

Theory at LHC

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DESY summer student program, August 03, 2009, Zeuthen

Theory at LHC

- Introduction to QCD and Electroweak Physics *Monday, August 03, 2009*
- Higgs Physics, Supersymmetry and beyond *Tuesday, August 04, 2009*

Lecture 1

- The big questions
- Basics of perturbative QCD
- QCD factorization for hard scattering
- Parton luminosity
- Jet cross sections at hadron colliders
- $W^\pm$ and Z -boson production at LHC
- Hadro-production of Top-Quarks

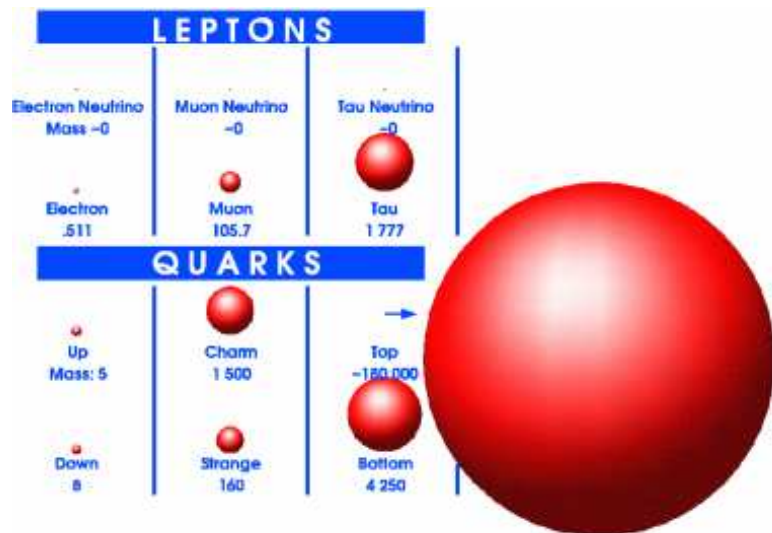
Things we do know

- Elementary particles
 - fermions (leptons, quarks)
(constituents of matter)
 - bosons
(carrier particles of forces)

Elementary Particles						
Quarks	u up	c charm	t top	g gluon	Force Carriers	
	d down	s strange	b bottom	γ photon		
Leptons	ν_e e neutrino	ν_μ μ neutrino	ν_τ τ neutrino	W W boson		
	e electron	μ muon	τ tau	Z Z boson		
3 $\rightarrow$			I	II	III	$\leftarrow$ Generations

Things we do know

- Elementary particles
 - fermions (leptons, quarks)
(constituents of matter)
 - bosons
(carrier particles of forces)
- Masses of fermions



Elementary Particles						
Quarks	<i>u</i> up	<i>c</i> charm	<i>t</i> top	<i>g</i> gluon	Force Carriers	
	<i>d</i> down	<i>s</i> strange	<i>b</i> bottom	γ photon		
Leptons	ν_e <i>e</i> neutrino	ν_μ μ neutrino	ν_τ τ neutrino	<i>W</i> <i>W</i> boson		
	<i>e</i> electron	μ muon	τ tau	<i>Z</i> <i>Z</i> boson		
3 → I II III ← Generations						

massive neutrinos first glimpse
beyond SM



The Nobel Prize in Physics 2008

"for the discovery of the mechanism of spontaneous broken symmetry in subatomic physics"

"for the discovery of the origin of the broken symmetry which predicts the existence of at least three families of quarks in nature"



Photo: SCANPIX

Yoichiro Nambu

🏆 1/2 of the prize

USA

Enrico Fermi Institute,
University of Chicago
Chicago, IL, USA

b. 1921



Photo: Kyodo/Reuters

Makoto Kobayashi

🏆 1/4 of the prize

Japan

High Energy Accelerator
Research Organization



Photo: Kyoto University

Toshihide Maskawa

🏆 1/4 of the prize

Japan

Kyoto University

b. 1940

Nobel prize 2008 for spontaneous symmetry breaking and CP violation

Titles, data and places given above refer to the time of the award.

Things we want to know

The Big Questions

- What is the origin of mass?
- What is 96% of the universe made of?
- Why is there no more antimatter?
- Do extra dimensions of space really exist?
- ...

Things we want to know

The Big Questions

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Highest energies at colliders until 201x

Energy frontier

- Search for Higgs boson, new massive particles at highest energies

$$E = m c^2$$

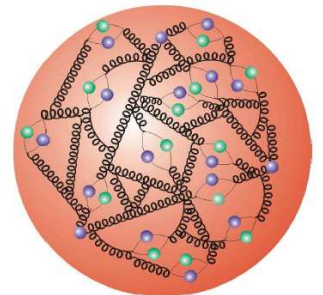
Hadron colliders

- Proton–(anti)-proton collisions reach TeV-scale
 - Tevatron $\sqrt{S} = 1.96\text{TeV}$ (until 2009), LHC with $\sqrt{S} = 14\text{TeV}$

- Proton: composite multi-particle bound state
 - collider: "wide-band beams" of quarks and gluons

- Protons are heavy

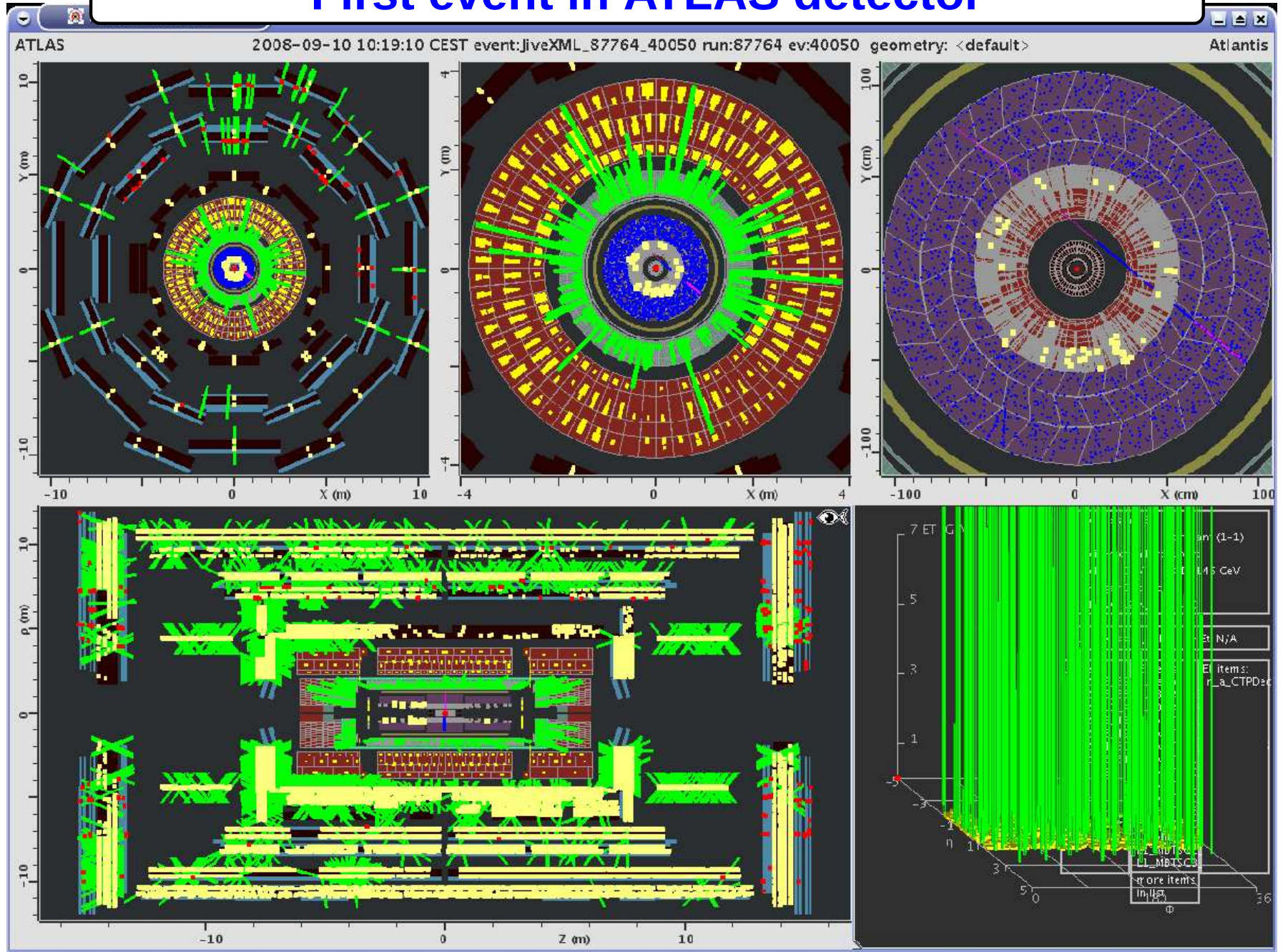
- no significant synchrotron radiation $\sim \left(\frac{E}{m}\right)^4 / r$



Large Hadron Collider



First event in ATLAS detector



Theoretical predictions for the LHC

Challenge

- Solve master equation

$$\text{new physics} = \text{data} - \text{Standard Model}$$

- New physics searches require understanding of SM background
- LHC explores the energy frontier
 - theory has to match or exceed accuracy of LHC data

Theoretical predictions for the LHC

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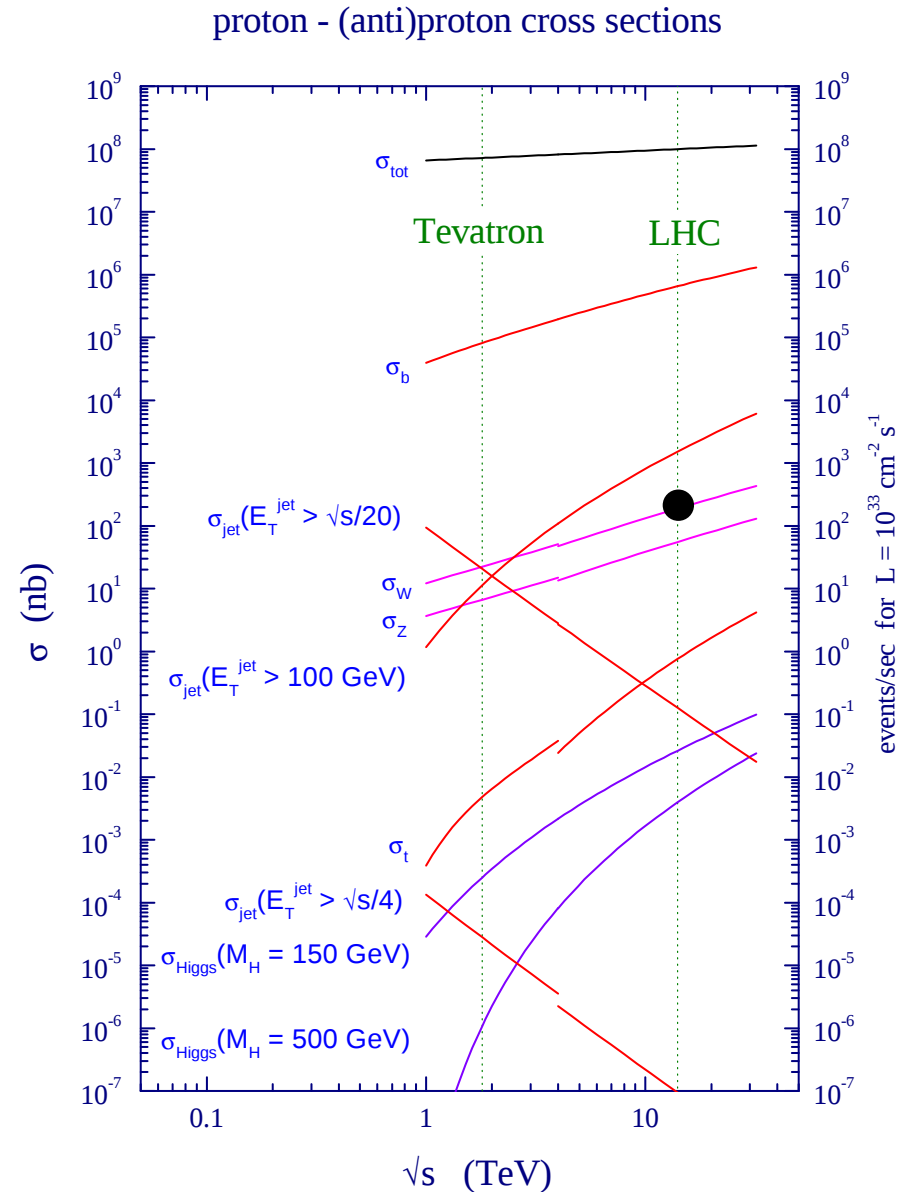
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Tools

- LHC is a QCD machine
 - perturbative QCD is essential and established part of toolkit (we no longer “test” QCD)
- Electroweak corrections important for precision predictions

