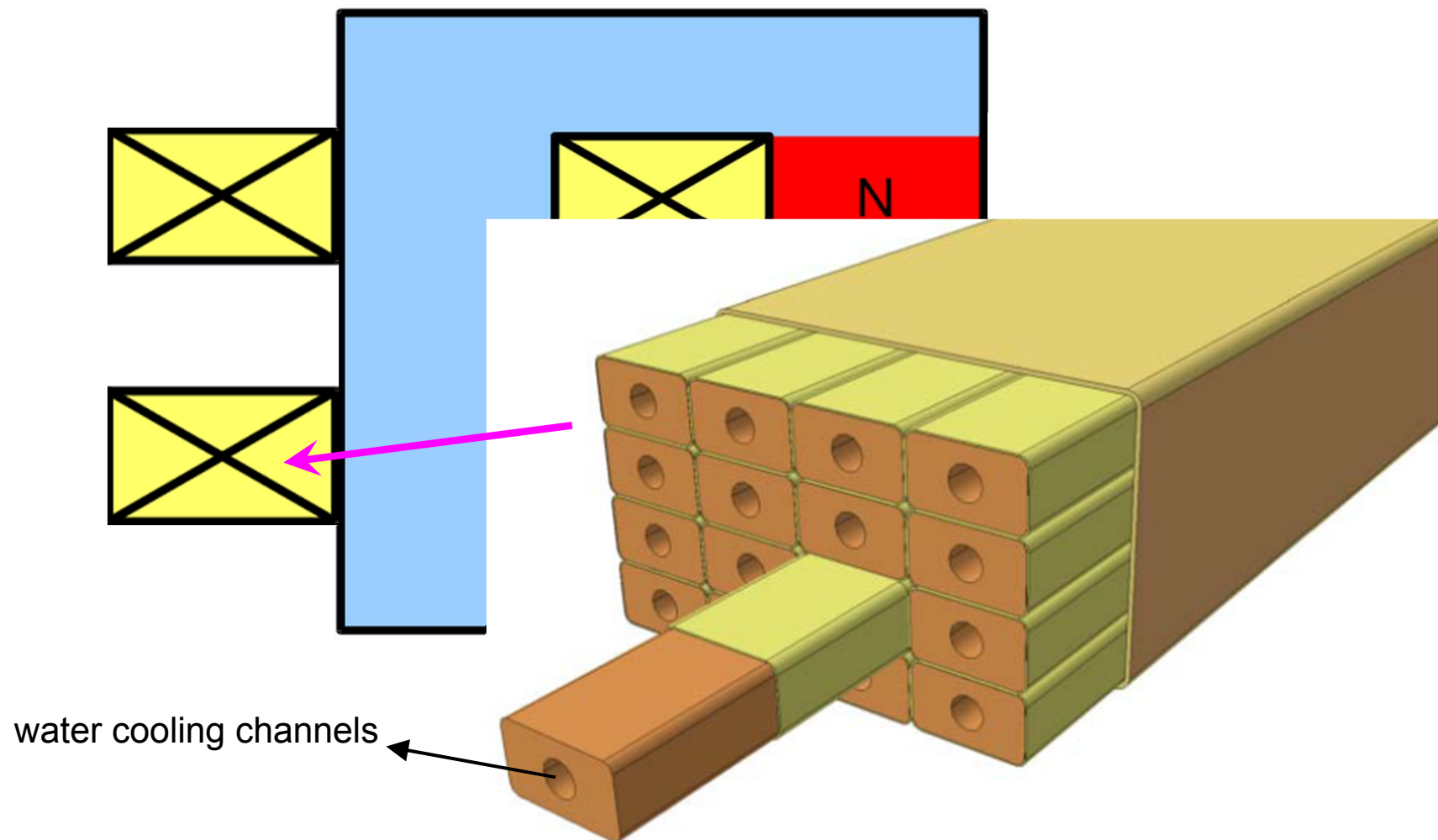
# Dipole magnet cross section



Max.  $B \rightarrow$  max. current  $\rightarrow$  large conductor cables

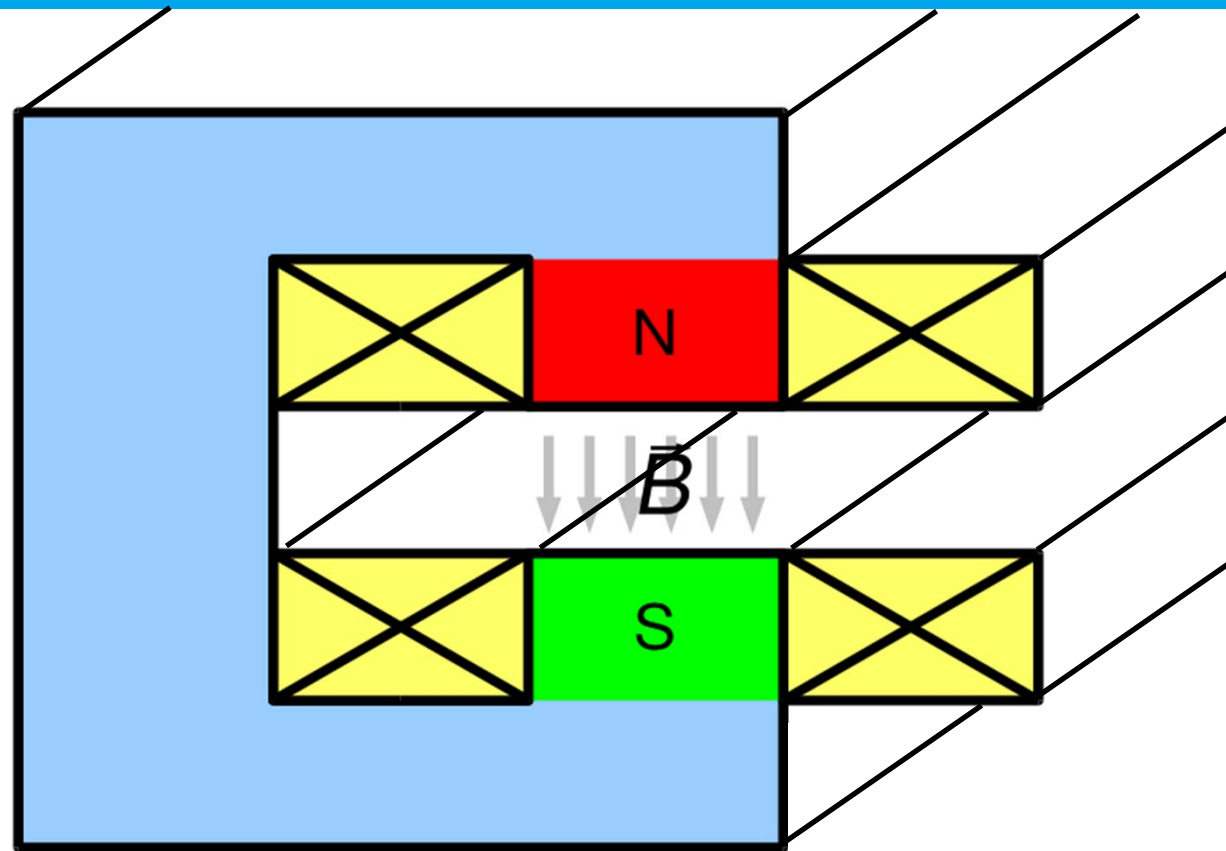
$$\text{Power dissipated: } P = R \cdot I^2$$

