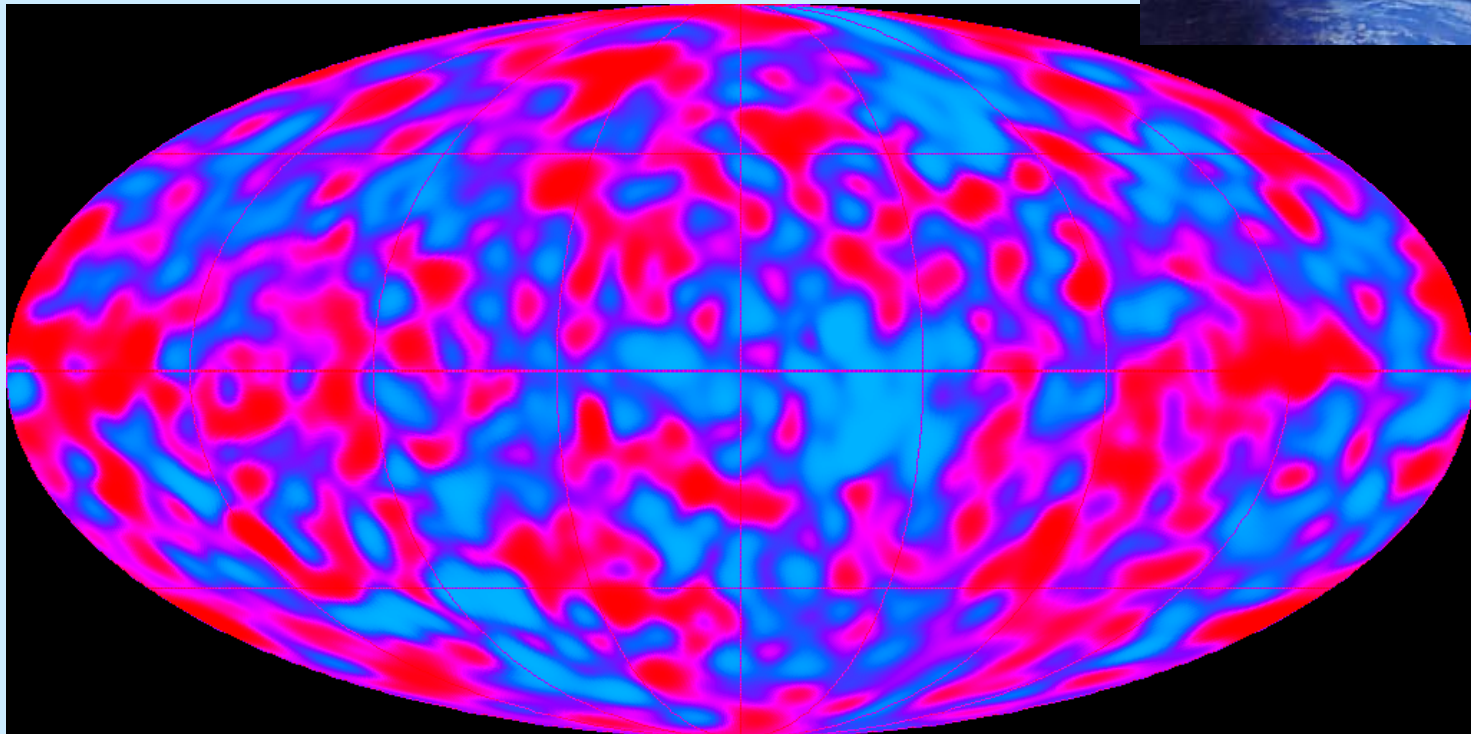


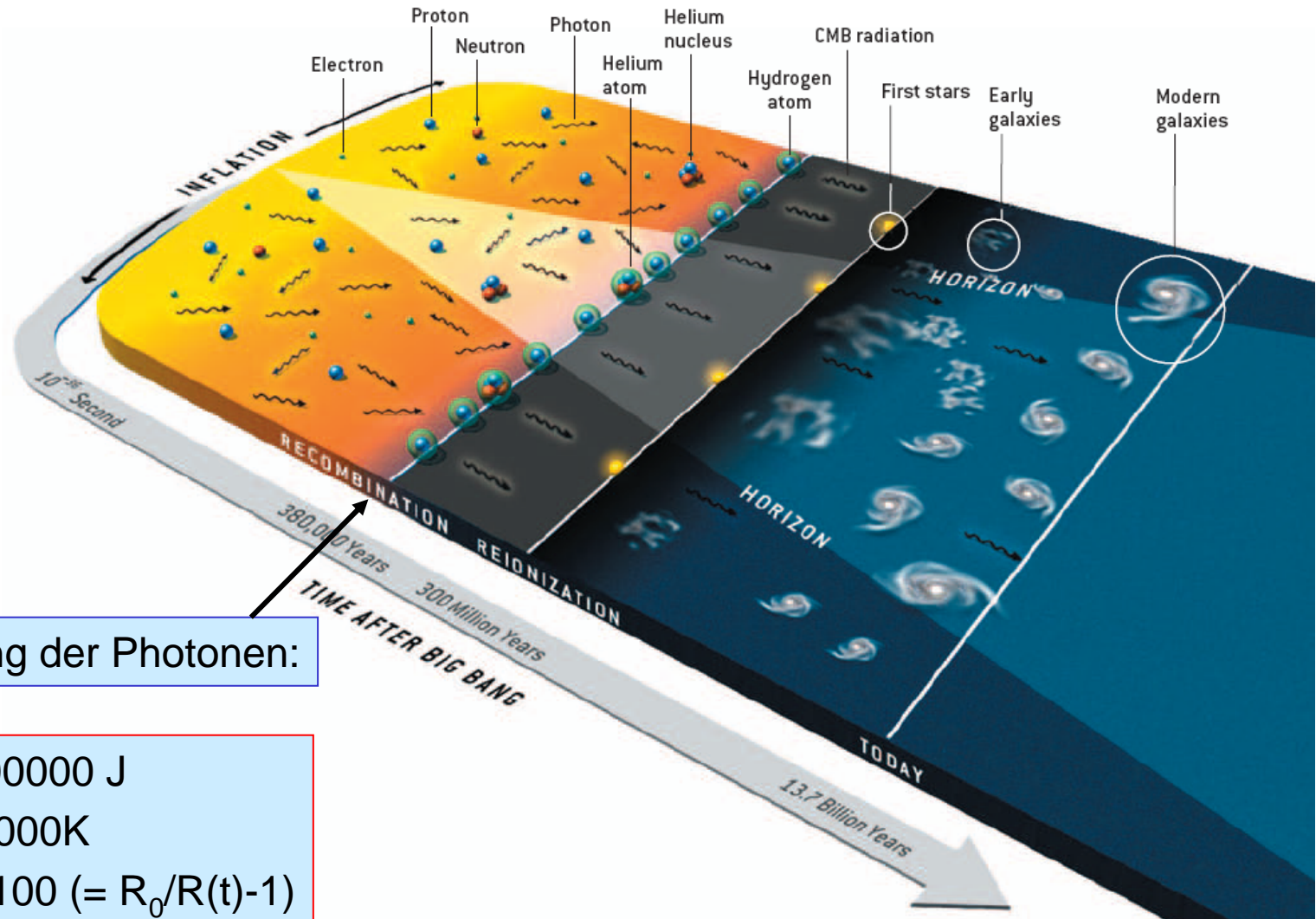
2.5 Mikrowellen-Hintergrundstrahlung (CMBR)

Entkopplung der Photonen:

- $t \approx 400000 \text{ J}$
- $T \approx 3000\text{K}$
- $z \approx 1100 (= R_0/R(t)-1)$