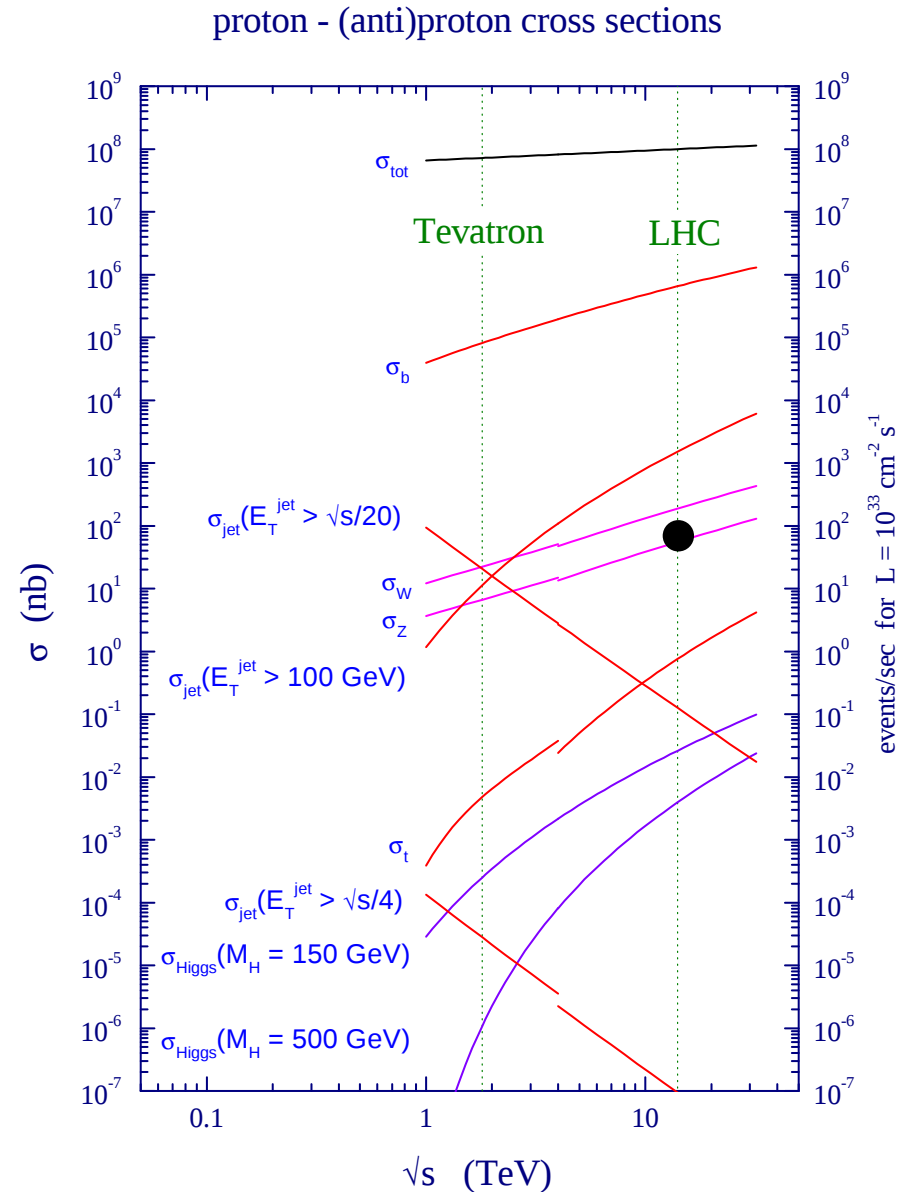
Proton-proton scattering

- Large rates expected for many Standard Model processes
- $\sigma_W \sim 150 \text{ nb}$
 - $BR(W \rightarrow e + \mu) \sim 20\%$
 10 fb^{-1} gives 300M leptonic events
 $\text{rate}(10^{33} \text{ cm}^{-2} \text{ s}^{-1}) \sim 30 \text{ Hz}$
 $\text{rate}(10^{34} \text{ cm}^{-2} \text{ s}^{-1}) \sim 300 \text{ Hz}$



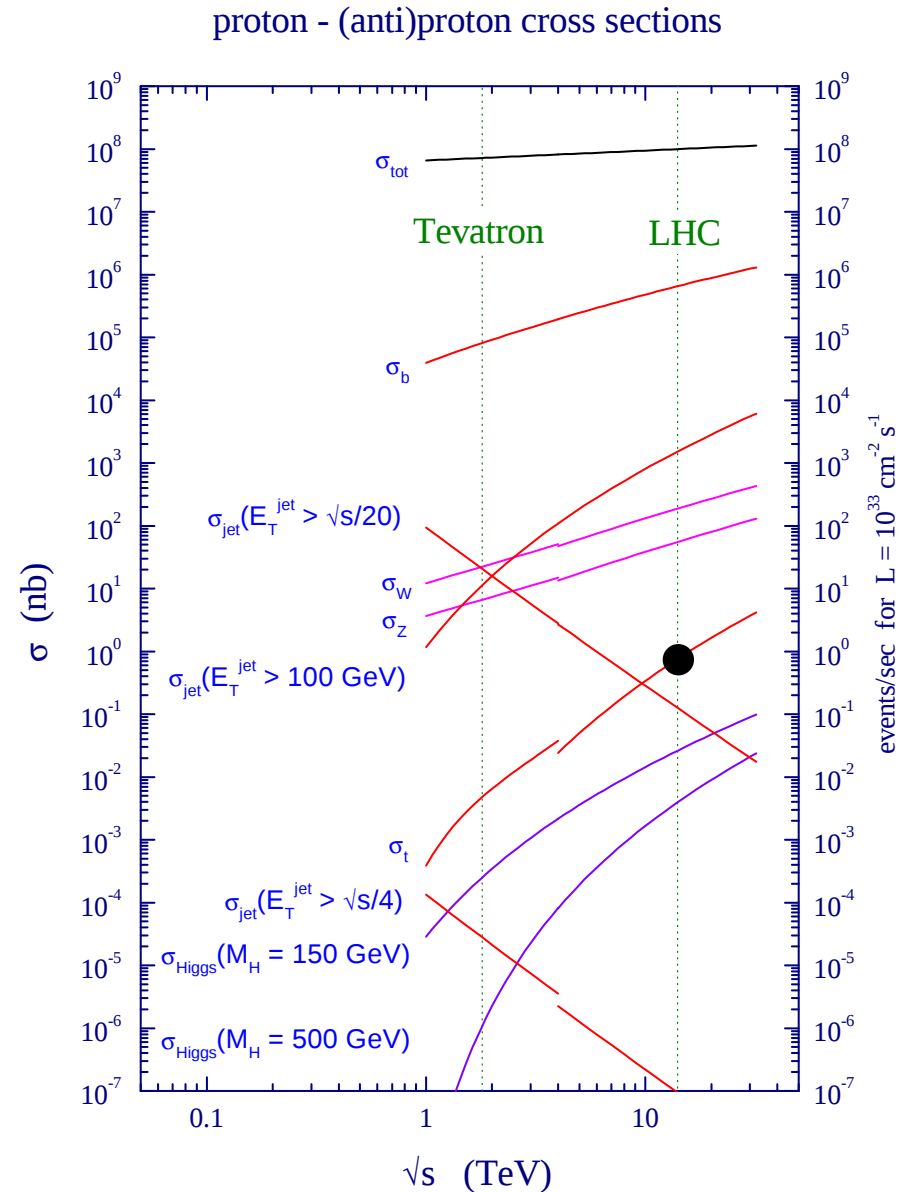
Proton-proton scattering

- Large rates expected for many Standard Model processes
- $\sigma_Z \sim 50 \text{ nb}$
 - $BR(W \rightarrow ee + \mu\mu) \sim 6.6\%$
 10 fb^{-1} gives 33M leptonic events
 $\text{rate}(10^{33} \text{ cm}^{-2} \text{ s}^{-1}) \sim 3.5 \text{ Hz}$
 $\text{rate}(10^{34} \text{ cm}^{-2} \text{ s}^{-1}) \sim 35 \text{ Hz}$



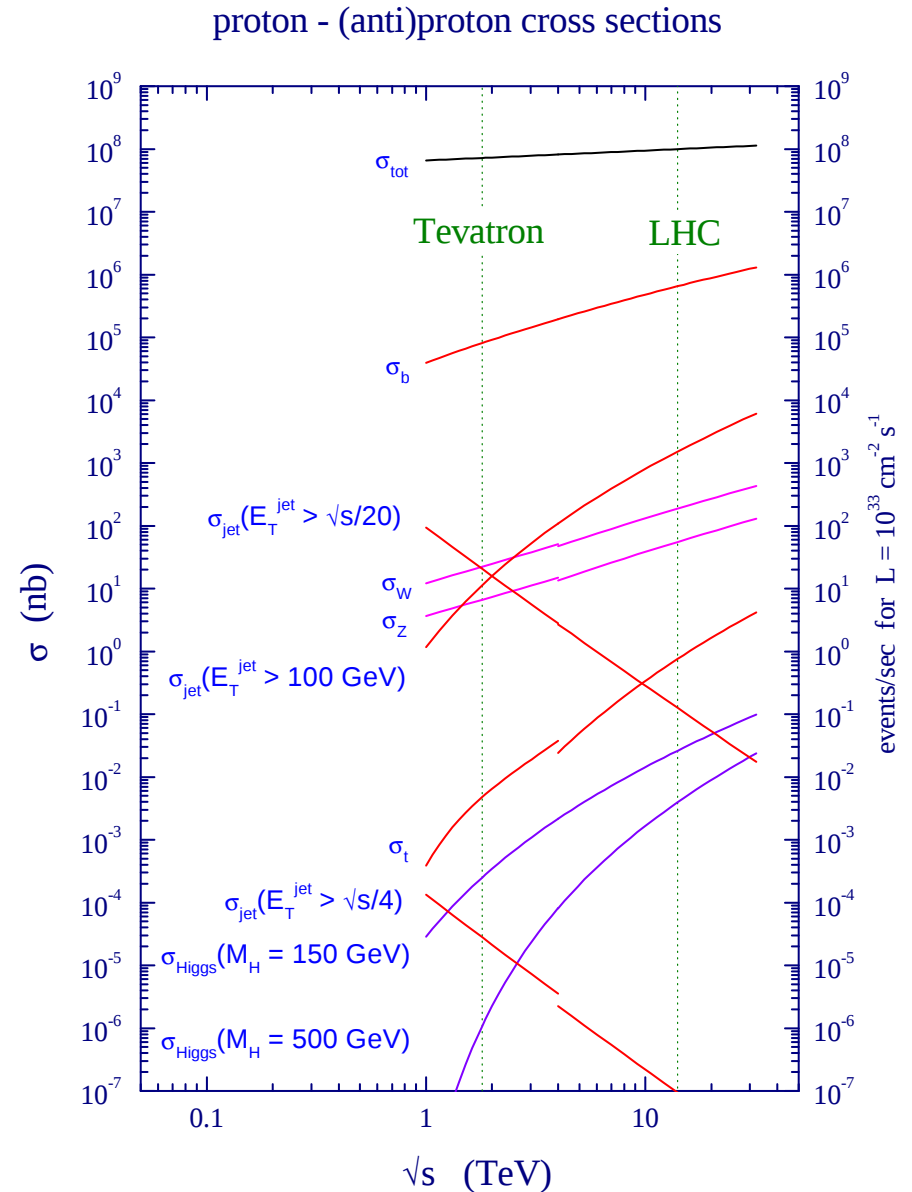
Proton-proton scattering

- Large rates expected for many Standard Model processes
- $\sigma_{t\bar{t}} \sim 800 \text{ pb}$
 - $BR(W \rightarrow e + \mu) \sim 30\%$
 10 fb^{-1} gives 2.4M leptonic events
 $\text{rate}(10^{33} \text{ cm}^{-2} \text{ s}^{-1}) \sim 0.2 \text{ Hz}$
 $\text{rate}(10^{34} \text{ cm}^{-2} \text{ s}^{-1}) \sim 2 \text{ Hz}$



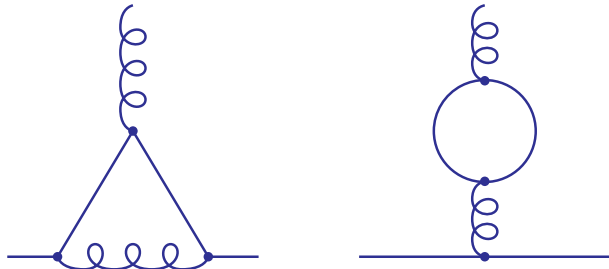
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- New physics signals
 - cross section predictions
 $\sigma_{\text{new physics}} \sim \mathcal{O}(1 - 10) \text{ pb}$
 - superpartners in MSSM
 (neutralinos, charginos, squarks, gluinos, ...), KK modes
 - searches often assume 100 fb^{-1}

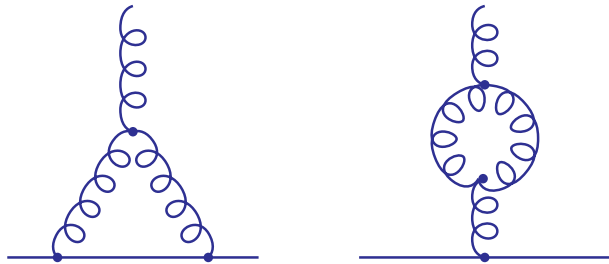


Asymptotic freedom in QCD

- Effective coupling constant α_s depends on resolution, momentum scale Q

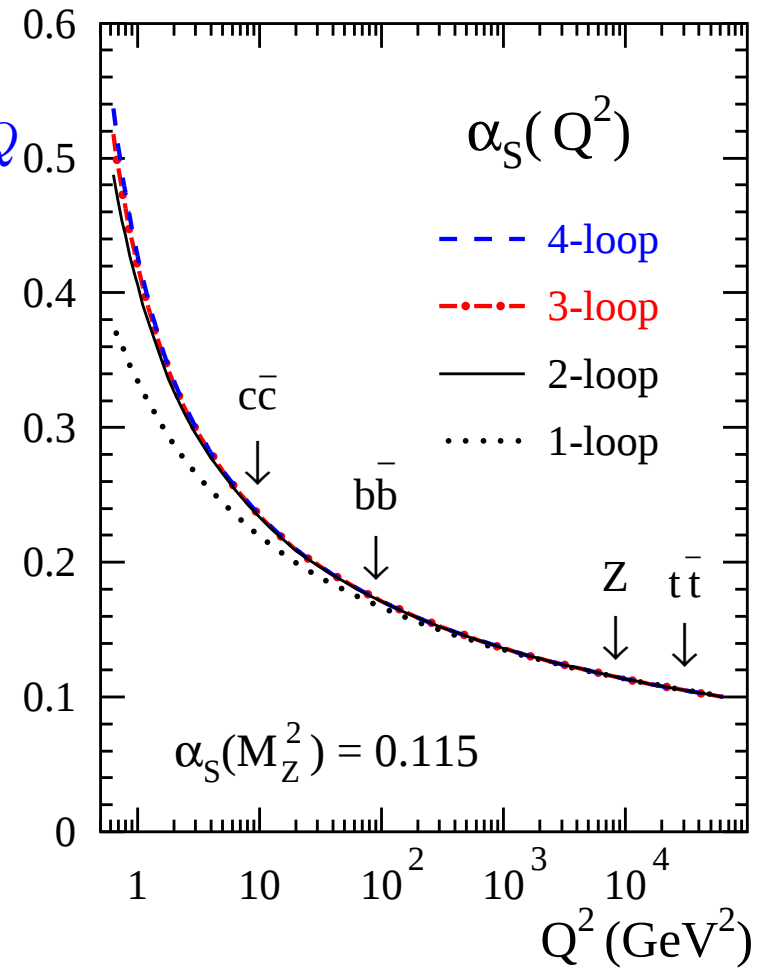


– screening (like in QED)