# Dipole magnet cross section

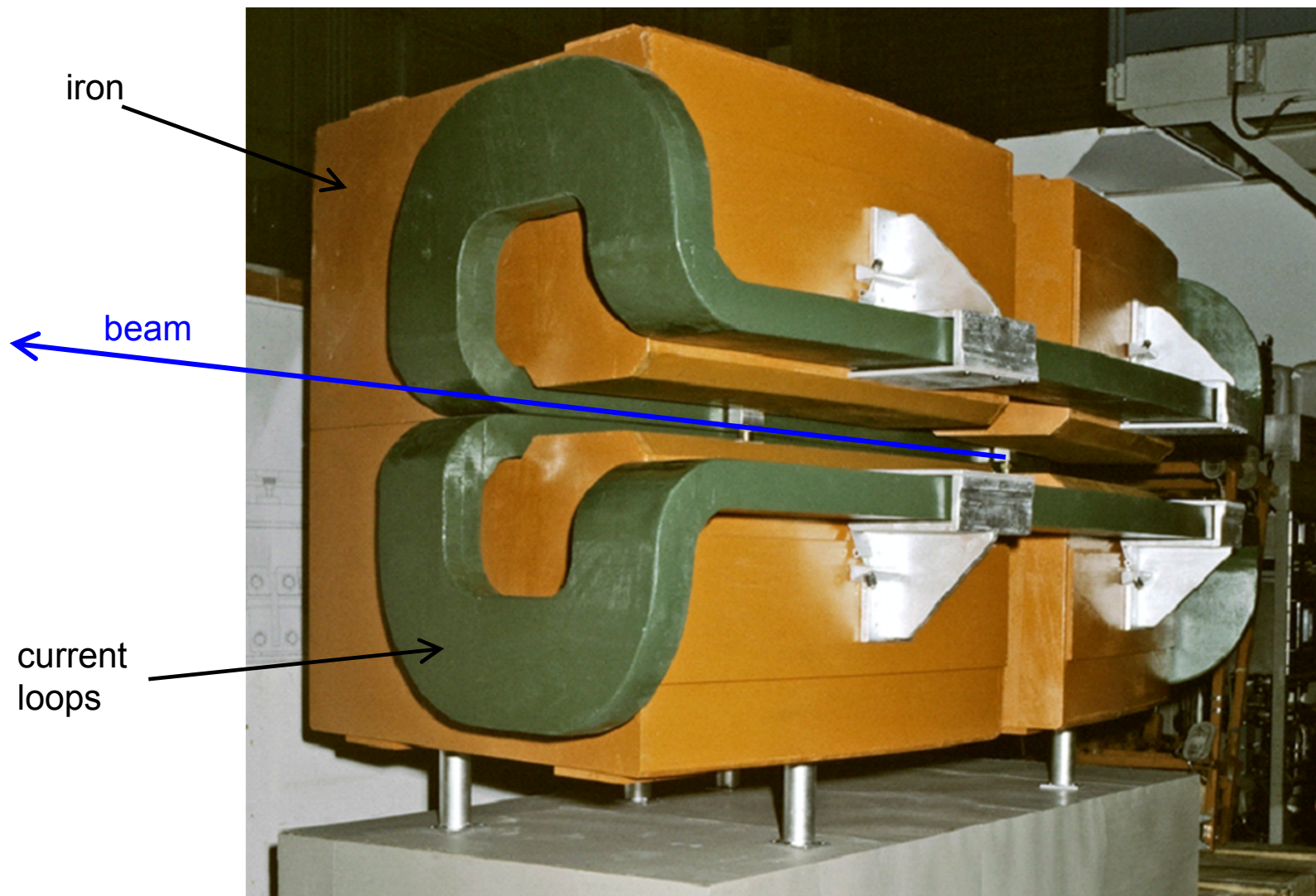




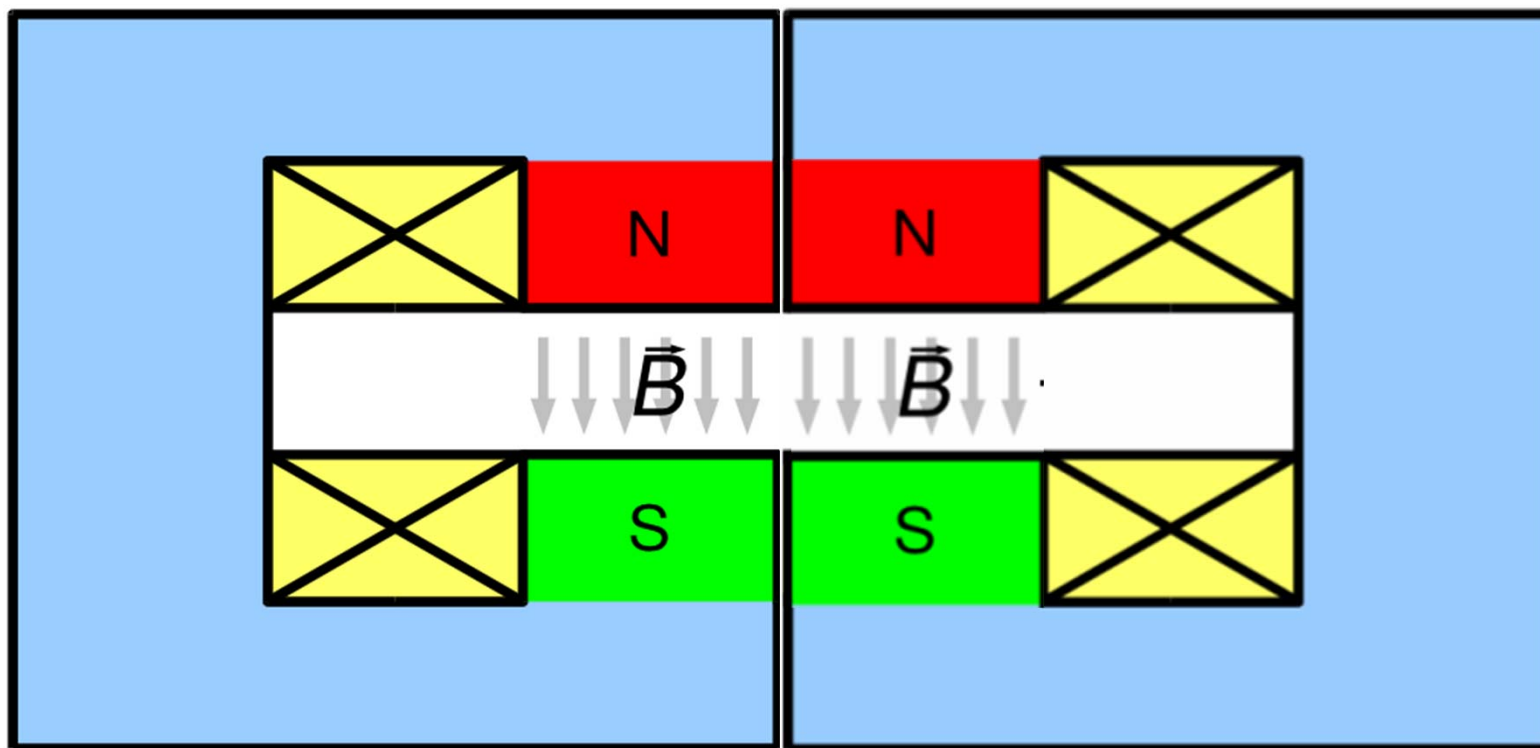
# Dipole magnet cross section



# Dipole magnet

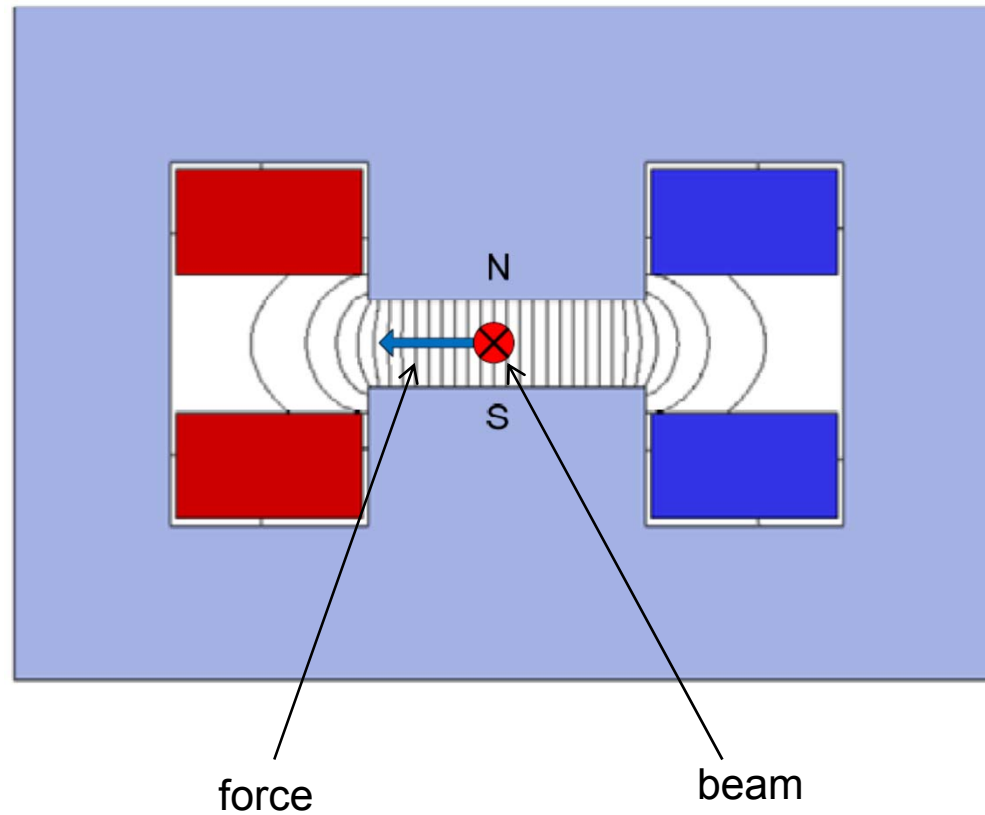


# Dipole magnet cross section

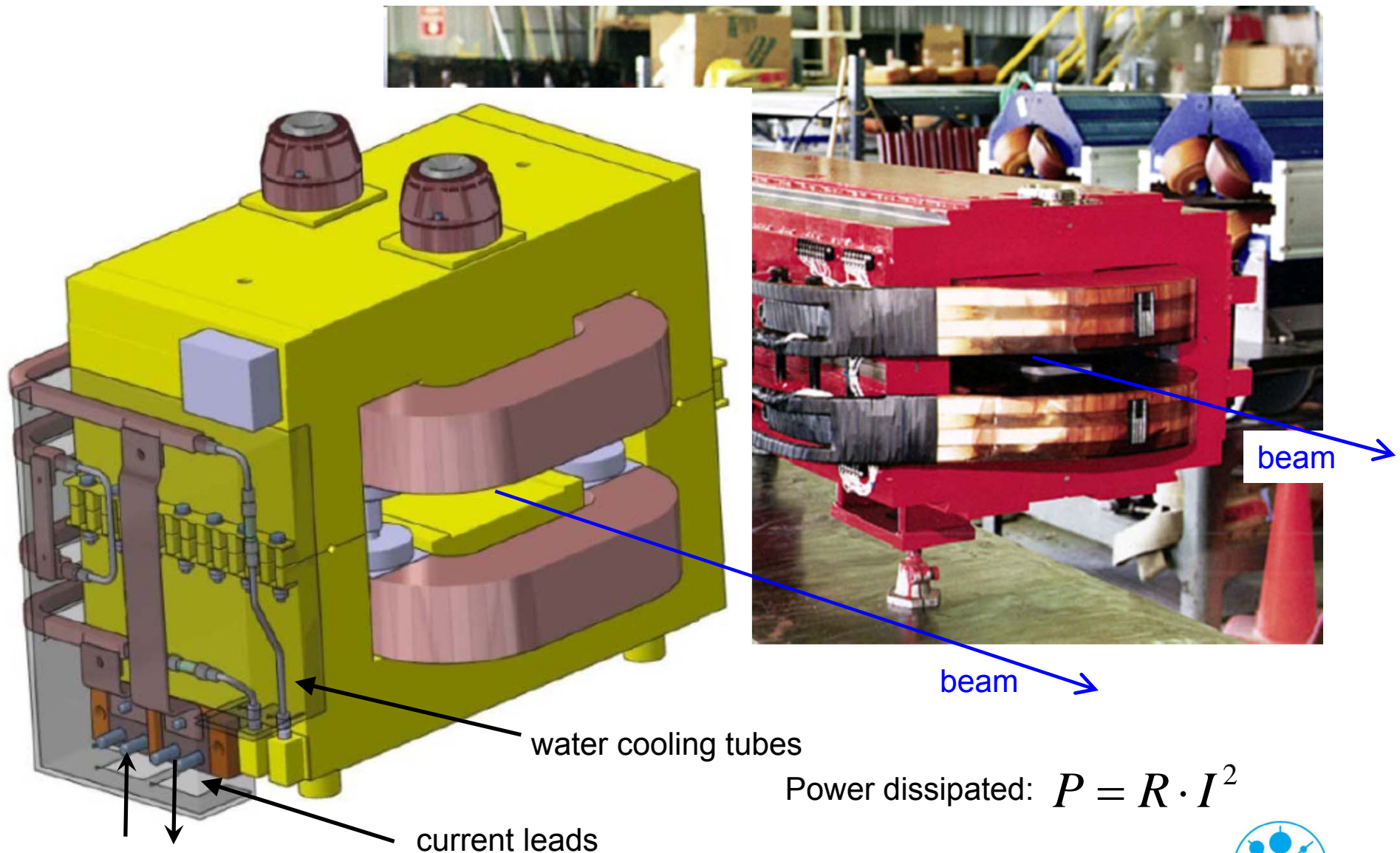


C magnet + C magnet = H magnet