Entwicklung des Universums

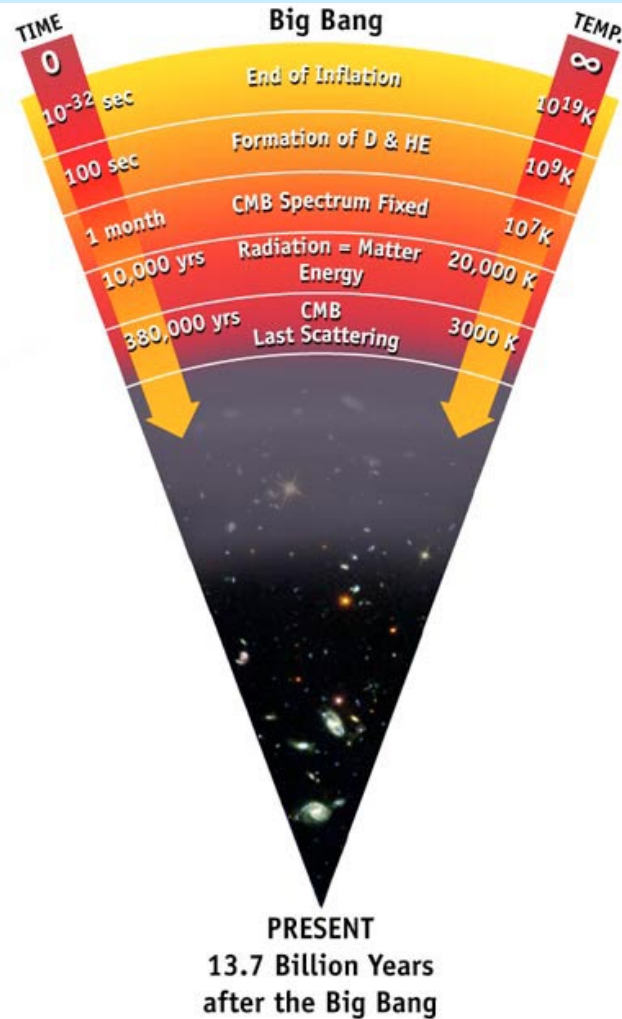


Entkopplung der Photonen:

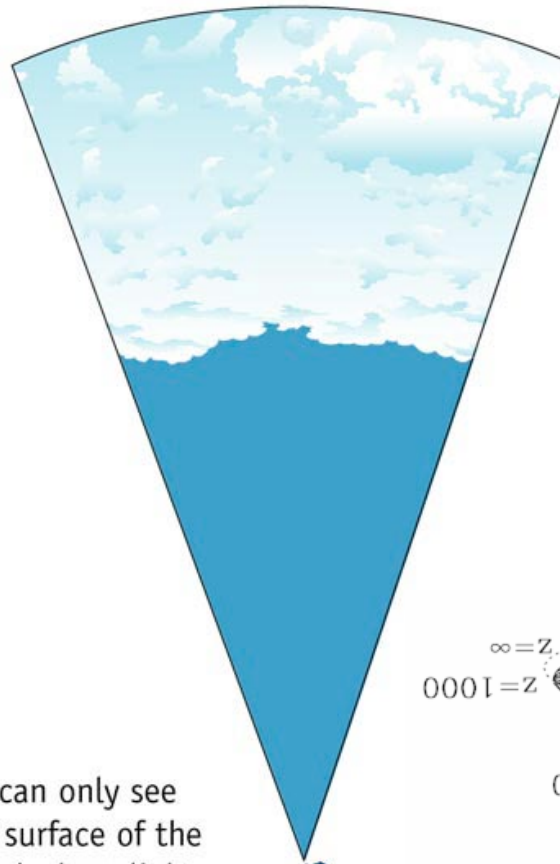
- $t \approx 400000$ J
- $T \approx 3000$ K
- $z \approx 1100 (= R_0/R(t)-1)$

Die 'letzte Streufläche' der Photonen

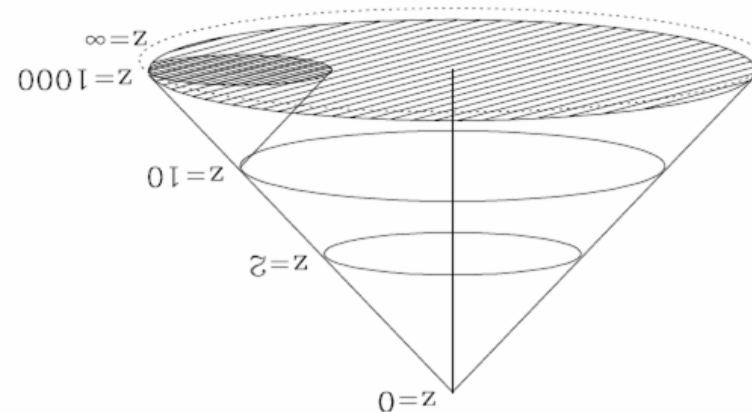
(Last Scattering Surface)



The cosmic microwave background Radiation's "surface of last scatter" is analogous to the light coming through the clouds to our eye on a cloudy day.