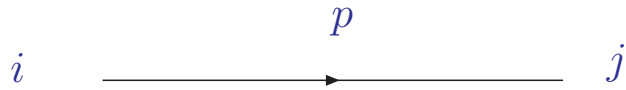
– anti-screening (color charge of g)

- At large scales: application of perturbation theory (but $\alpha_s \gg \alpha_{\text{QED}}$)

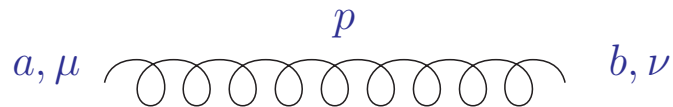


Feynman rules

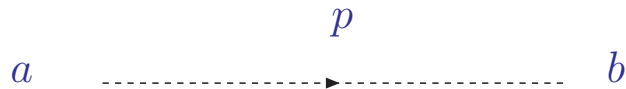
- Propagators
 - fermions, gluons, ghosts
 - covariant gauge



$$\delta^{ij} \frac{i}{\not{p} - m}$$



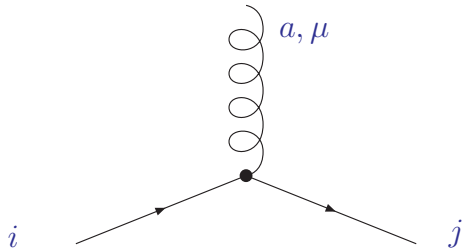
$$\delta^{ab} i \left(\frac{-g^{\mu\nu}}{p^2} + (1 - \lambda) \frac{p^\mu p^\nu}{(p^2)^2} \right)$$



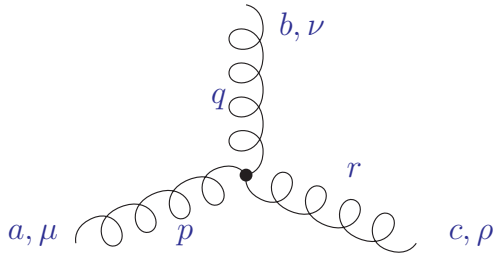
$$\delta^{ab} \frac{i}{p^2}$$

Feynman rules (cont'd)

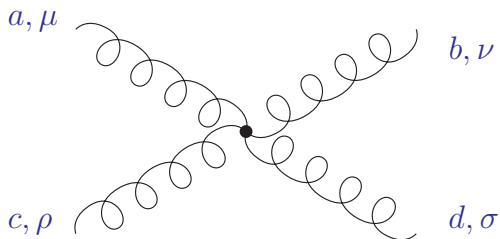
Vertices



$$-i g (t^a)_{ji} \gamma^\mu$$



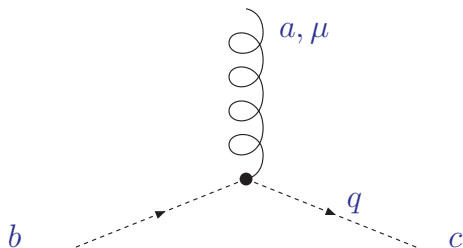
$$-g f^{abc} ((p - q)^\rho g^{\mu\nu} + (q - r)^\mu g^{\nu\rho} + (r - p)^\nu g^{\mu\rho})$$



$$-i g^2 f^{xac} f^{xbd} (g^{\mu\nu} g^{\rho\sigma} - g^{\mu\sigma} g^{\nu\rho})$$

$$-i g^2 f^{xad} f^{xbc} (g^{\mu\nu} g^{\rho\sigma} - g^{\mu\rho} g^{\nu\sigma})$$

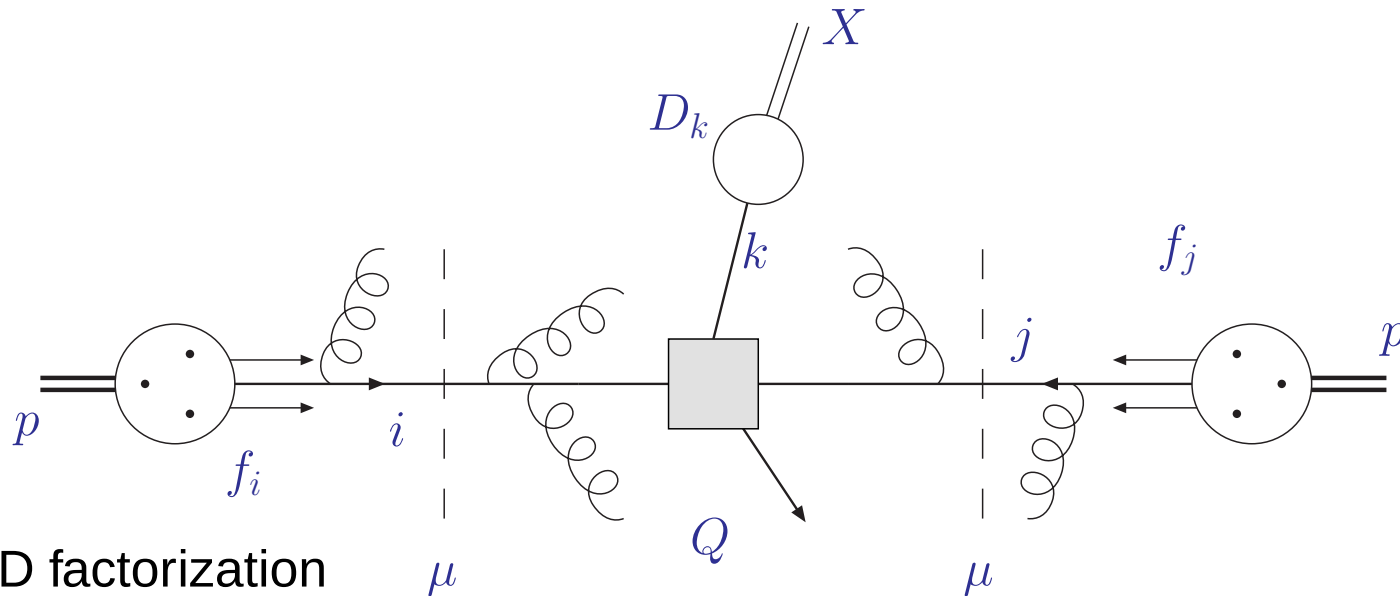
$$-i g^2 f^{xab} f^{xcd} (g^{\mu\rho} g^{\nu\sigma} - g^{\mu\sigma} g^{\nu\rho})$$



$$g f^{abc} q^\mu$$

Perturbative QCD at colliders

- Hard hadron-hadron scattering
 - constituent partons from each incoming hadron interact at short



- QCD factorization
 - separate sensitivity to dynamics from different scales

$$\sigma_{pp \rightarrow X} = \sum_{ijk} f_i(\mu^2) \otimes f_j(\mu^2) \otimes \hat{\sigma}_{ij \rightarrow k}(\alpha_s(\mu^2), Q^2, \mu^2) \otimes D_{k \rightarrow X}(\mu^2)$$

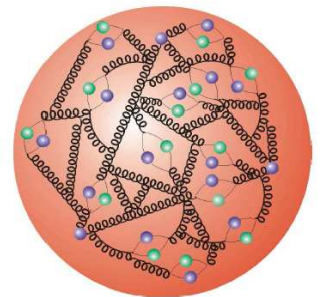
- factorization scale μ , subprocess cross section $\hat{\sigma}_{ij \rightarrow k}$ for parton types i, j and hadronic final state X

Hard scattering cross section

- Standard approach to uncertainties in theoretical predictions
 - variation of factorization scale μ : $\frac{d}{d \ln \mu^2} \sigma_{pp \rightarrow X} = \mathcal{O}(\alpha_s^{l+1})$

$$\sigma_{pp \rightarrow X} = \sum_{ijk} f_i(\mu^2) \otimes f_j(\mu^2) \otimes \hat{\sigma}_{ij \rightarrow k}(\alpha_s(\mu^2), Q^2, \mu^2) \otimes D_{k \rightarrow X}(\mu^2)$$

- Parton cross section $\hat{\sigma}_{ij \rightarrow k}$ calculable perturbatively in powers of α_s
 - constituent partons from incoming protons interact at short distances of order $\mathcal{O}(1/Q)$
- Parton luminosity $f_i \otimes f_j$
 - proton: very complicated multi-particle bound state
 - colliders: wide-band beams of quarks and gluons
- Final state X : hadrons, mesons, jets, ...
 - fragmentation function $D_{k \rightarrow X}(\mu^2)$ or jet algorithm
 - interface with showering algorithms (Monte Carlo)



Approaches to the calculation of σ_{had}

- LO (leading order)
 - Automated tree level calculations in Standard Model, MSSM, ... (Madgraph, Sherpa, Alpgen, CompHEP, ...)
 - LO + parton shower
 - String inspired techniques
- NLO (next-to-leading order)
 - Analytical (or numerical) calculations of diagrams yield parton level Monte Carlos (NLOJET++, MCFM, ...)
 - NLO + parton shower (MC@NLO, VINCIA)
- NNLO (next-to-next-to-leading order)
 - selected results known (mostly inclusive kinematics)
- N³LO (next-to-next-to-next-to-leading order)
 - very few ...

Approaches to the calculation of σ_{had}

easy

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← level of talk here

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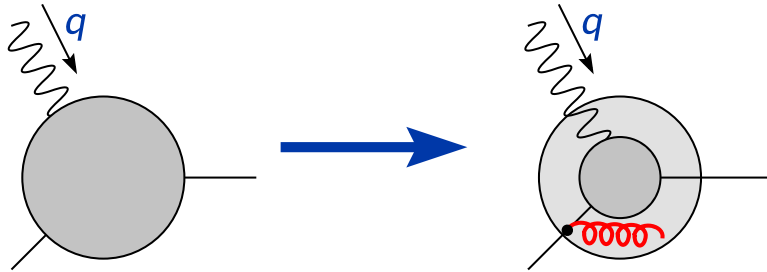
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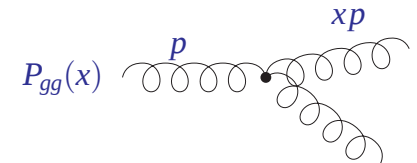
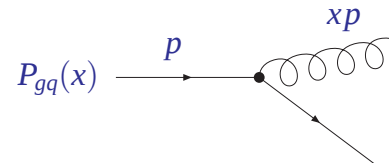
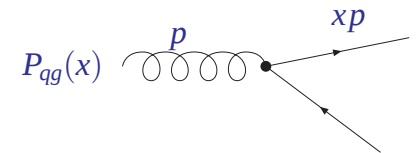
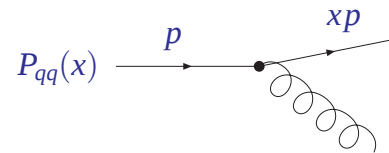
difficult

Parton luminosity

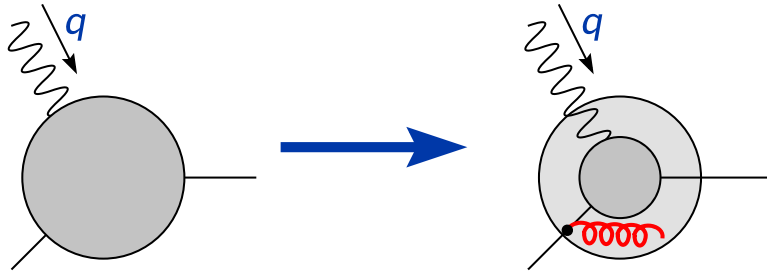


- Proton in resolution $1/Q \rightarrow$ sensitive to lower momentum partons

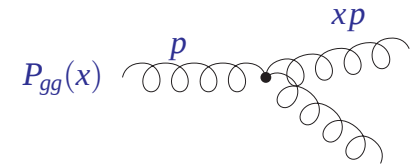
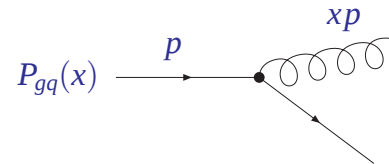
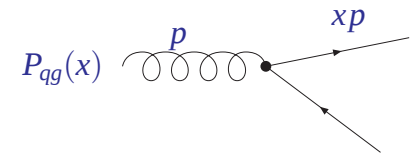
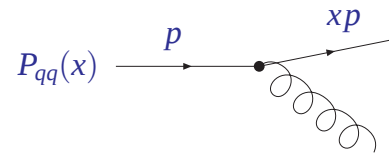
● Feynman diagrams in leading order



Parton luminosity



● Feynman diagrams in leading order



● Proton in resolution $1/Q \rightarrow$ sensitive to lower momentum partons

● Evolution equations for parton distributions f_i

● predictions from fits to reference processes (universality)

$$\frac{d}{d \ln \mu^2} f_i(x, \mu^2) = \sum_k \left[P_{ik}(\alpha_s(\mu^2)) \otimes f_k(\mu^2) \right] (x)$$