# Dipole magnet cross section (another design)



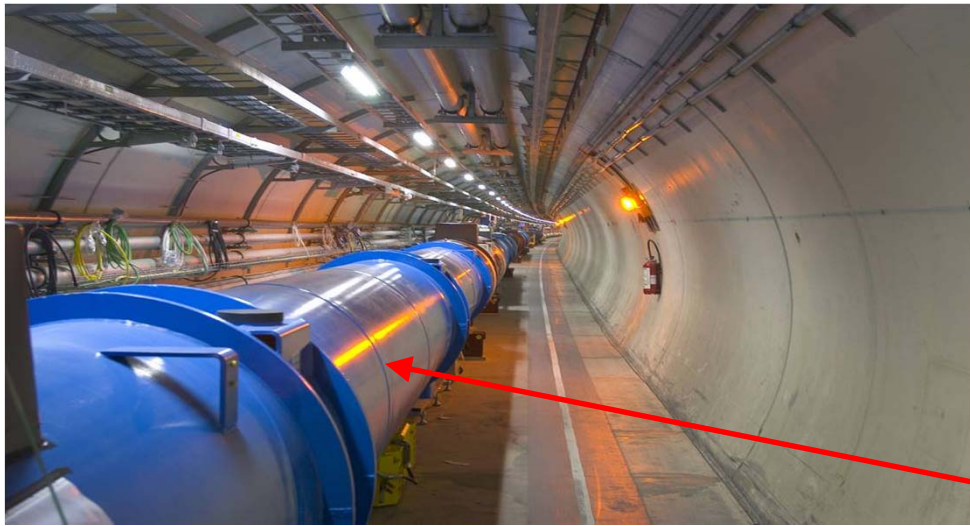
# Dipole magnet cross section (another design)



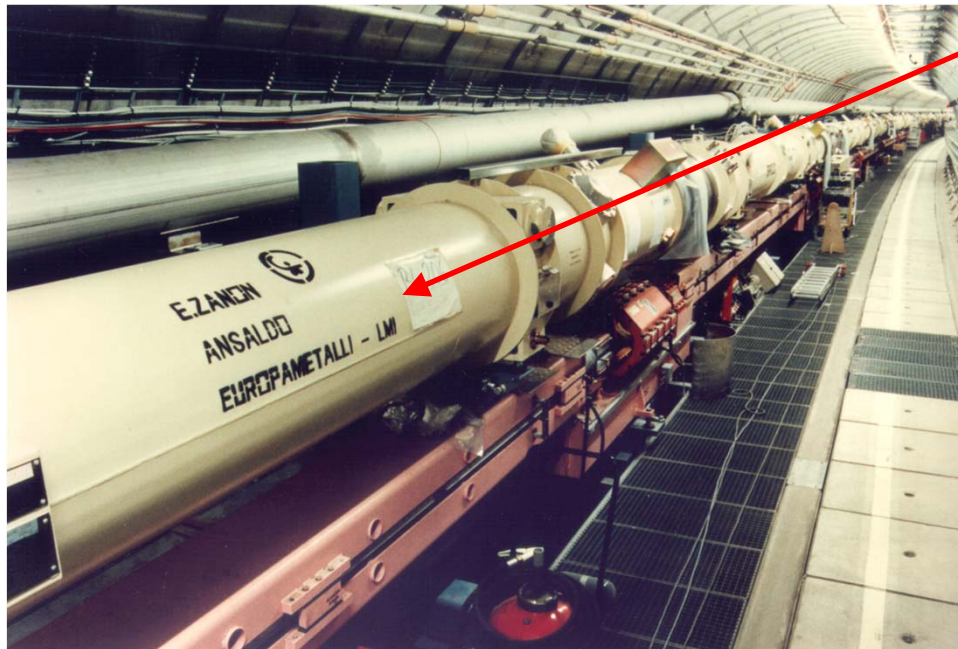
Power dissipated:  $P = R \cdot I^2$



# Superconducting dipole magnets



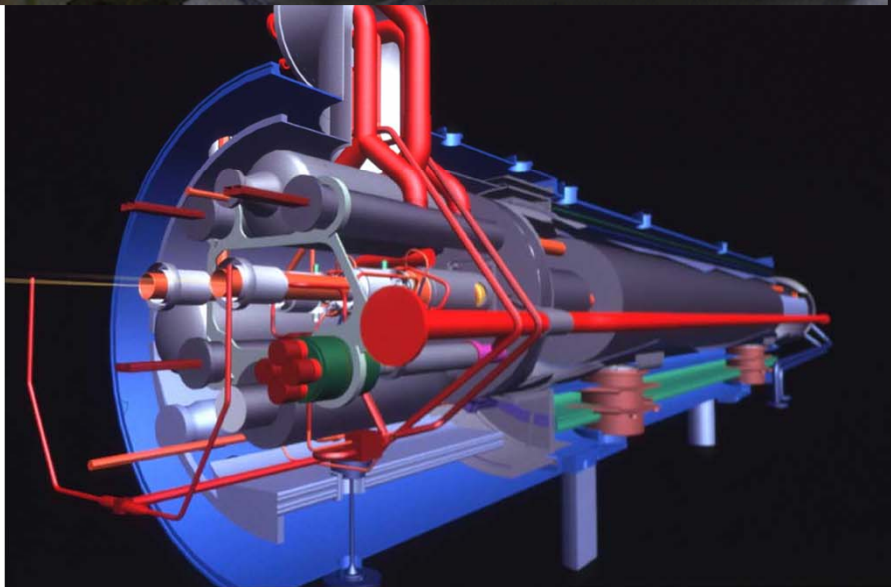
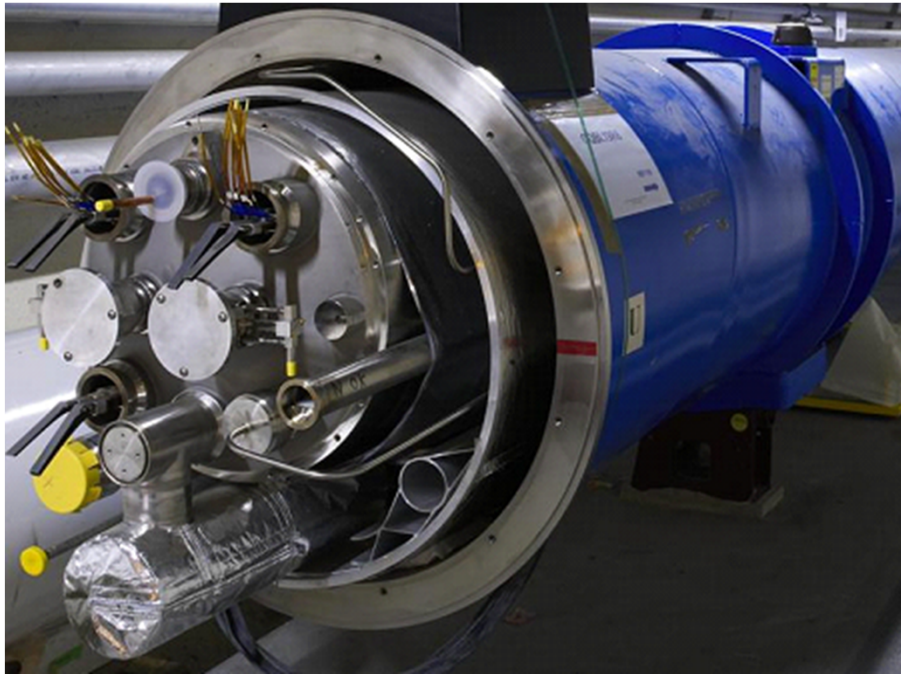
LHC