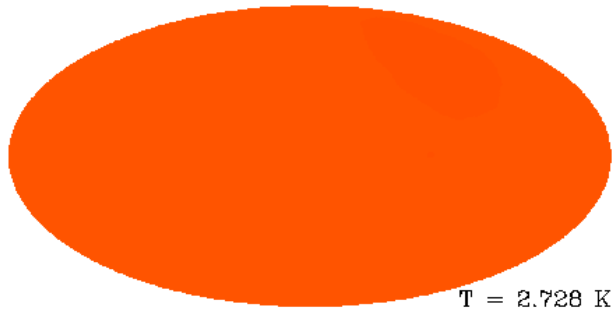
We can only see the surface of the cloud where light was last scattered



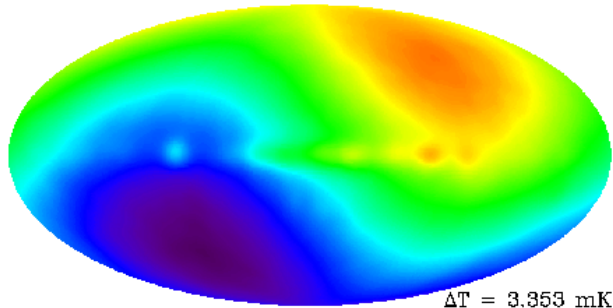
Phasen der kosmologischen Entwicklung

t [s]	E [GeV]	T [K]	R [m]	
10^{-44}	10^{19}	10^{32}	10^{-5}	Planckzeit, $\lambda_{Compton} \approx r_S$
10^{-36}	10^{15}	10^{28}	10^{-2}	$E \approx M_X$, GUT-Symmetrie-Brechung, Baryogenese
10^{-10}	10^2	10^{15}	10^{12}	$E \approx M_W$, $SU(2)_L \times U(1)$ -Symmetrie-Brechung
10^{-6}	10^0	10^{13}	10^{14}	Quark-Confinement, $p\bar{p}$ -Annihilation
10^0	10^{-3}	10^{10}	10^{17}	Neutrinos entkoppeln, e^+e^- -Annihilation
10^2	10^{-4}	10^9	10^{18}	Bildung leichter Kerne (Nukleosynthese)
10^{12}	10^{-9}	10^4	10^{23}	Photonen entkoppeln, Übergang von Strahlungs- zu Materie-Dominanz, Bildung von Atomen, Sternen, Galaxien
10^{17}	10^{-13}	10^0	10^{26}	Bildung des Sonnensystems und von organischem Leben, heute ($t_0 \approx 2 \cdot 10^{10}$ Jahre)