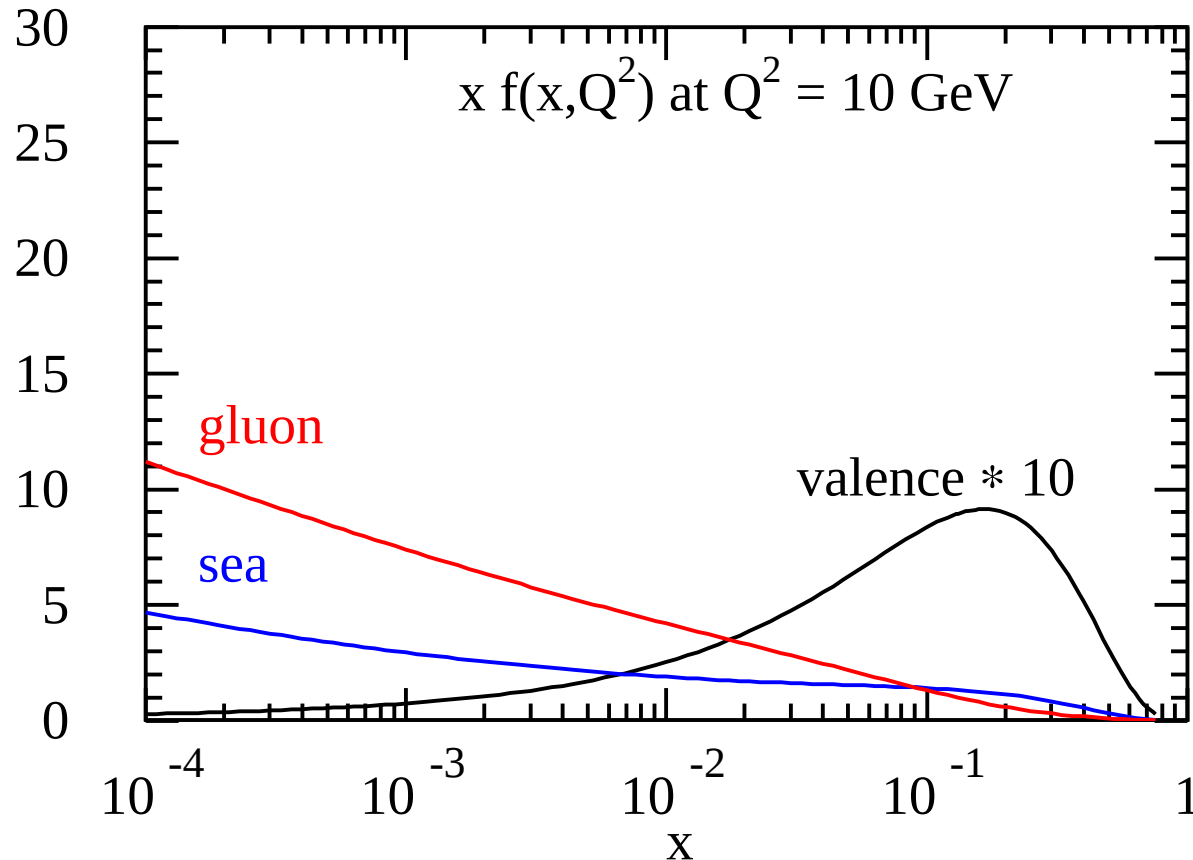
● Splitting functions P

$$P = \underbrace{\alpha_s P^{(0)} + \alpha_s^2 P^{(1)}} + \alpha_s^3 P^{(2)} + \dots$$

NLO: standard approximation (large uncertainties)

Parton distributions in proton

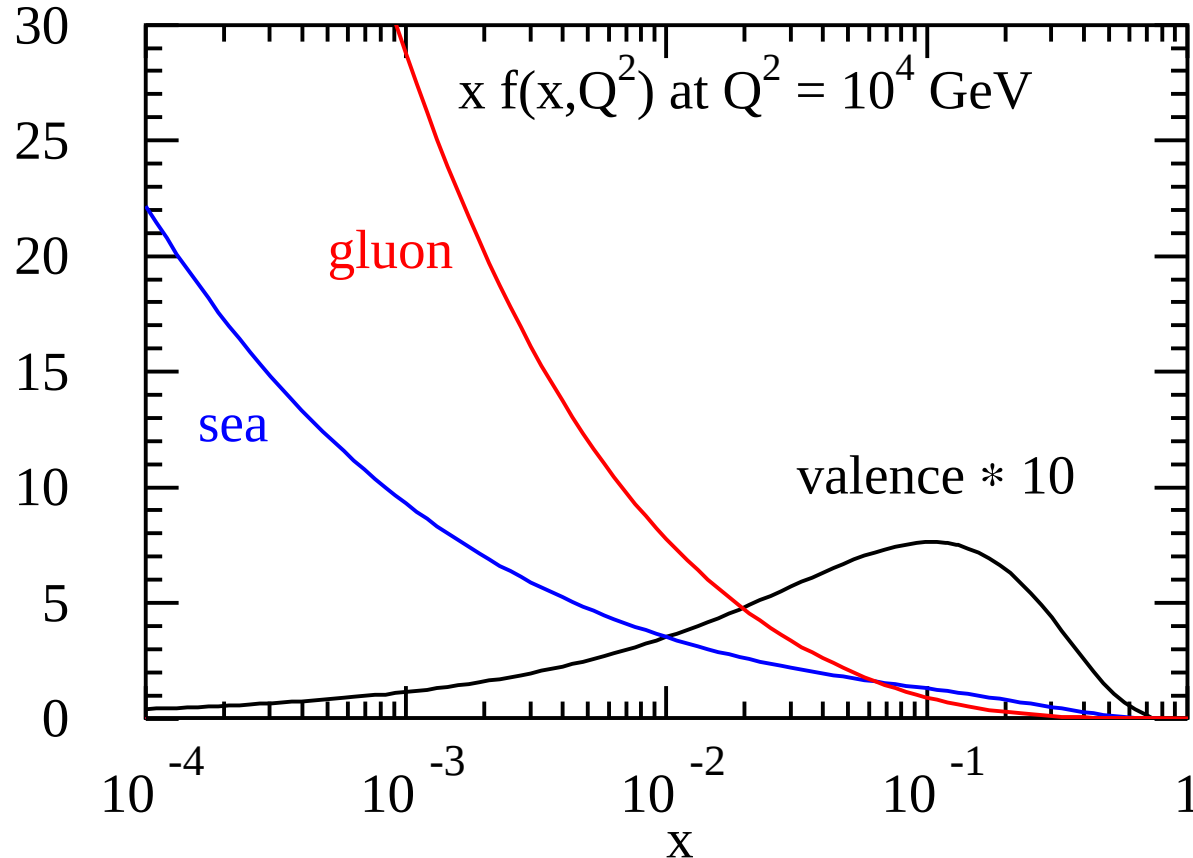
- Valence $q - \bar{q}$ (additive quantum numbers) sea (part with $q + \bar{q}$)



- Parameterization (bulk of data from deep-inelastic scattering)
 - structure function F_2 $\longrightarrow$ quark distribution
 - scale evolution (perturbative QCD) $\longrightarrow$ gluon distribution

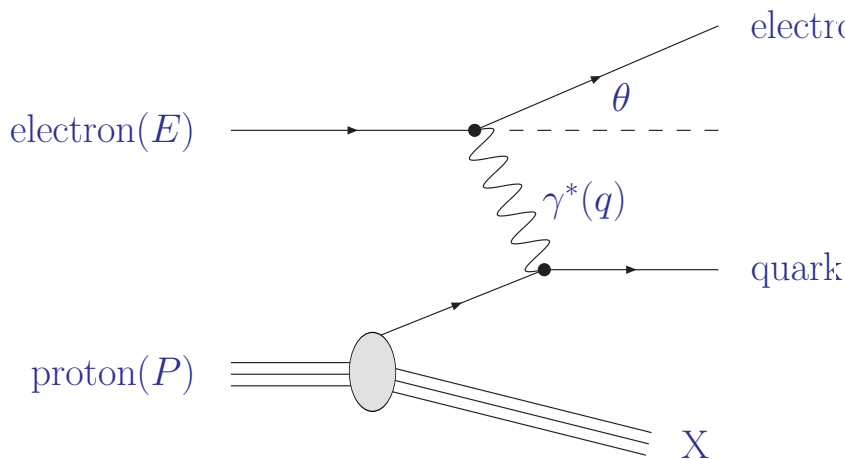
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Inelastic electron-proton scattering



- Virtuality of photon: resolution

$$Q^2 \equiv -q^2 = 4EE' \sin^2(\theta/2)$$

- Bjorken variable: inelasticity

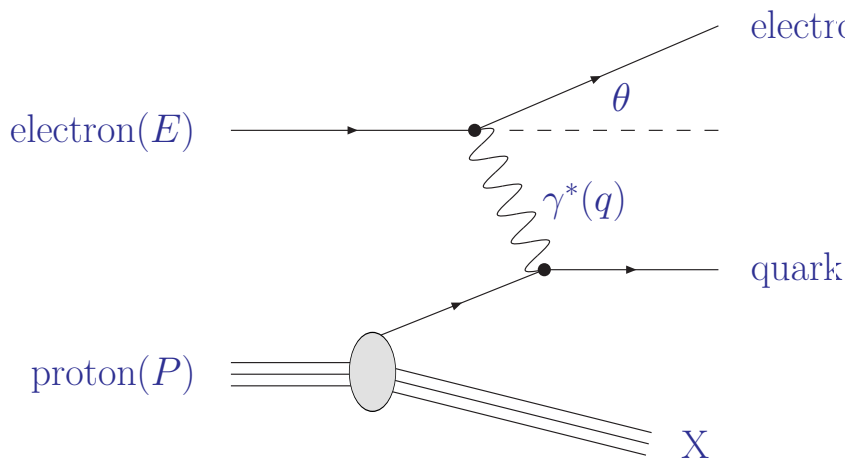
$$x = \frac{Q^2}{2P \cdot q} < 1$$

- Cross section (X inclusive): proton structure function F_i^p

$$(E - E') \frac{d\sigma}{d\Omega dE'} \stackrel{\text{lab}}{=} \underbrace{\frac{\alpha^2 \cos^2 \frac{\theta}{2}}{4E^2 \sin^4 \frac{\theta}{2}}}_{\text{Mott-scattering (point-like)}} \left\{ F_2^p(x, Q^2) + \tan^2 \frac{\theta}{2} F_1^p(x, Q^2) \right\}$$

Mott-scattering (point-like)

Inelastic electron-proton scattering



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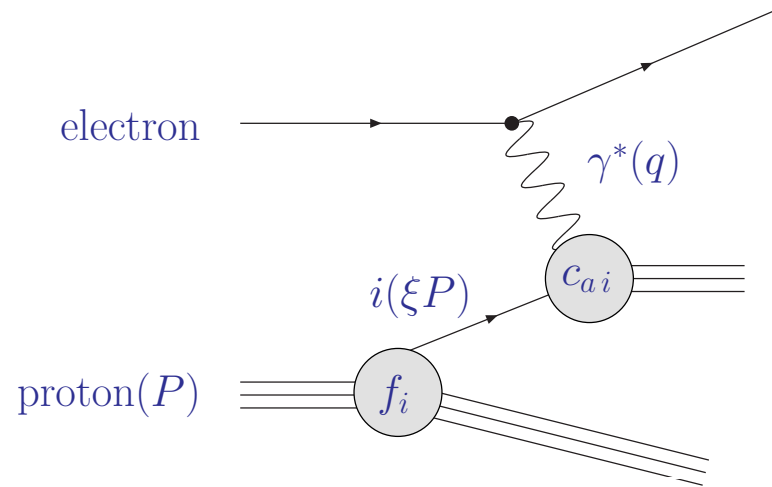
Mott-scattering (point-like)

- Deep-inelastic scattering (Bjorken limit: $Q^2 \rightarrow \infty$ and x fixed)
Parton model (quasi-free point-like constituents, incoherence)

$$F_2(x, Q^2) \simeq F_2(x) = \sum_i e_i^2 x f_i(x)$$

- $x f_i(x)$ distribution for momentum fraction x of parton i

QCD corrections in deep-inelastic scattering



- Structure function F_2 (up to terms $\mathcal{O}(1/Q^2)$)
 - Renormalization/factorization scale $\mu = \mathcal{O}(Q)$

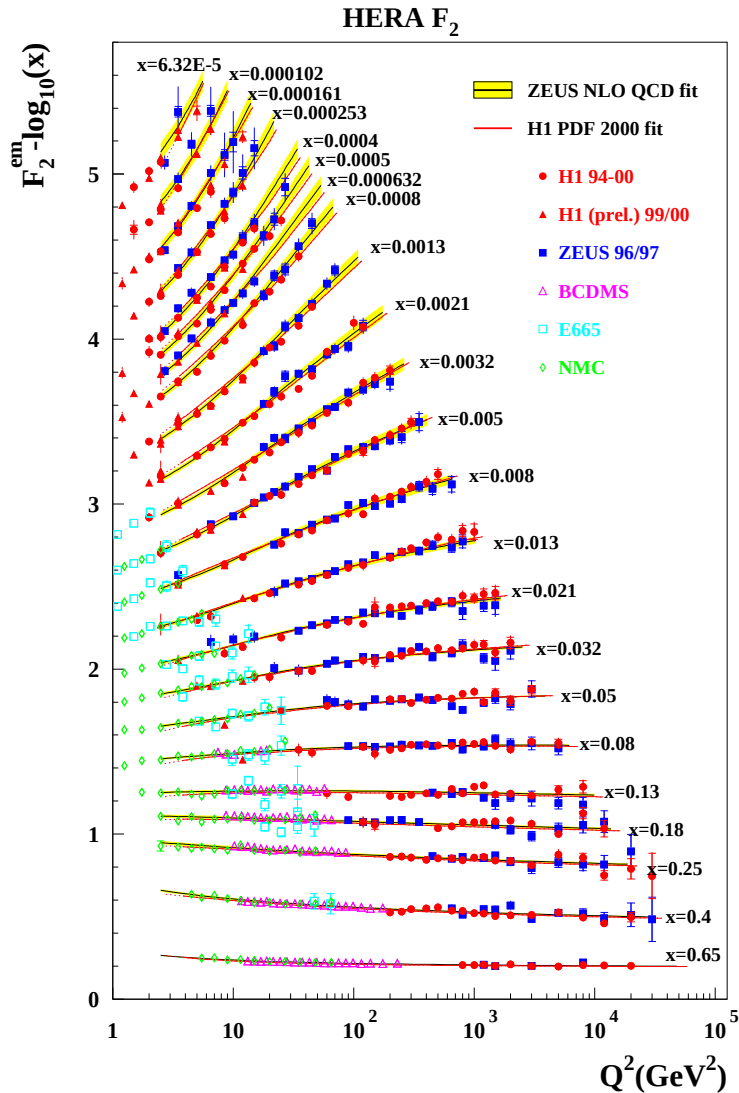
$$x^{-1} F_2^p(x, Q^2) = \sum_i \int_x^1 \frac{d\xi}{\xi} c_{2,i} \left(\frac{x}{\xi}, \alpha_s(\mu^2), \frac{\mu^2}{Q^2} \right) f_i^p(\xi, \mu^2)$$