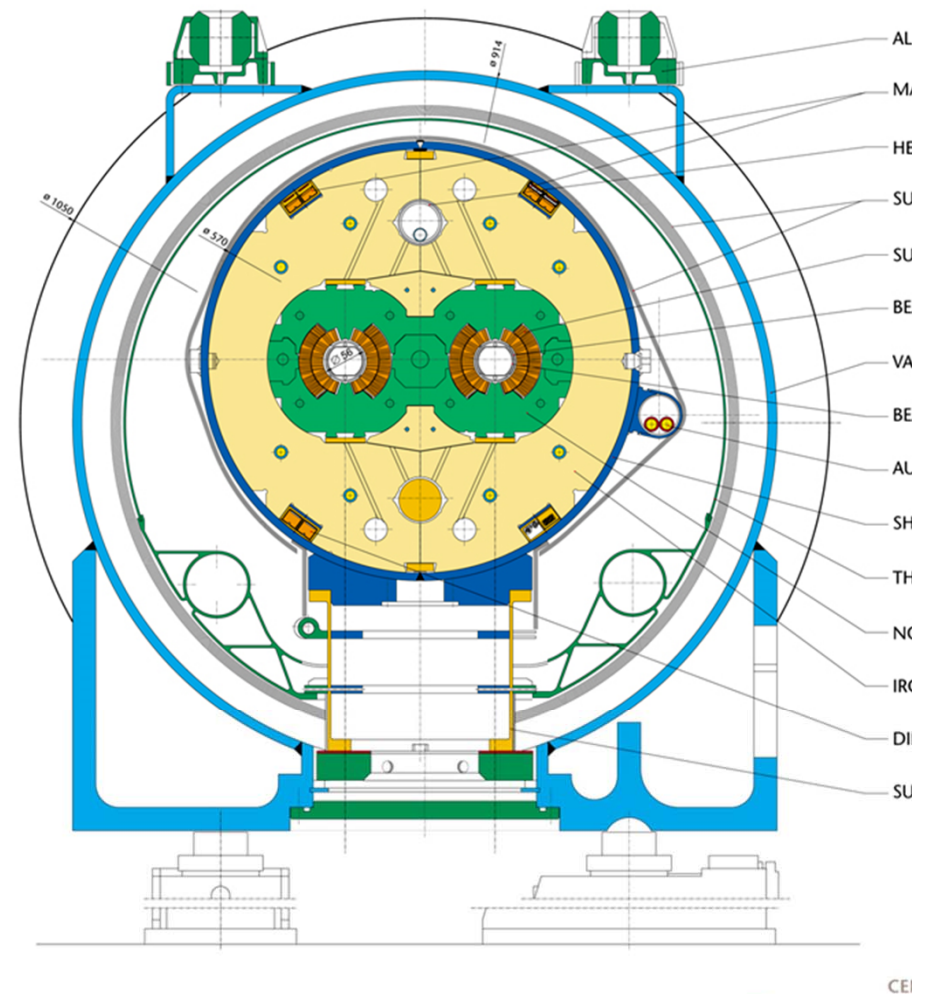
HERA

superconducting dipoles

# Superconducting dipole magnets



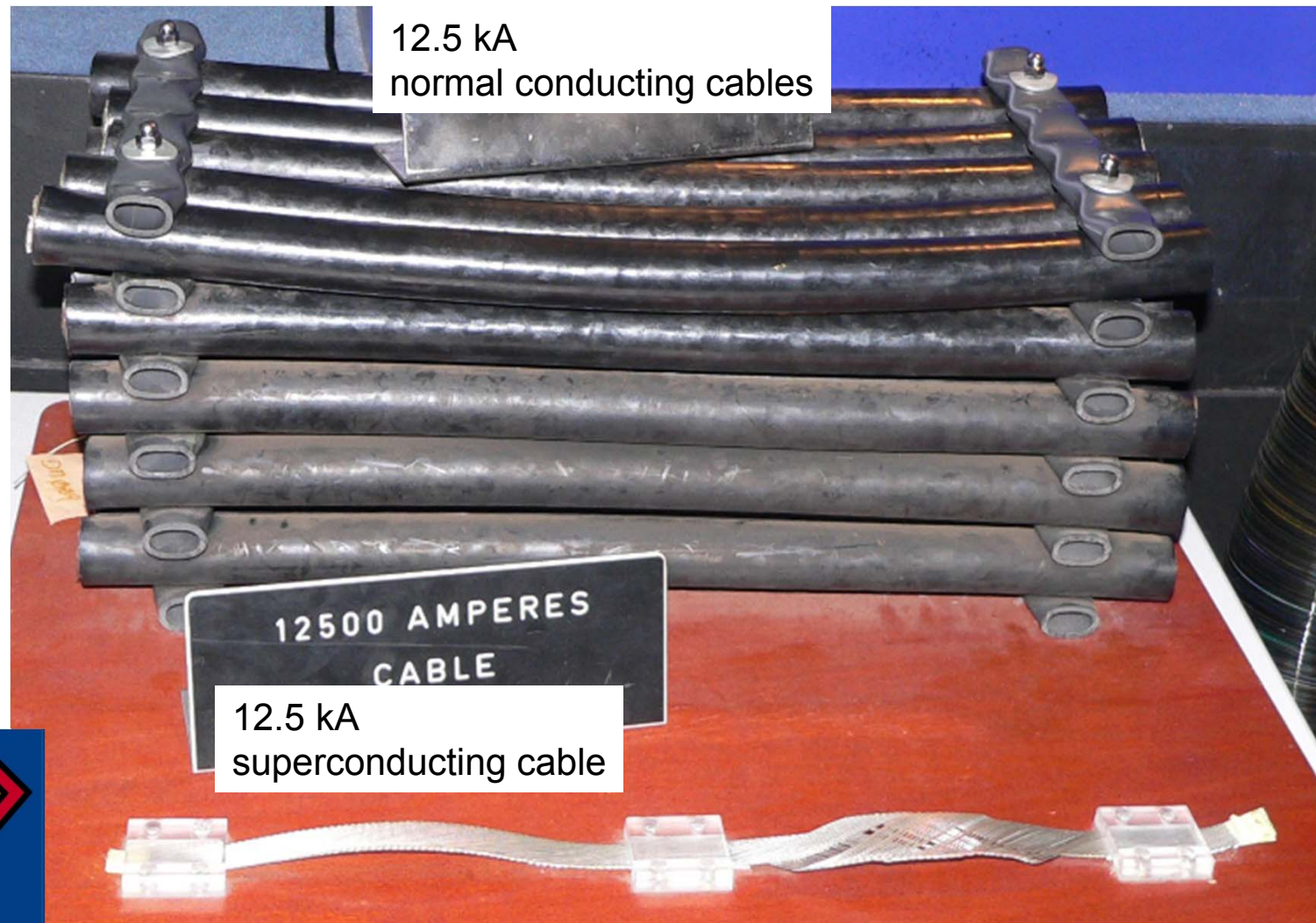
LHC DIPOLE : STANDARD CROSS-SECTION



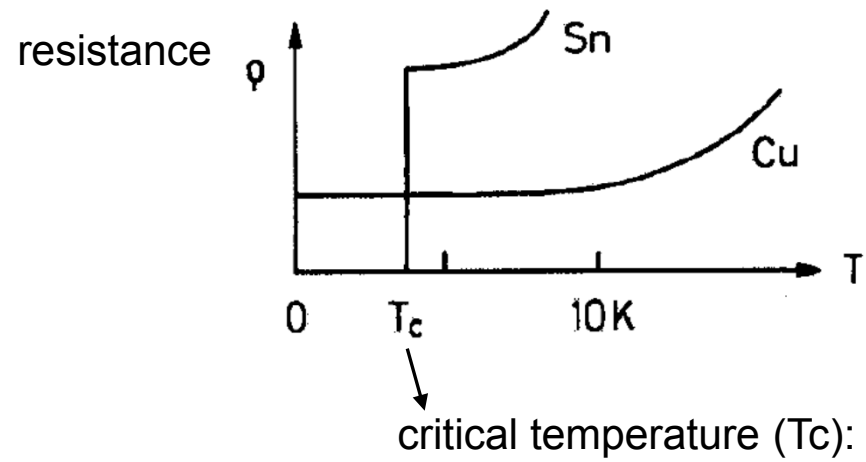
CEI



# Superconductivity



# Superconductivity



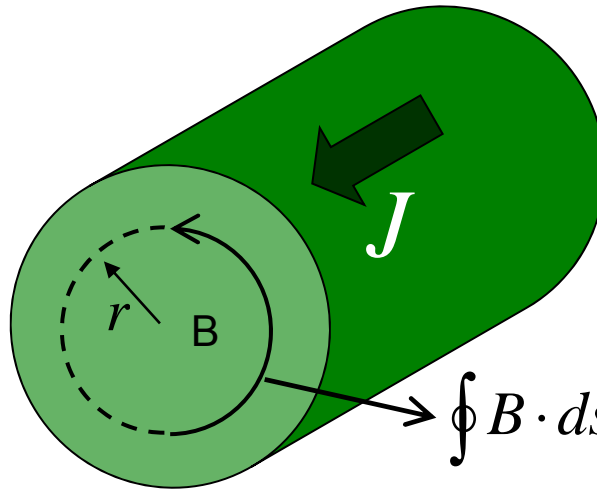
# Dipole field from 2 conductors

$J$  = uniform current density

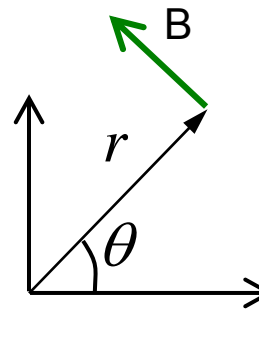
Ampere's law:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