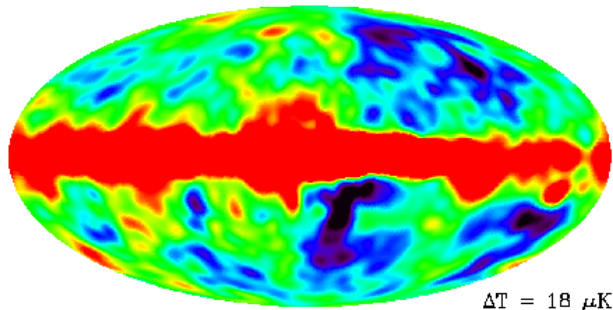
COBE-Messungen



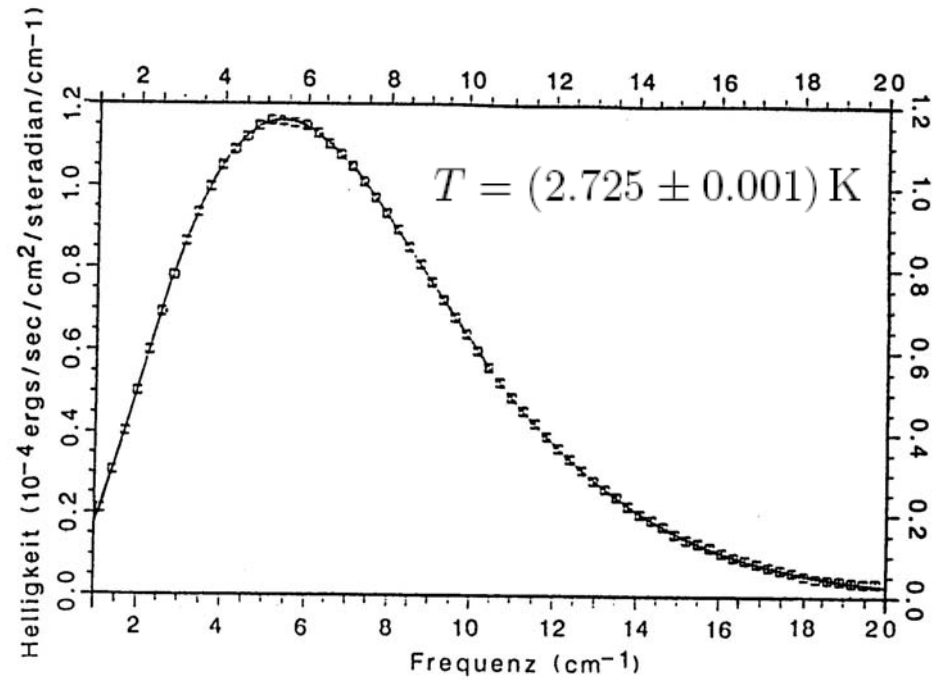
$T = 2.728 \text{ K}$



$\Delta T = 3.353 \text{ mK}$

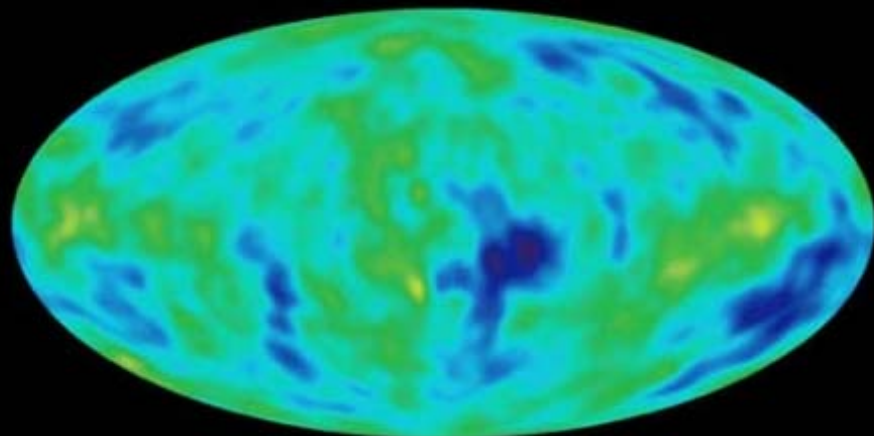
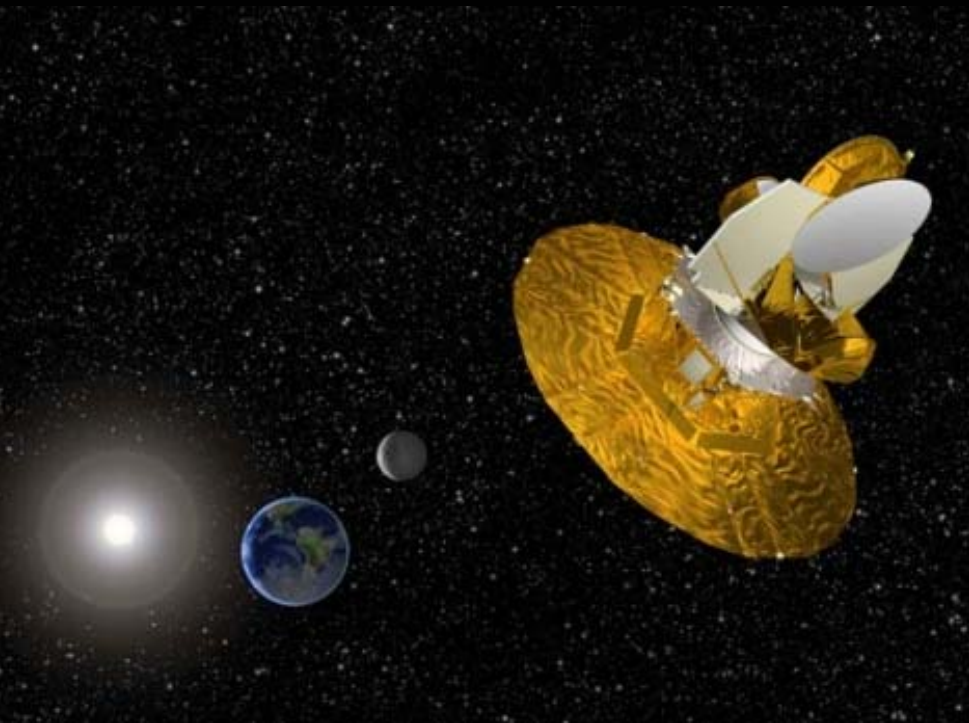