- Coefficient functions c_a

$$c_a = \underbrace{\alpha_s^{n_a} \left[c_a^{(0)} + \alpha_s c_a^{(1)} \right]}_{\text{NLO: standard approximation (large uncertainties)}} + \alpha_s^2 c_a^{(2)} + \dots$$

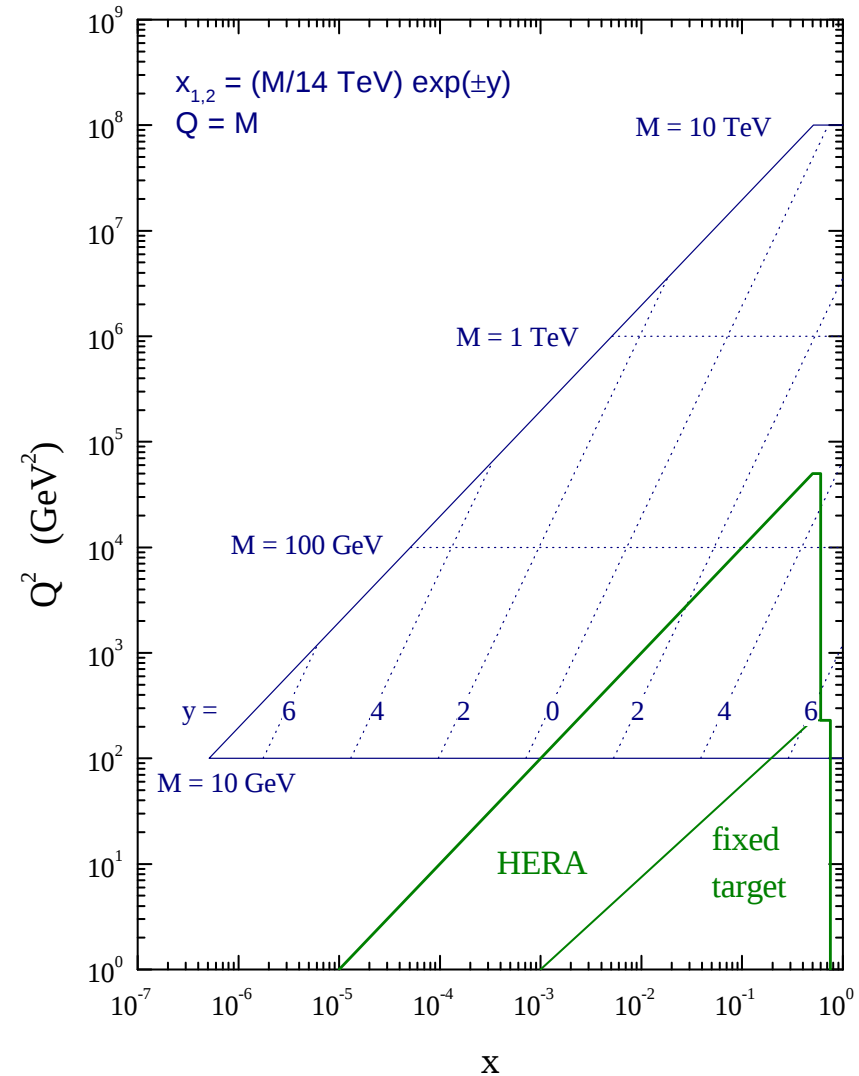
NLO: standard approximation (large uncertainties)

PDFs from HERA to LHC



● Precision HERA data on F_2

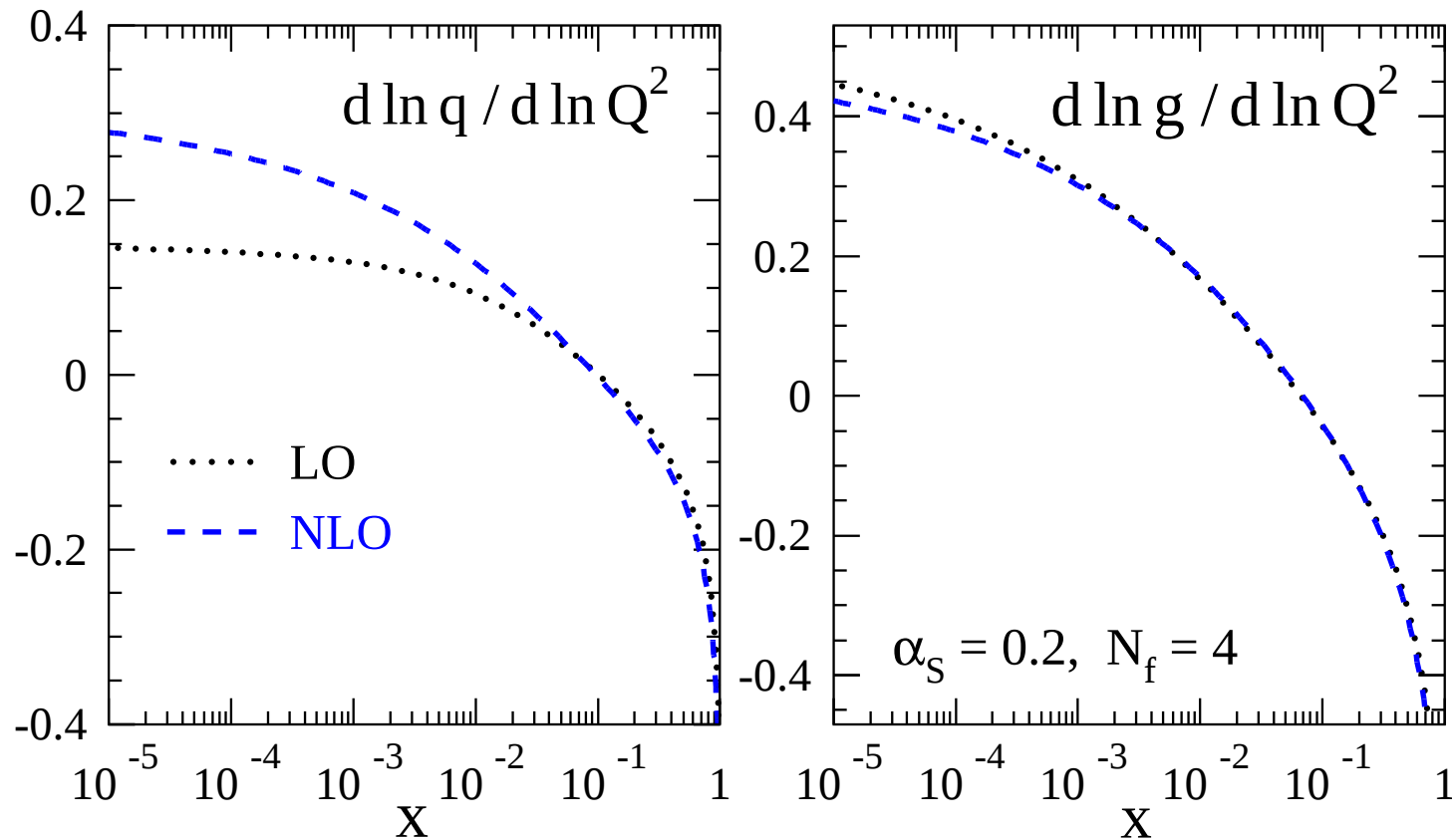
LHC parton kinematics



● Scale evolution of PDFs in Q over two to three orders

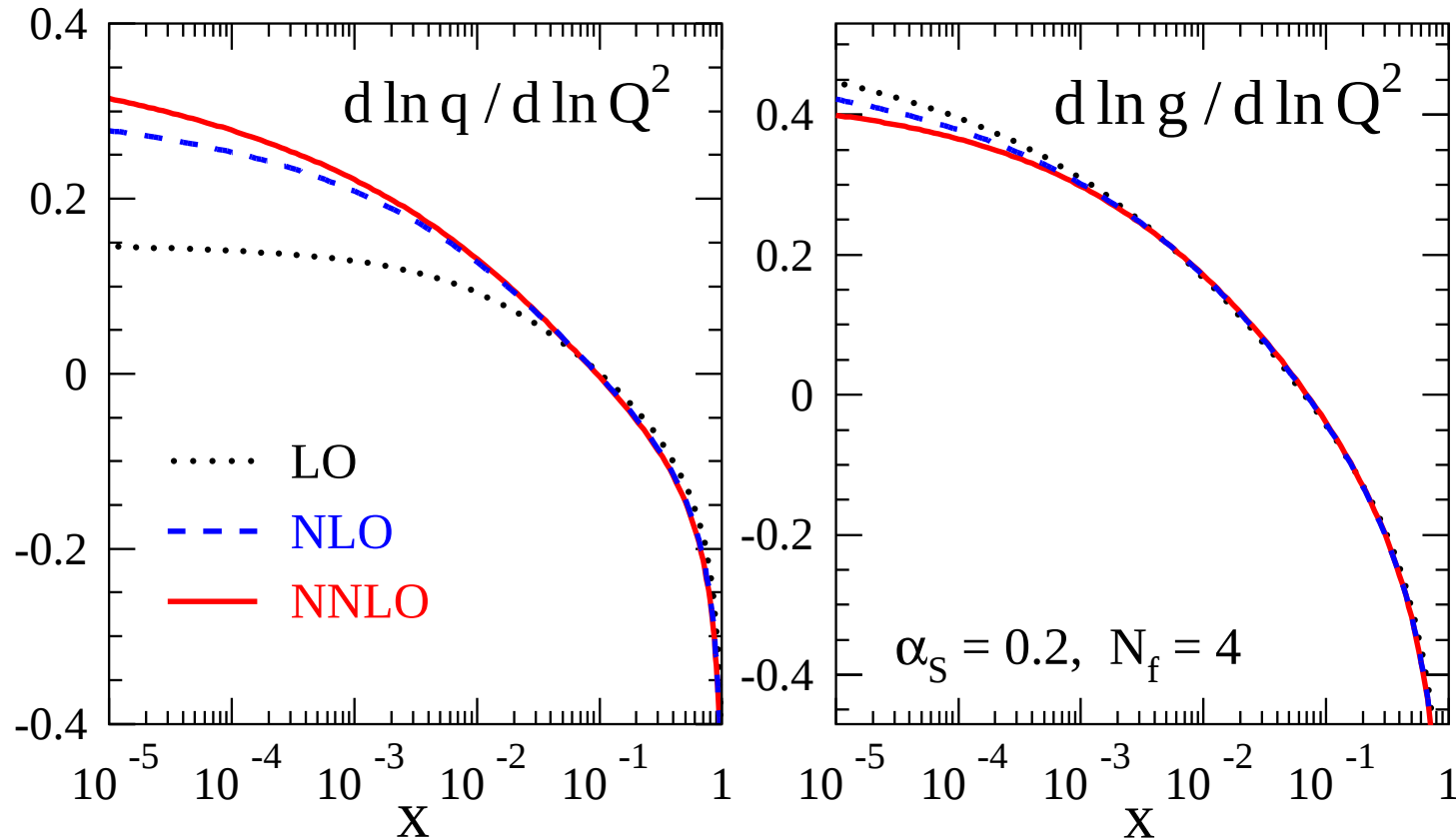
Perturbative stability of evolution

- Scale derivatives of quark and gluon distributions at $Q^2 \approx 30 \text{ GeV}^2$



Perturbative stability of evolution

- Scale derivatives of quark and gluon distributions at $Q^2 \approx 30 \text{ GeV}^2$



- Expansion very stable except for very small momenta $x \lesssim 10^{-4}$

Parton cross sections

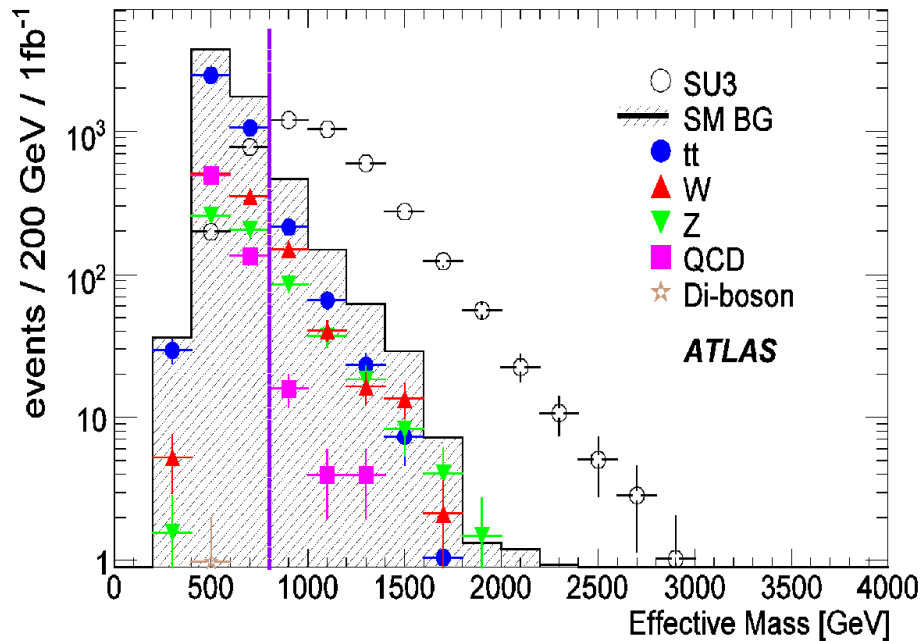
How precise are the predictions?