current through the circle

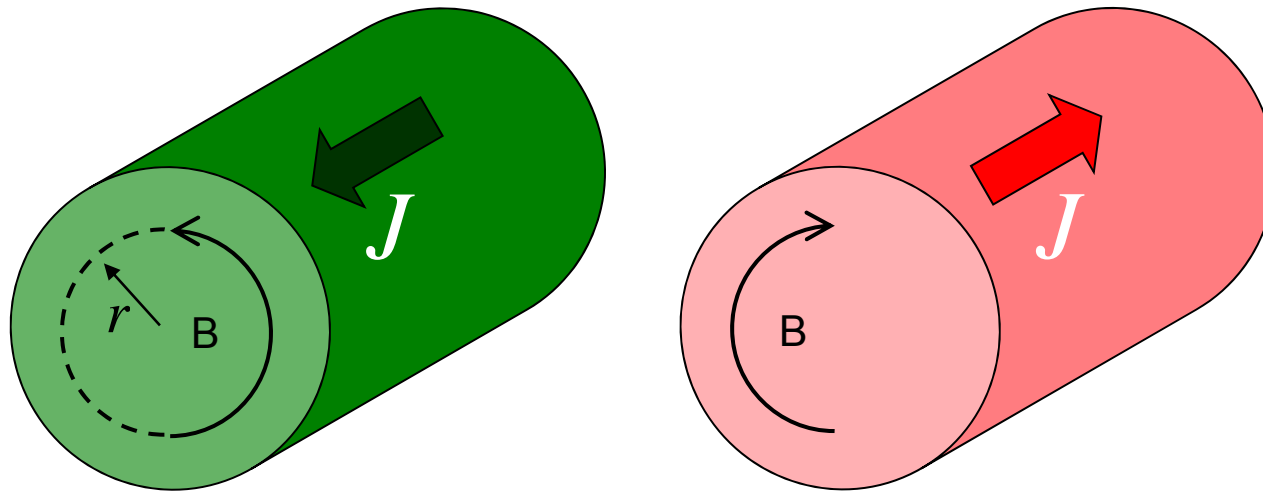


$$\oint B \cdot ds = 2\pi r B = \mu_0 \pi r^2 J \rightarrow B = \frac{\mu_0 J}{2} r$$


$$\left\{ \begin{array}{l} B_x = -\frac{\mu_0 J}{2} r \sin \theta \\ B_y = \frac{\mu_0 J}{2} r \cos \theta \end{array} \right.$$

# Dipole field from 2 conductors

$J$  = uniform current density

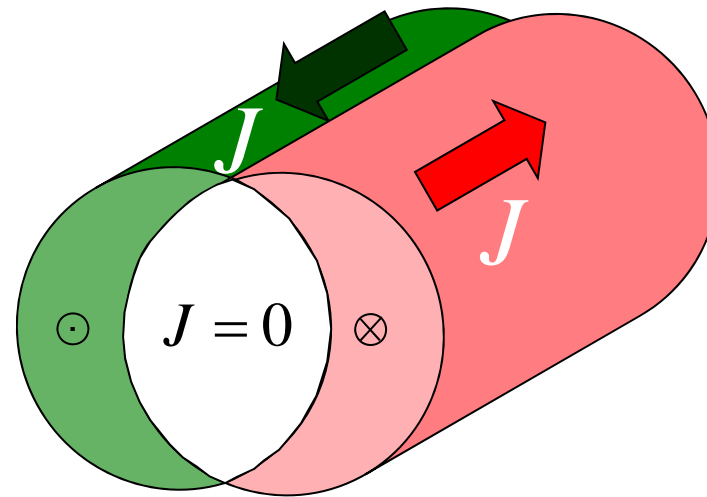




# Dipole field from 2 conductors

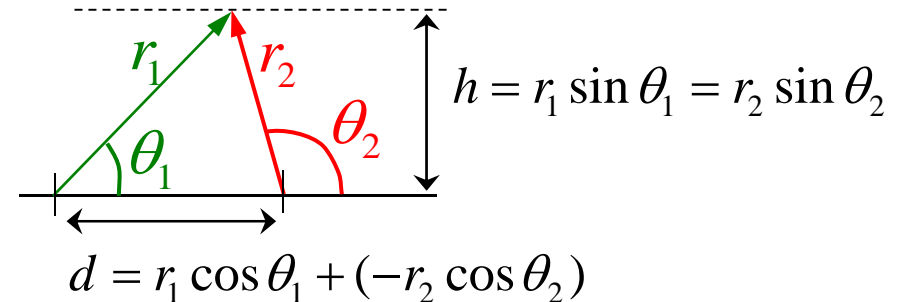
$J$  = uniform current density

$$B = \frac{\mu_0 J r}{2} \begin{cases} B_x = -\frac{\mu_0 J}{2} r \sin \theta \\ B_y = \frac{\mu_0 J}{2} r \cos \theta \end{cases}$$



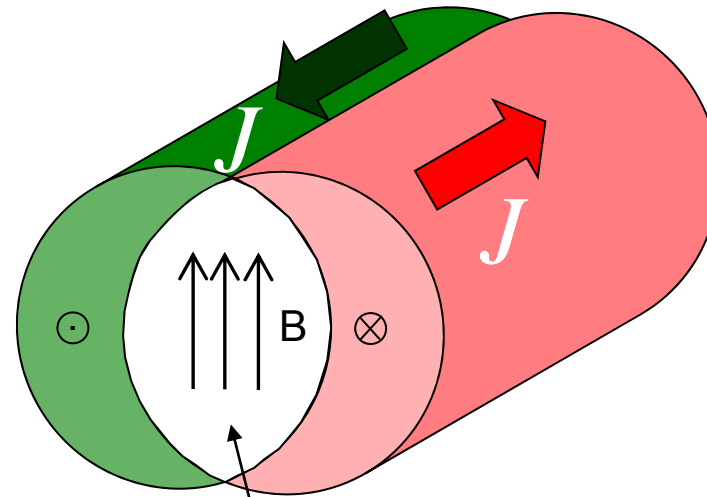
$$B_x = \frac{\mu_0 J}{2} (-r_1 \sin \theta_1 + r_2 \sin \theta_2) = 0$$

$$B_y = \frac{\mu_0 J}{2} (r_1 \cos \theta_1 - r_2 \cos \theta_2) = \frac{\mu_0 J}{2} d$$