$\Delta T = 18 \mu\text{K}$

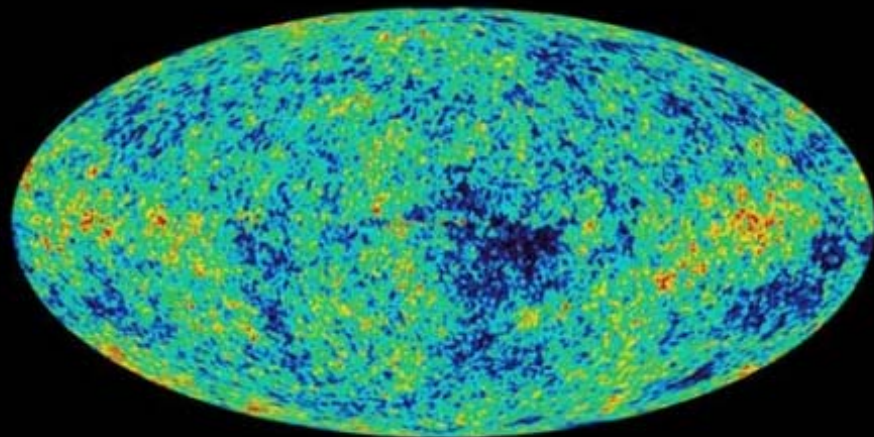


$$I(\nu)d\nu = \frac{2h\nu^3}{c^2} \frac{1}{\exp\left(\frac{h\nu}{kT}\right) - 1} d\nu,$$