- Isolation of new physics signal from background
 - look for deviations from the Standard Model (if possible data driven)
 - e.g. R-parity conserved SUSY with cascade decays into LSP multiple jets, leptons and missing E_T

Perturbative QCD

- NLO QCD corrections are essential NLO (important for rates)
 - large K -factors, new parton channels may dominate beyond tree level
 - e.g. $pp \rightarrow Z(\rightarrow \nu\bar{\nu}) + 4\text{jets}$ is $\mathcal{O}(\alpha_s^4)$ and $\Delta(\alpha_s^{\text{LO}}) \simeq 10\%$ gives $\Delta(\sigma^{\text{LO}}) \simeq 40\%$

SUSY searches



Typical selection cuts

- $N_{\text{jet}} \geq 4$
- $E_{T(1)} > 100\text{GeV}$
- $E_{T(2,3,4)} > 50\text{GeV}$
- $M_{\text{eff}} = \text{MET} + \sum_i E_{Ti}$

Example: mSUGRA, point SU3

- $m_0 = 100\text{ GeV}, m_{1/2} = 300\text{ GeV},$
 $\tan \beta = 6, A_0 = -300, \mu > 0$

- Discrimination of BSM signal from background requires precise predictions (exact LO matrix elements)
- SM background in high-end tail of missing E_T
e.g. $pp \rightarrow Z(\rightarrow \nu\bar{\nu}) + 4\text{jets}$
- Significance of potential disagreement between data and MadGraph/Sherpa/Algen/... ?

LHC “priority” wishlist

process ($V \in \{\gamma, W^\pm, Z\}$)	background to	accomplished
$pp \rightarrow VV + 1 \text{ jet}$ $pp \rightarrow H + 2 \text{ jets}$ $pp \rightarrow t\bar{t}b\bar{b}$ $pp \rightarrow t\bar{t} + 2 \text{ jets}$ $pp \rightarrow VVb\bar{b}$ $pp \rightarrow VV + 2 \text{ jets}$ $pp \rightarrow V + 3 \text{ jets}$ $pp \rightarrow VVV$	$t\bar{t}H$, new physics H production by vector boson fusion (VBF) $t\bar{t}H$ $t\bar{t}H$ $\text{VBF} \rightarrow VV, t\bar{t}H$, new physics $\text{VBF} \rightarrow VV$ various new physics signatures SUSY trilepton	$WW + 1 \text{ jet}$ $H + 2 \text{ jets}$ $t\bar{t}b\bar{b}$

Les Houches 2005 [hep-ph/0604120]

Why are one-loop corrections difficult ?

- Outline of a generic NLO calculation

Real corrections

- subtractions (IR-divergent)

Virtual corrections

+ subtractions (IR-divergent)

Cancellation of singularities

Finite partonic cross sections

Phase space integration

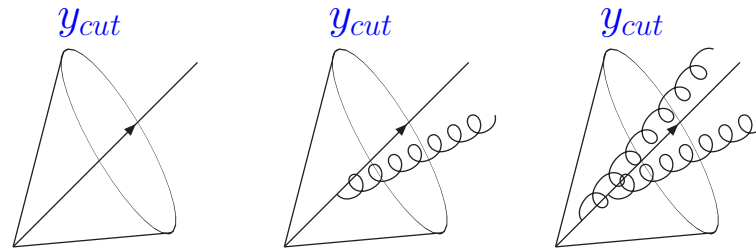
Convolution with PDFs

Monte Carlo

- All conceptual issues solved (“just” technical work)
- However, no general libraries available
- **Speed and stability** are the important criteria in practice

Jet definitions

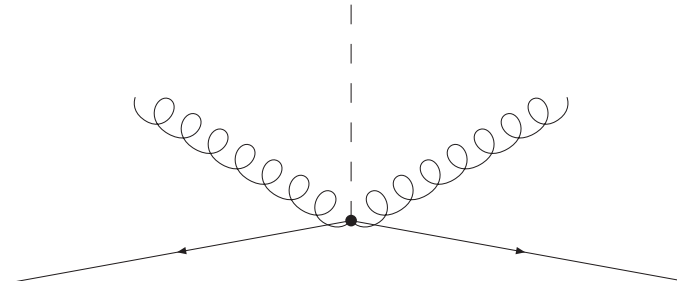
- Historically: Stermen-Weinberg criterium for two-jet event
 - energy fraction $1 - \epsilon$ in cone of half angle δ
 - not practical for multi-particle events
- Modern modelling of jets
 - cone- or k_t -algorithms



- JADE algorithm

$$\min (p_i + p_j)^2 = \min 2E_i E_j (1 - \cos \theta_{ij}) > y_{\text{cut}} s$$

- combines also soft gluons at large relative k_t (disadvantage)
e.g. potential three-jet event



Jets in hadronic collisions

- Cone algorithm

- define cone of radius R in η, ϕ for $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$

(Some) uses of hadronic di-jets

- Hadronic di-jets: large statistics even with high- p_t cuts
 - experimental calibration (HCAL uniformity, establish missing E_t)
 - gluon jets constrain gluon PDF at medium/large x
 - searches for quark sub-structure (di-jet angular correlations)

Kinematics (differential)

- Proton-proton scattering (two broad-band beams of incoming partons)
 - cms of parton-parton scattering boosted wrt incoming protons
- Final state variables (simple transformations under longitud. boosts)

$$p^\mu = (E, p_x, p_y, p_z) = (m_t \cosh y, p_t \sin \phi, p_t \cos \phi, m_t \sinh y)$$

- rapidity $y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$
- transverse momentum p_t and mass $m_t = \sqrt{p_t^2 + m^2}$
- azimuthal angle ϕ

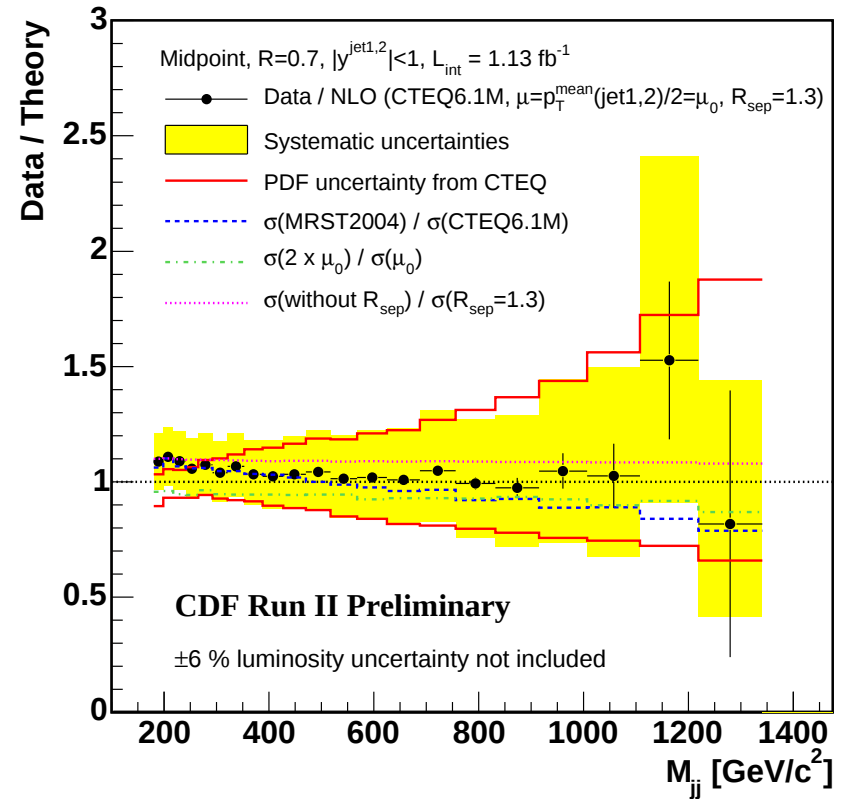
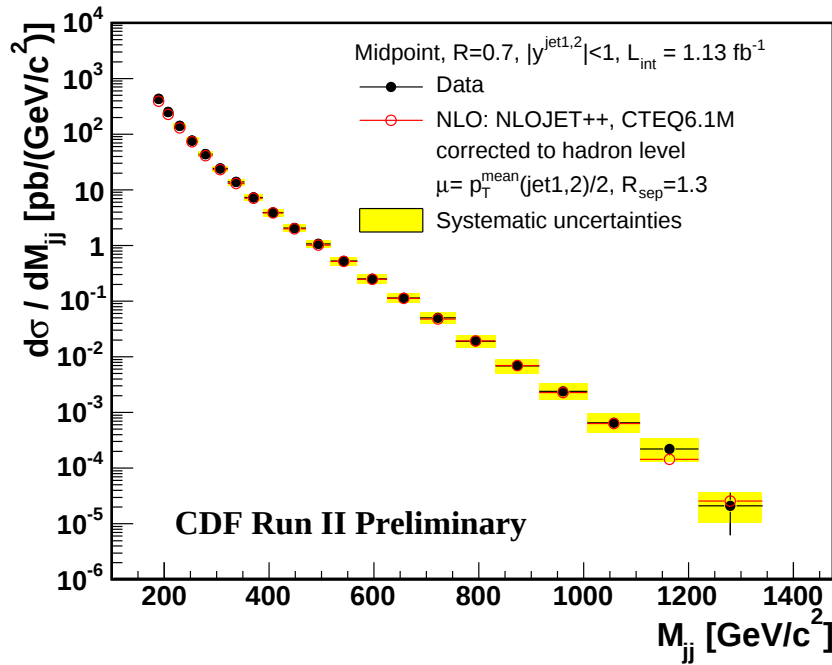
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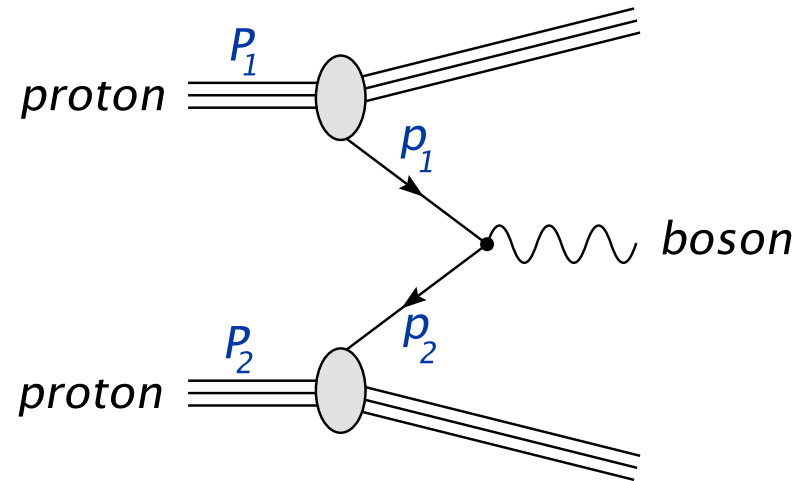
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- transverse momentum p_t and mass $m_t = \sqrt{p_t^2 + m^2}$
- azimuthal angle ϕ
- Differences in rapidity Δy and azimuthal angle $\Delta \phi$ invariant under boosts
- In practice (for $E \gg m_p$)
 - pseudo-rapidity $\eta = -\ln \tan \left(\frac{\theta}{2} \right)$ with angle from beam axis

Jets at Tevatron



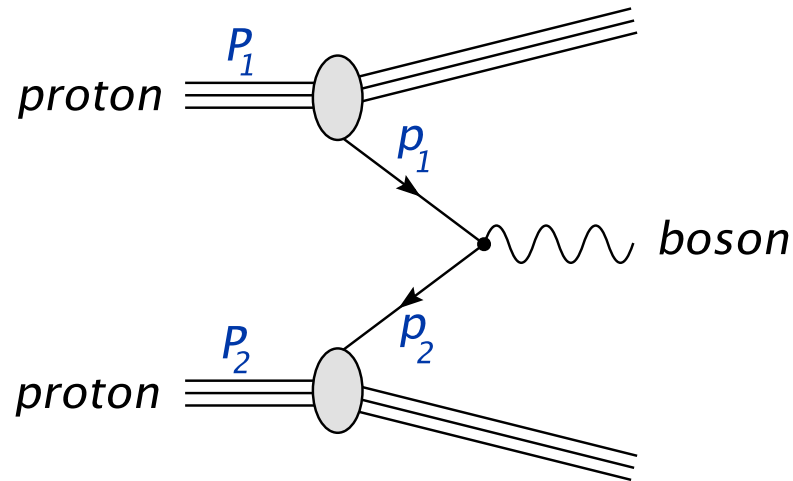
- Di-jet invariant mass distribution
 - agreement with perturbative QCD over eight orders of magnitude
 - larger uncertainties for high M_{jj}^2