# Dipole field from 2 conductors

$J$  = uniform current density

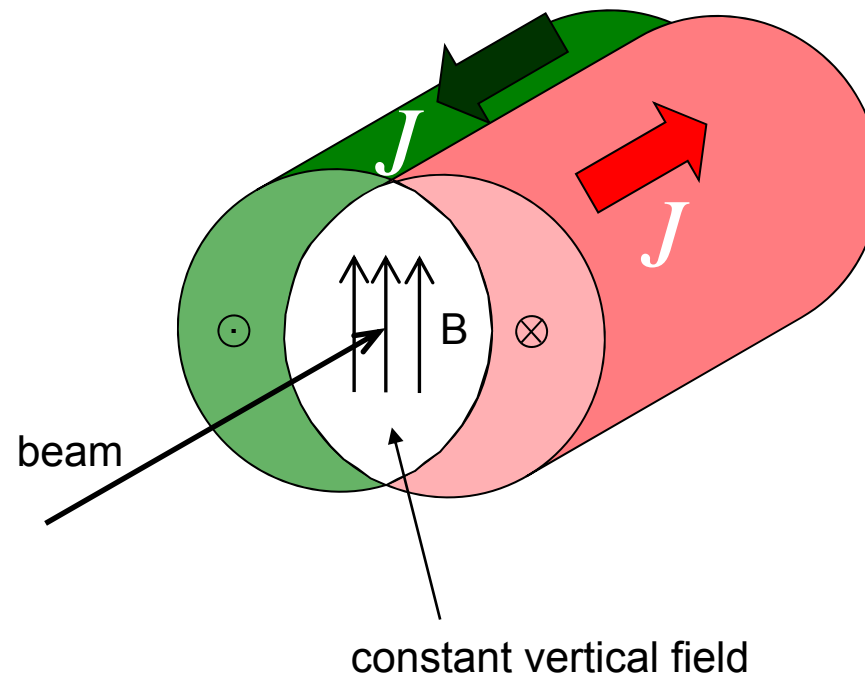


$$B_x = \frac{\mu_0 J}{2} (r_1 \sin \theta_1 - r_2 \sin \theta_2) = 0$$

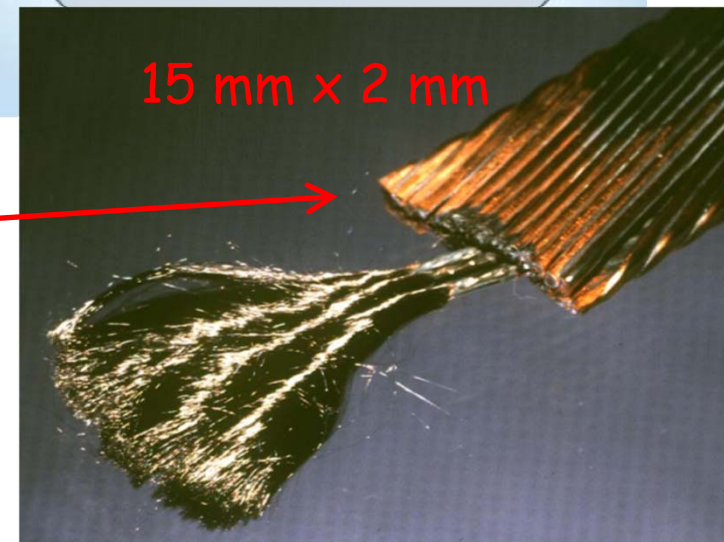
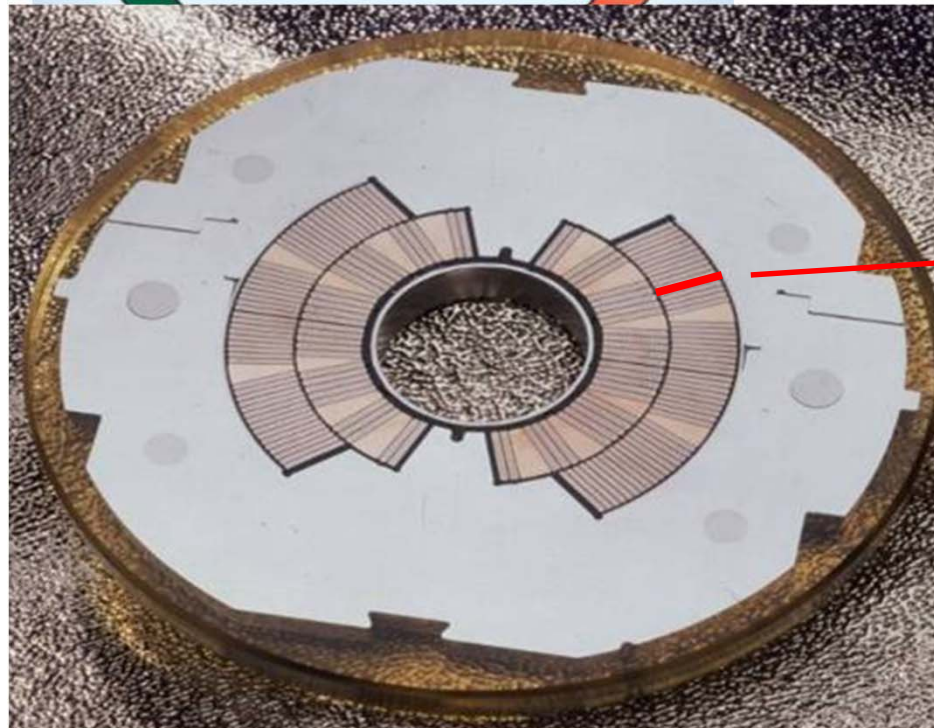
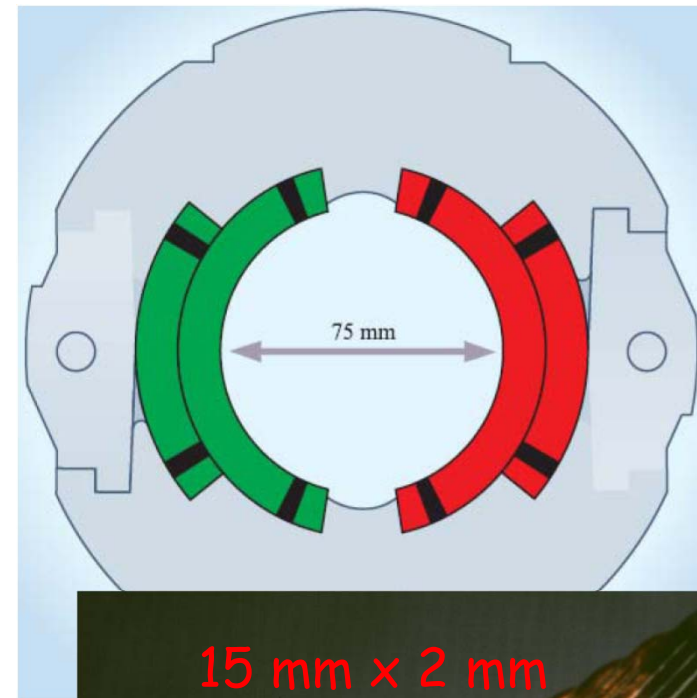
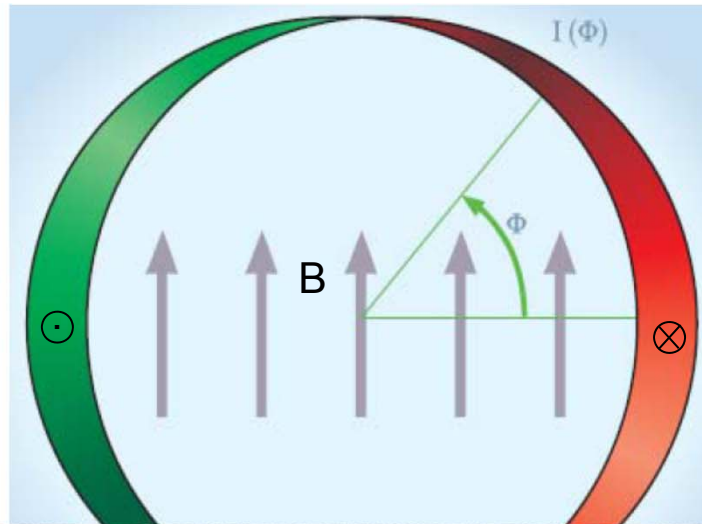
$$B_y = \frac{\mu_0 J}{2} (r_1 \cos \theta_1 - r_2 \cos \theta_2) = \frac{\mu_0 J}{2} d$$