WMAP

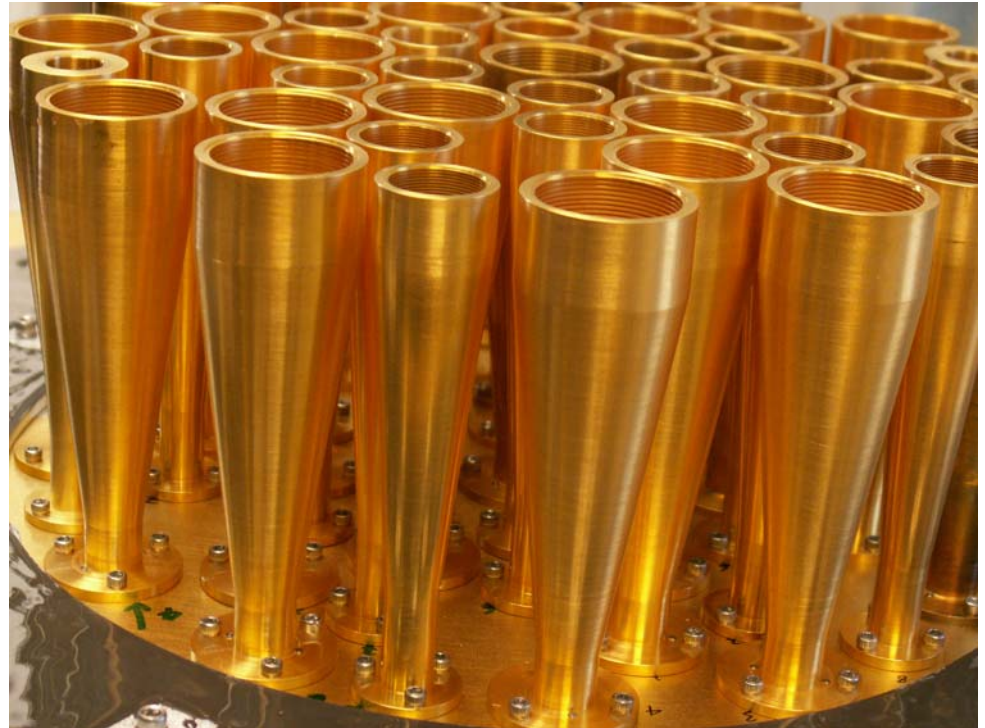
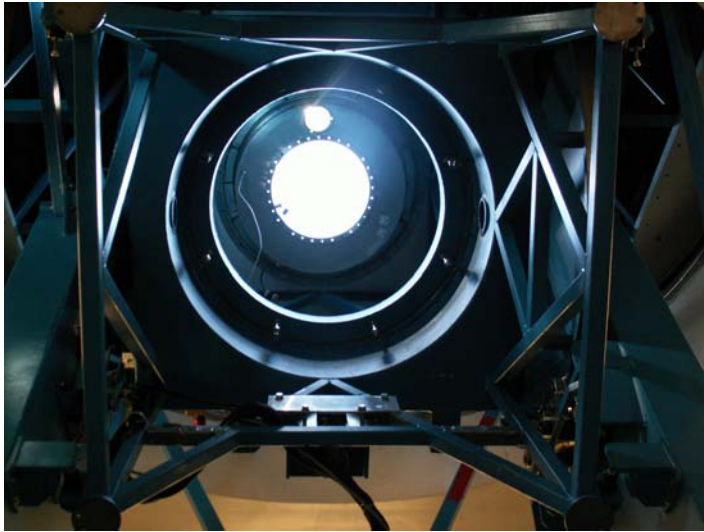