Vector boson production

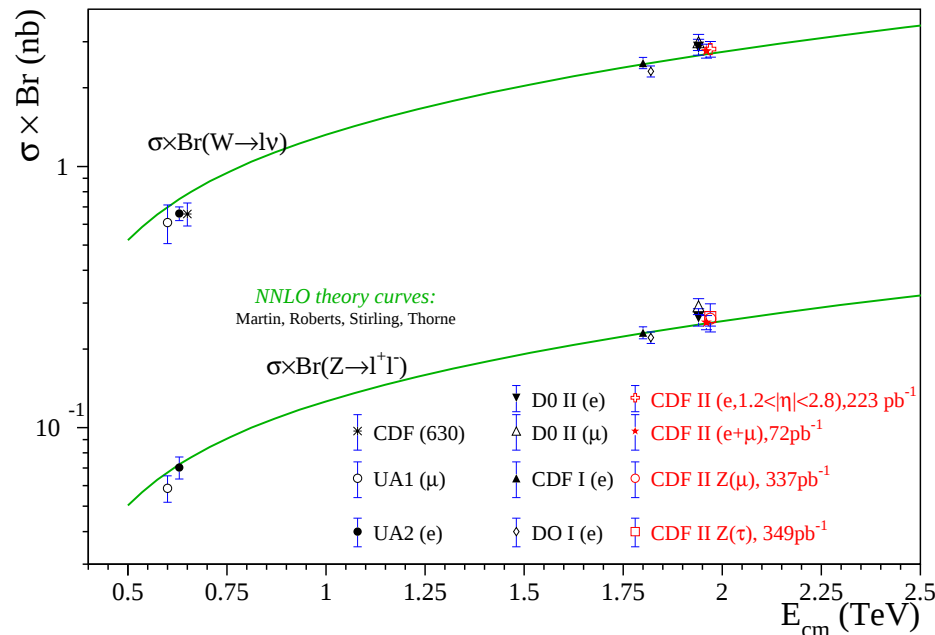


- Kinematical variables (inclusive)
 - energy (cms) $s = Q^2$ (space-like)
 - scaling variable $x = M_{W^\pm/Z}^2/s$

Vector boson production

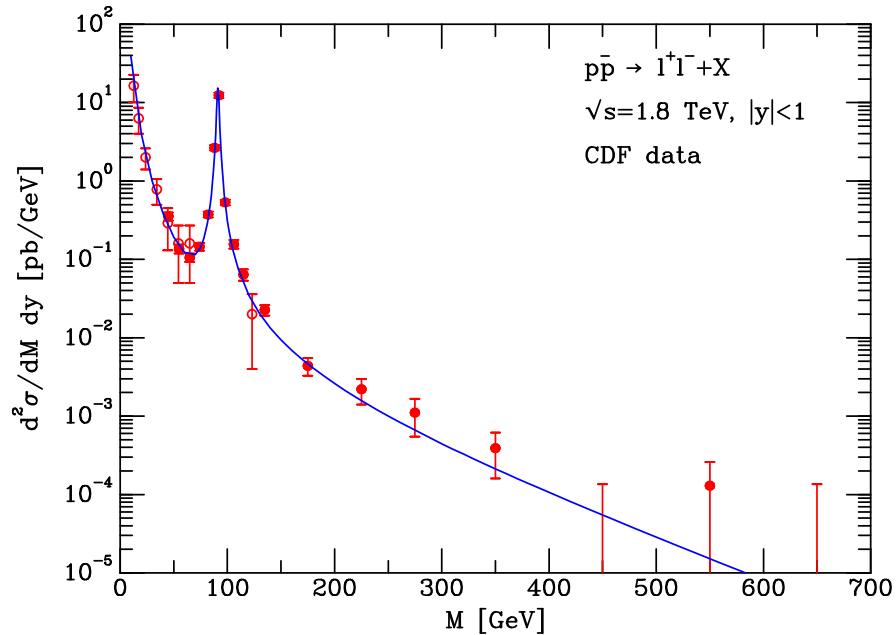


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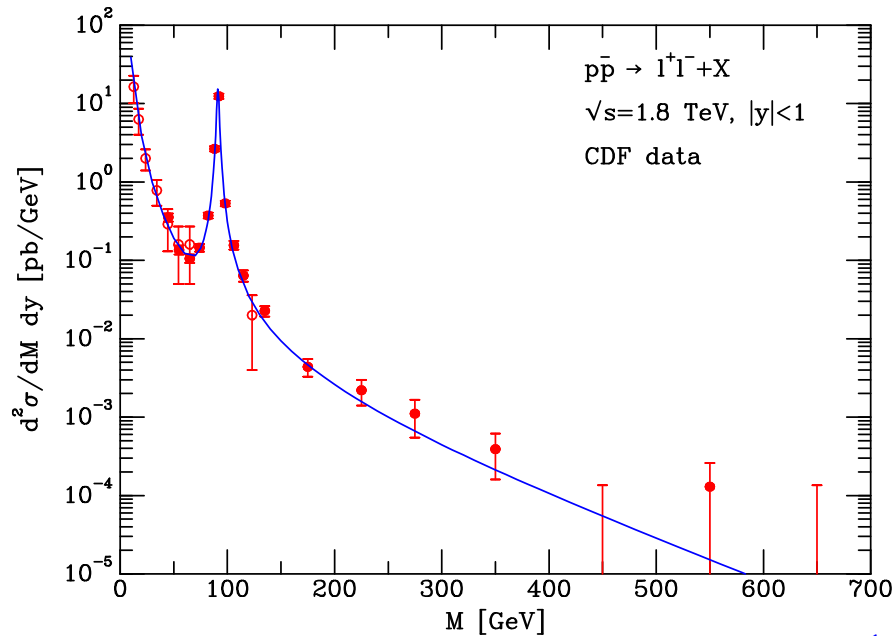
- 20 years of measurements of $W^\pm$ and Z cross sections at hadron colliders

Differential distributions



- Invariant mass distribution $\frac{d\sigma}{dM^2}$ of lepton pair for Z -production in $p\bar{p}$ -collisions
- CDF data at $\sqrt{s} = 1.8 \text{ TeV}$ and NLO QCD prediction

Differential distributions



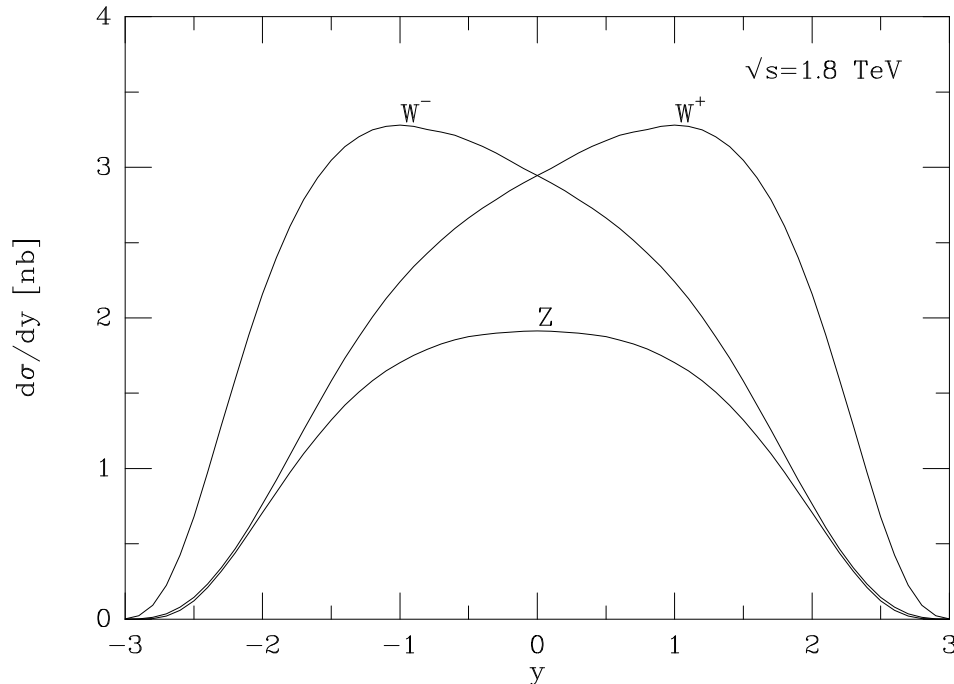
- Invariant mass distribution $\frac{d\sigma}{dM^2}$ of lepton pair for Z -production in $p\bar{p}$ -collisions
- CDF data at $\sqrt{s} = 1.8$ TeV and NLO QCD prediction

$$M^4 \frac{d\sigma}{dM^2} = \sigma^{(0)} \frac{1}{N} \frac{M^2}{s} \int_0^1 dx_1 dx_2 \delta \left(x_1 x_2 - \frac{M^2}{s} \right) \times \sum_q e_q^2 \{ f_q(x_1) f_{\bar{q}}(x_2) + f_{\bar{q}}(x_1) f_q(x_2) \}$$

- Double-differential cross section $\frac{d\sigma}{dM^2 dy}$ local in PDFs

- $y = \frac{1}{2} \ln \left(\frac{x_1}{x_2} \right)$ lepton-pair rapidity

$W^\pm$ asymmetry

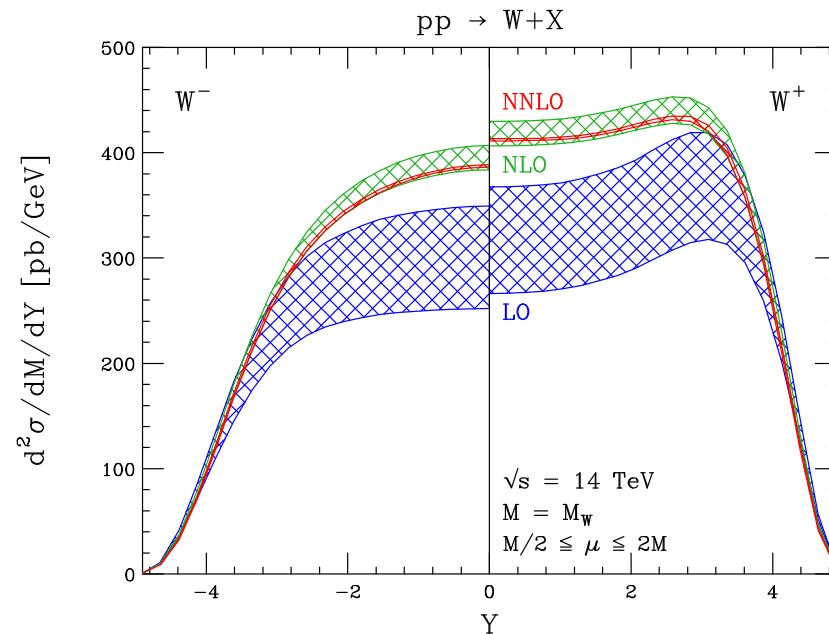
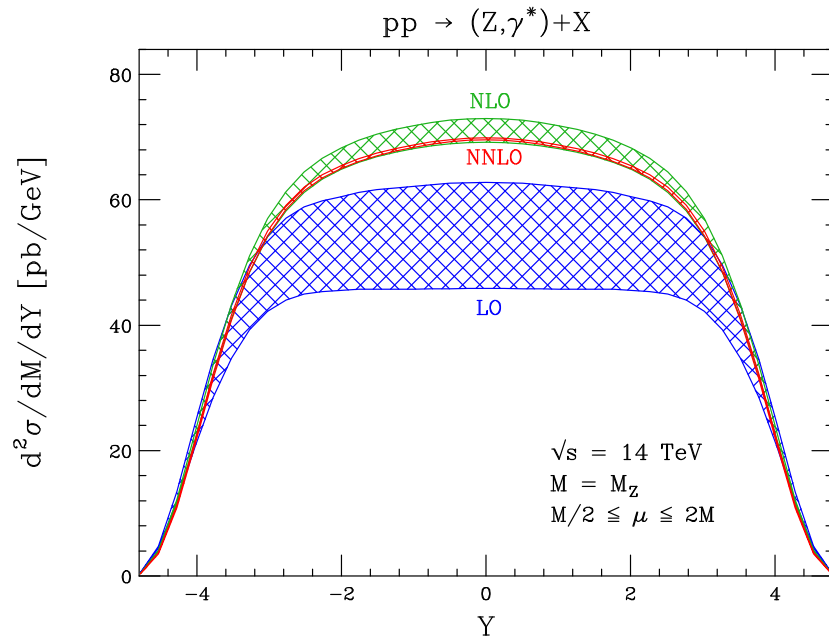


- Rapidity distributions for $W^\pm$ - and Z -production in $p\bar{p}$ -collisions
- CP invariance $\longrightarrow$ $\frac{d\sigma}{dy}$ for Z -production symmetric around $y = 0$

- $W^\pm$ rapidity asymmetry sensitive to flavor decomposition of proton

$$A_W(y) = \frac{d\sigma(W^+)/dy - d\sigma(W^-)/dy}{d\sigma(W^+)/dy + d\sigma(W^-)/dy}$$
$$\simeq \frac{u(x_1)d(x_2) - d(x_1)u(x_2)}{u(x_1)d(x_2) + d(x_1)u(x_2)}$$

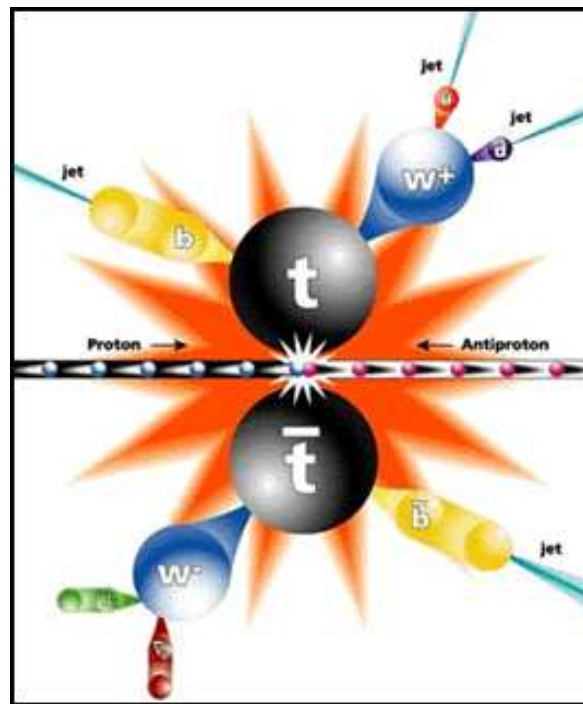
Differential distributions at NNLO in QCD