constant vertical field

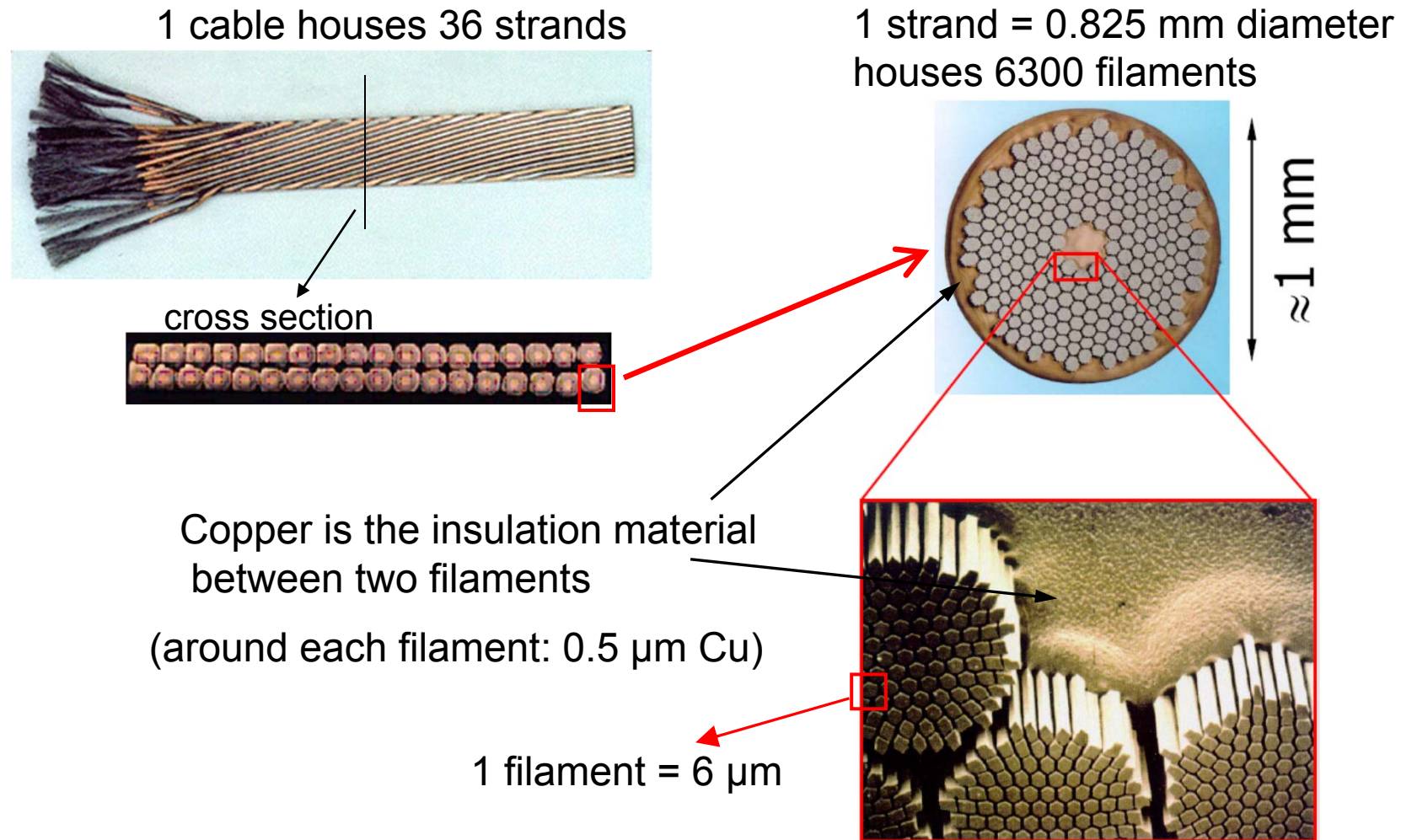
# Dipole field from 2 conductors



# From the principle to the reality...

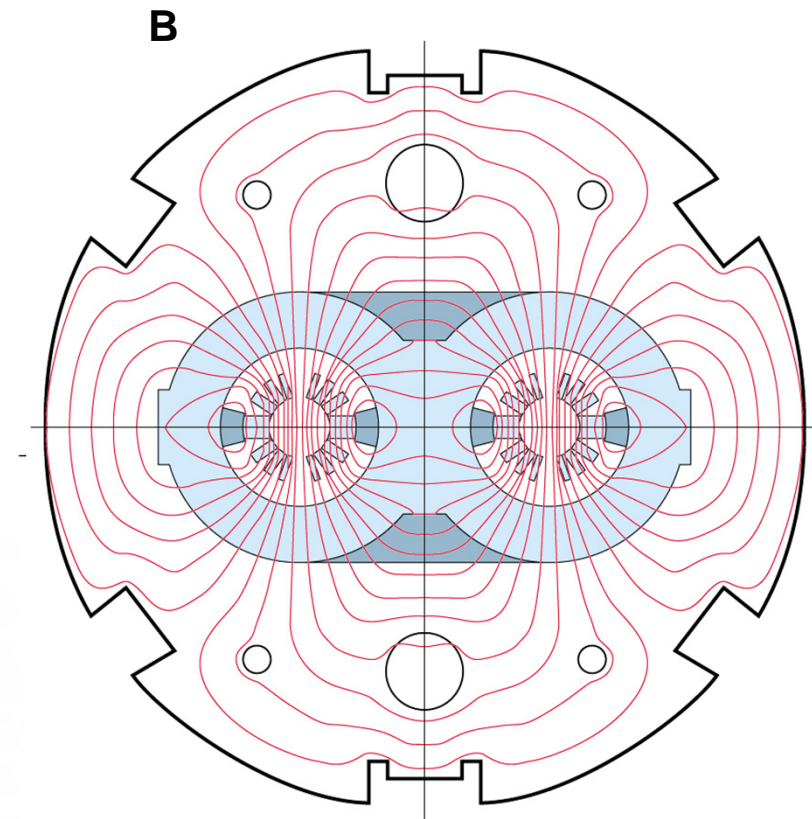
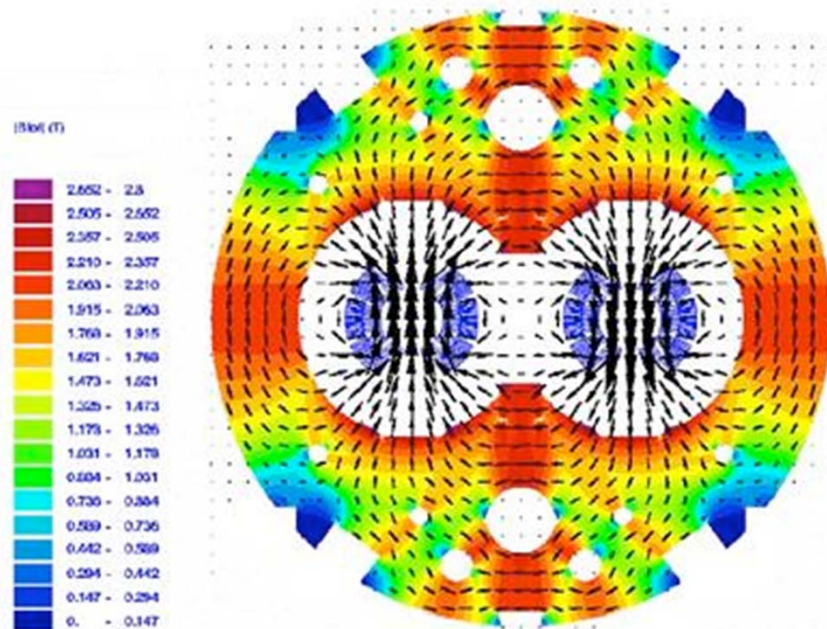
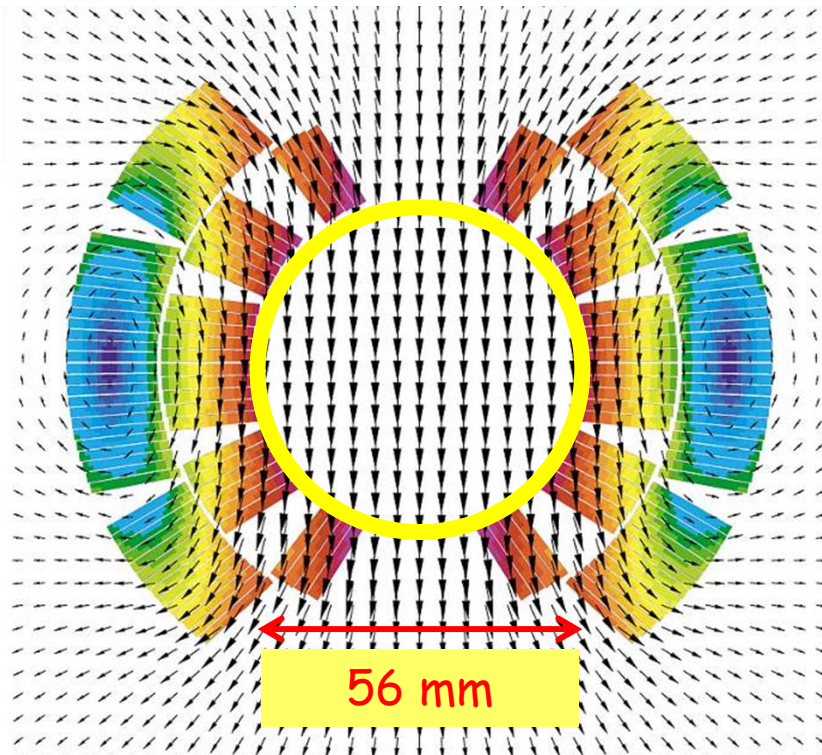


# LHC cables



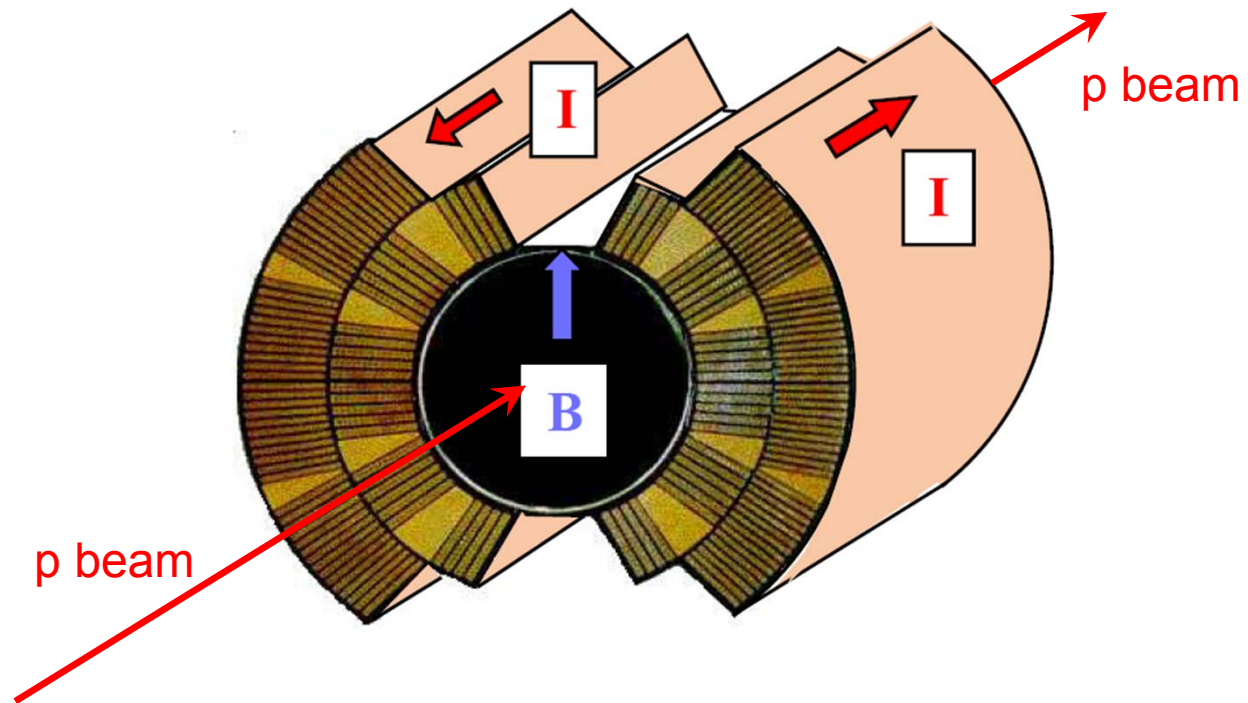


# Computed magnetic field



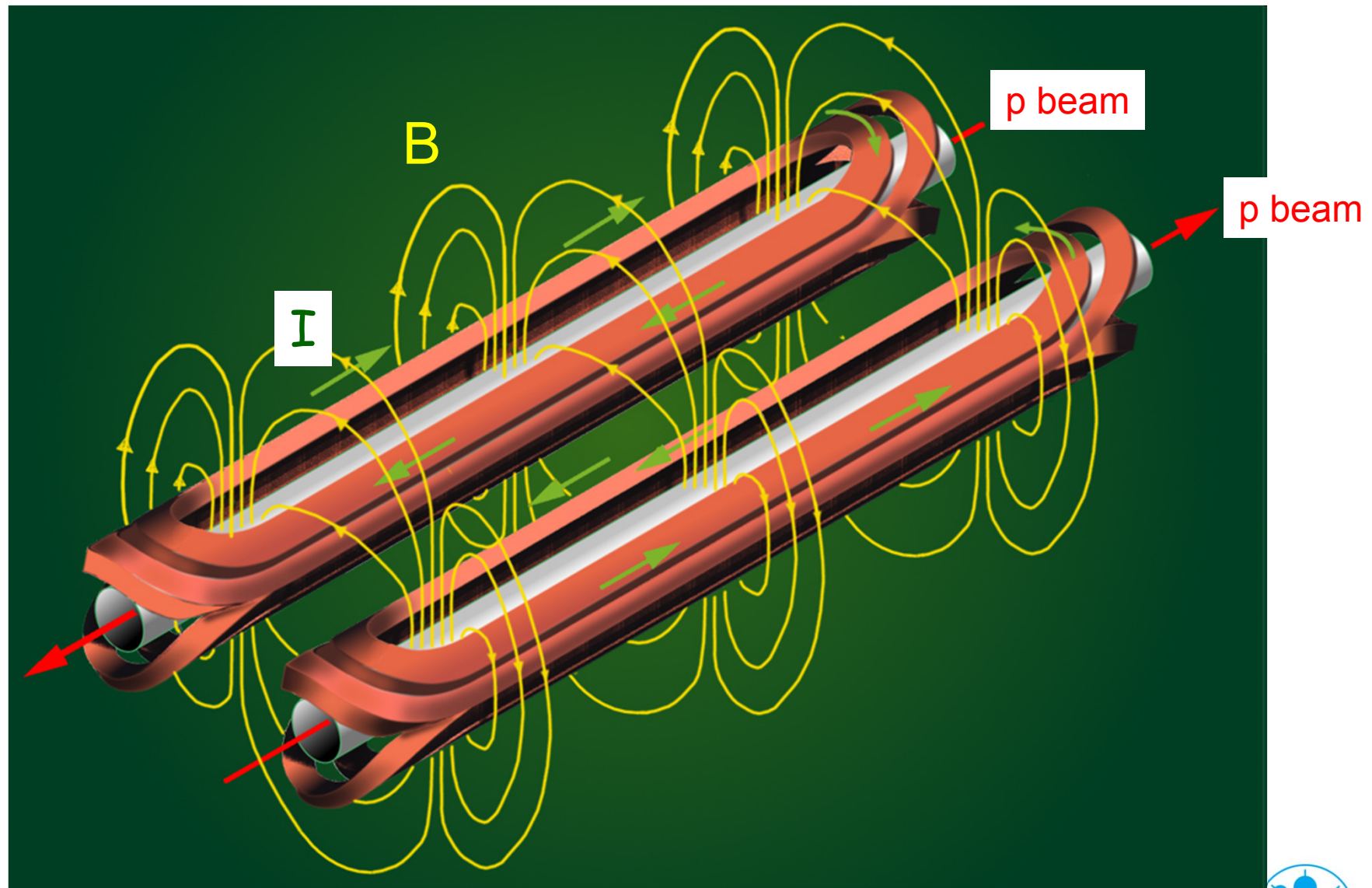
Computed magnetic flux map

# LHC dipole coils in 3D

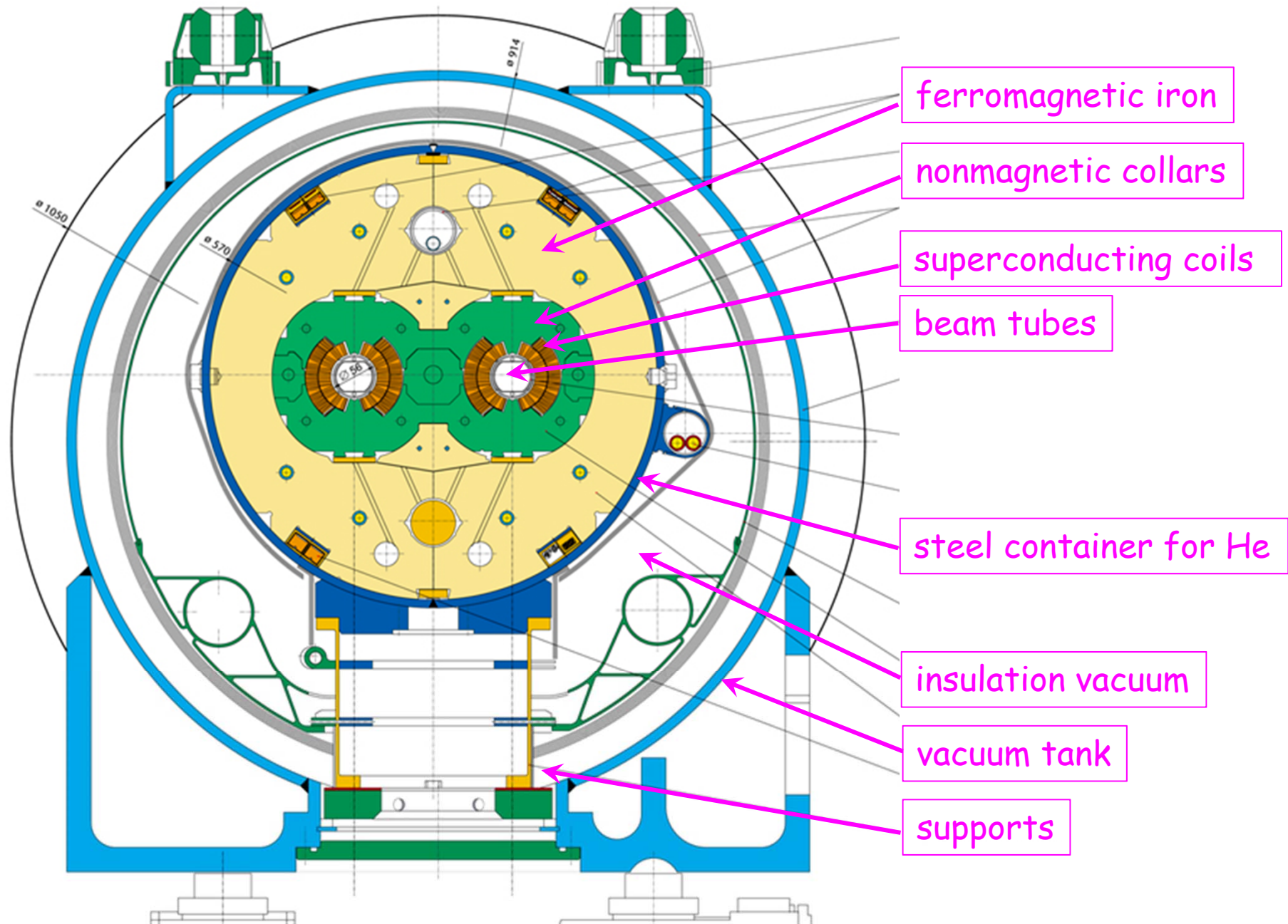




# LHC dipole coils in 3D

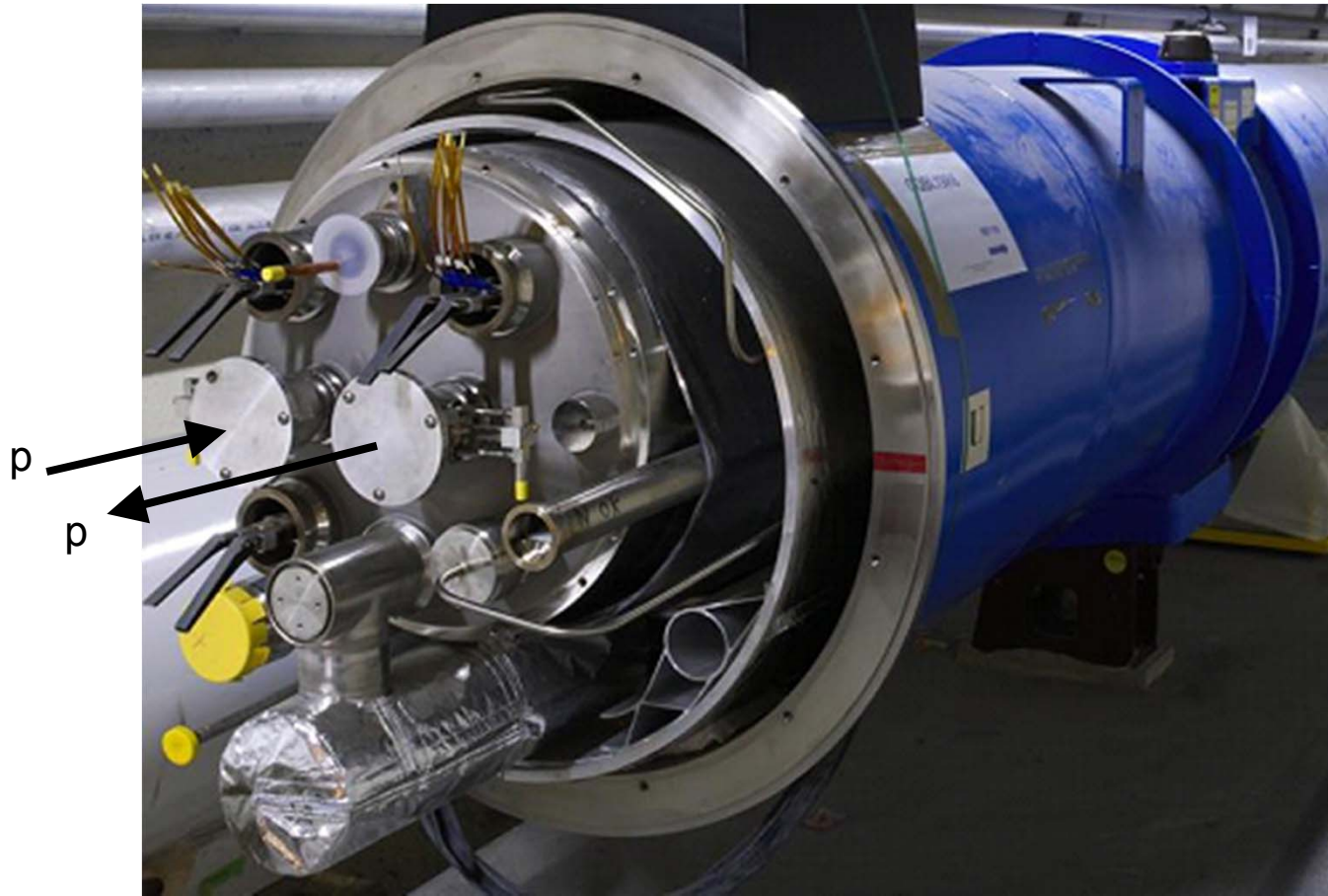


# LHC DIPOLE : STANDARD CROSS-SECTION



# Superconducting dipole magnets

LHC dipole magnet interconnection:





## Second summing-up

Linear accelerators:

- Alvarez drift-tube structure

Circular accelerators:

- Cyclotron, E. Lawrence
- Synchrotron

Dipole magnets: {  
normal conducting dipoles  
superconducting dipoles