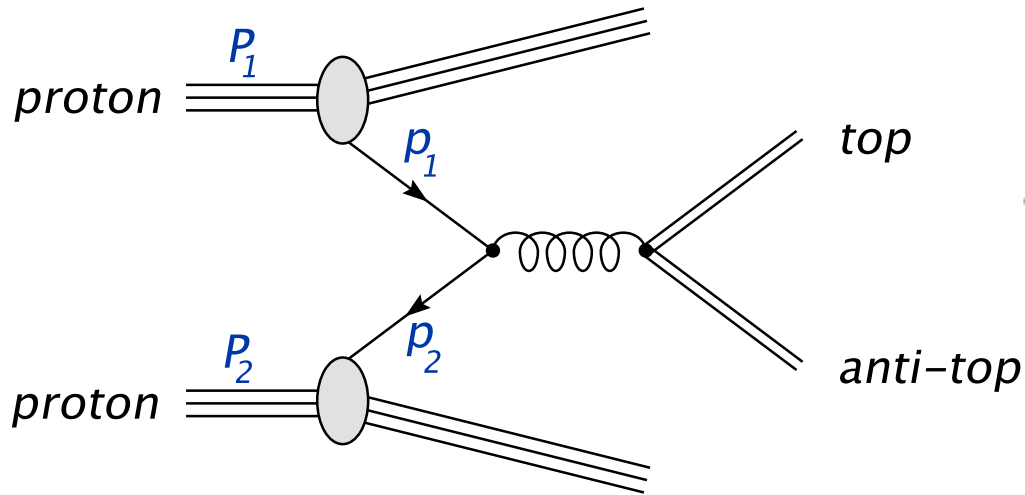
- $W^\pm, Z$ -boson rapidity distribution with scale variation $m_{W,Z}/2 \leq \mu \leq 2m_{W,Z}$
Anastasiou, Petriello, Melnikov '05
- Reduction of theoretical uncertainties (renormalization / factorization scale) to level of 1% in NNLO QCD analysis
Dissertori '05

Hadronic top-quark pair-production

- Tevatron: $t\bar{t}$ -pair with subsequent decay
 - $t \rightarrow Wb$ decay and leptonic or hadronic $W^\pm$ -decay



Top-quark pair-production

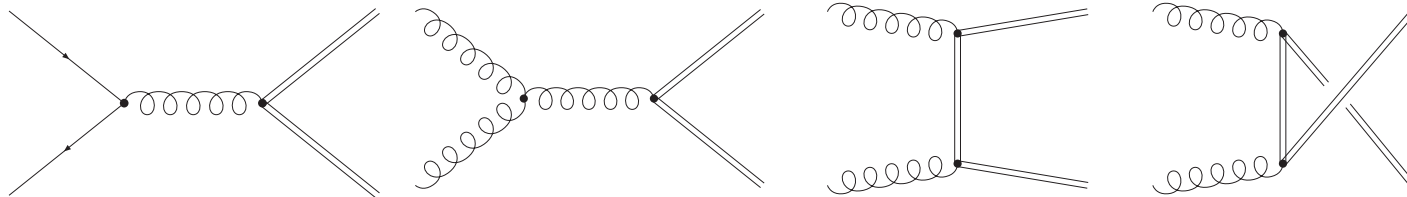


- Top decay
 leptonic: $t \rightarrow W^+ + b \rightarrow l^+ + \nu + b$
 hadronic: $t \rightarrow W^+ + b \rightarrow q + \bar{q} + b$

- Leading order Feynman diagrams

$$q + \bar{q} \longrightarrow Q + \bar{Q}$$

$$g + g \longrightarrow Q + \bar{Q}$$

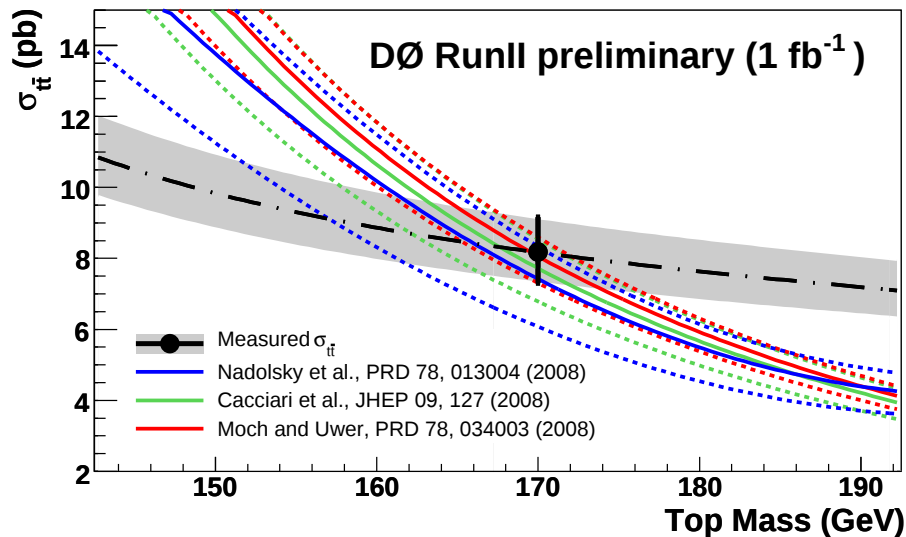


- NLO in QCD Nason, Dawson, Ellis '88; Beenakker, Smith, van Neerven '89; Mangano, Nason, Ridolfi '92; Bernreuther, Brandenburg, Si, Uwer '04; ...

- $q\bar{q}$ and gg dominant at NLO; neglect $qg \longrightarrow$ at NLO only $\mathcal{O}(1\%)$

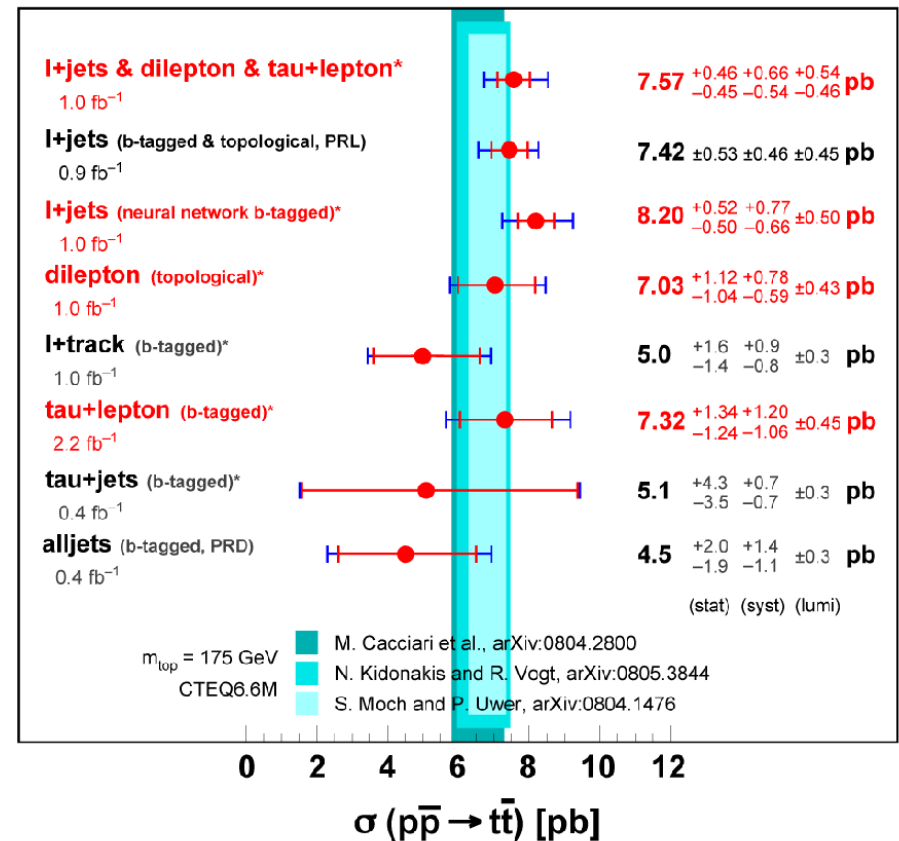
Tevatron analyses

- Total cross section and different channels of Tevatron analyses (theory uncertainty band from scale variation)
- Determination of m_t from total cross section (slope $d\sigma/dm_t$)
 - e.g. DZero '09: NLO $m_t = 165.5^{+6.1}_{-5.9}$; NNLO $m_t = 169.1^{+5.9}_{-5.2}$; ...



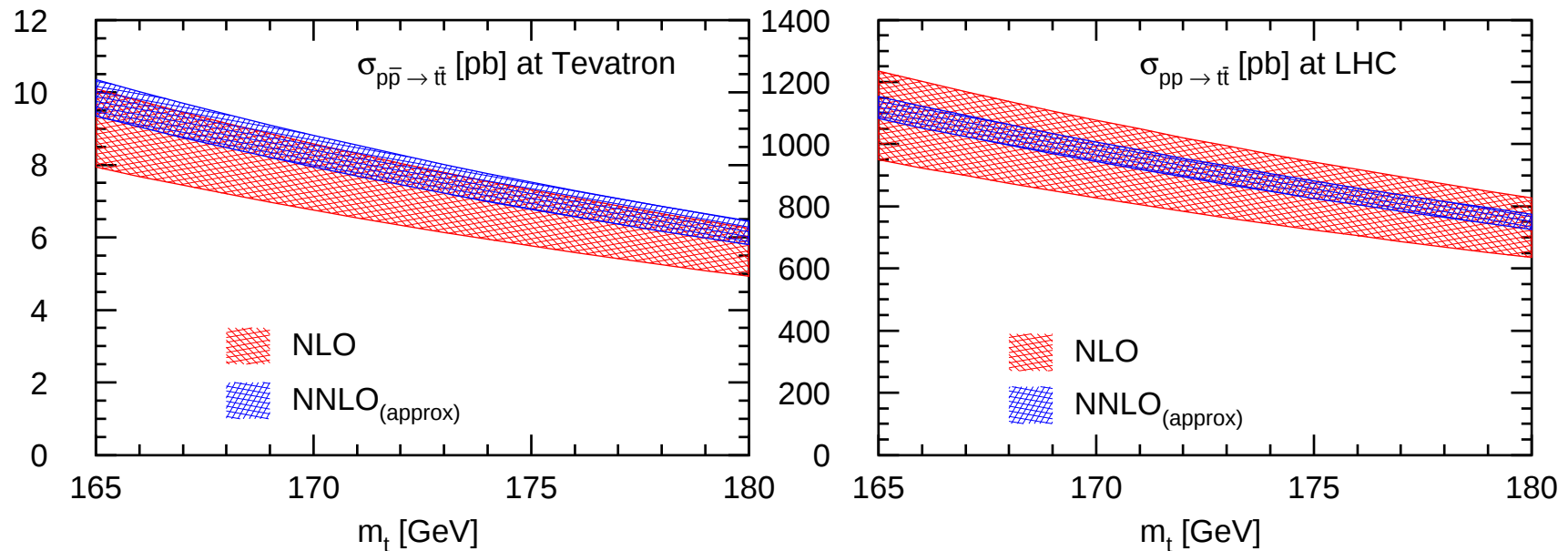
D0 Run II * = preliminary

April 2009



LHC total cross section

- NLO (with MRST2006 PDF set)
 - scale uncertainty $\mathcal{O}(10\%) \oplus$ PDF uncertainty $\mathcal{O}(5\%)$
- NNLO_{approx} (with MRST2006 PDF set)
 - scale uncertainty $\mathcal{O}(3\%) \oplus$ PDF uncertainty $\mathcal{O}(2\%)$

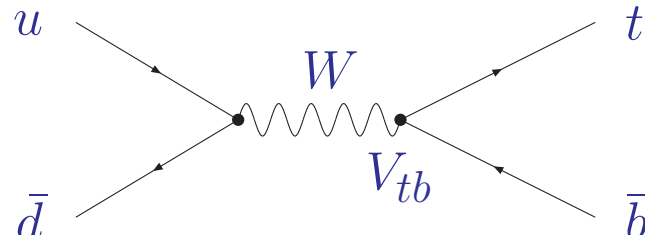


- Theory at NNLO matches anticipated experimental precision $\mathcal{O}(10\%)$

Single top-quark production

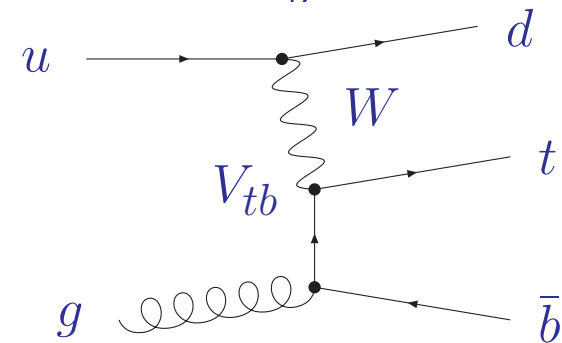
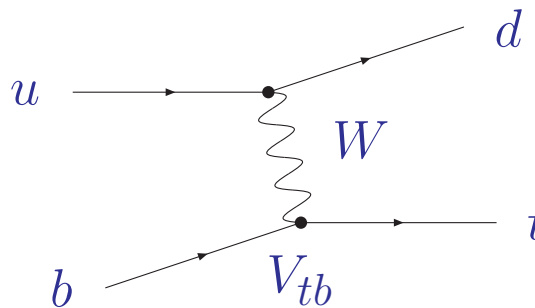
- Single-top production allows study of charged-current weak interaction of top quark
 - direct extraction of the CKM-matrix element V_{tb}
 - flagship measurement of Tevatron run II (control QCD bckgrd !)

- s -channel production



- t -channel production

- bg -channel at NLO enhanced by gluon luminosity



- Large corrections from extensions of Standard Model

- t -channel: anomalous couplings or flavor changing neutral currents
- s -channel: charged “top-pion”, Kaluza-Klein modes of W or W' -boson

Summary

Introduction to QCD and Electroweak Physics

- The big questions
- Basics of perturbative QCD
- QCD factorization for hard scattering
- Parton luminosity
- Jet cross sections at hadron colliders
- $W^\pm$ and Z -boson production at LHC
- Hadro-production of Top-Quarks

Outlook

- Higgs, Supersymmetry and beyond *Tuesday, August 04, 2009*

Literature

- Review

- *Expectations at LHC from hard QCD*

- J. Phys. G: Nucl. Part. Phys. **35**, 073001 (2008) [arXiv:0803.0457] [hep-ph].