COBE



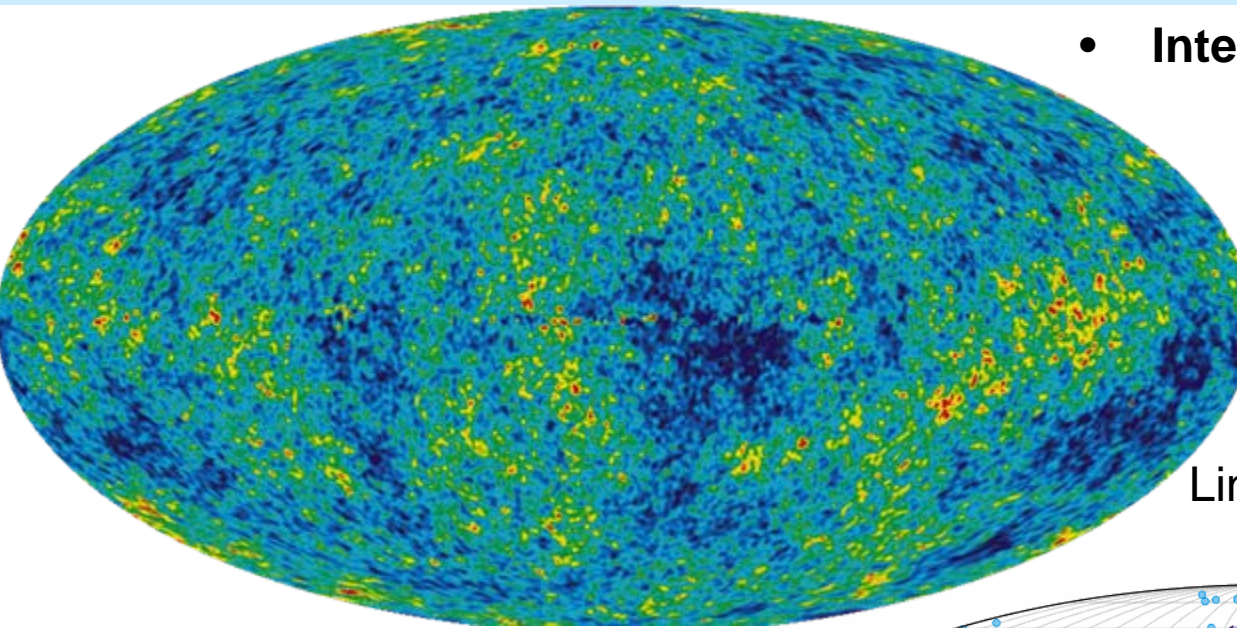
MAP

DASI-Feier am Südpol



Hörner zum Empfangen der CMBR

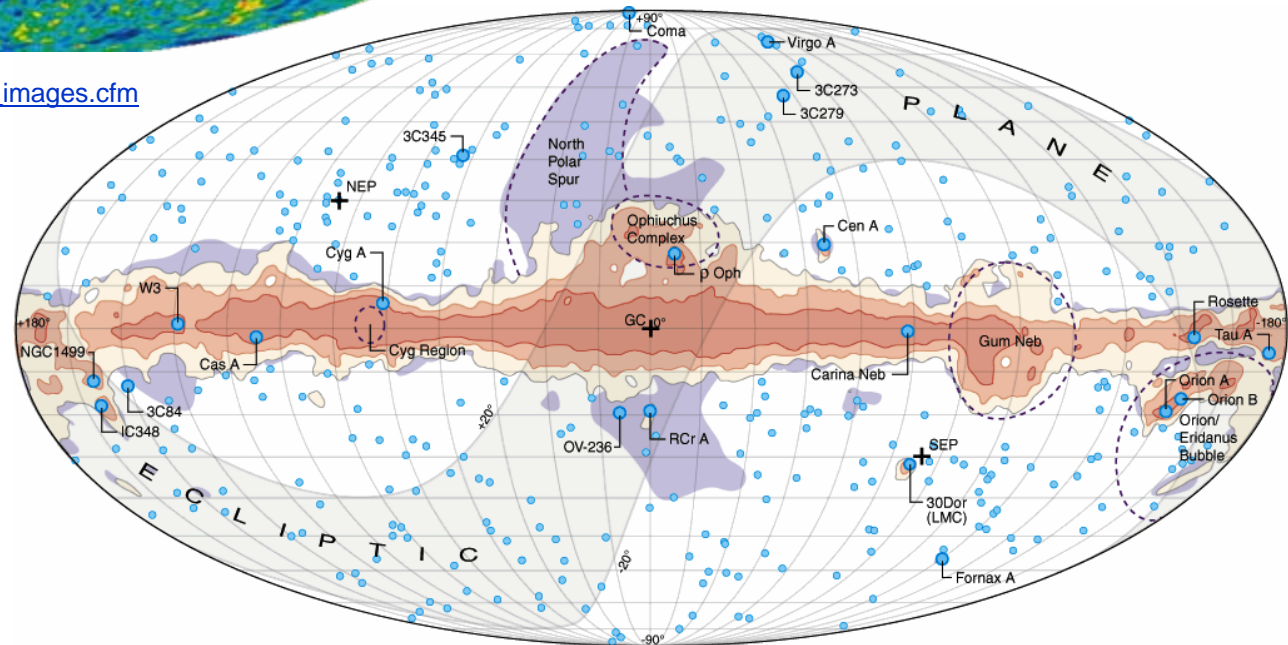
ΔT -Karte in Galaktischen Koordinaten



- **Internal Linear Combination Map**
Galactic coordinates,
Mollweide projection

Linear scale from -200 to 200 μK

http://lambda.gsfc.nasa.gov/product/map/current/m_images.cfm



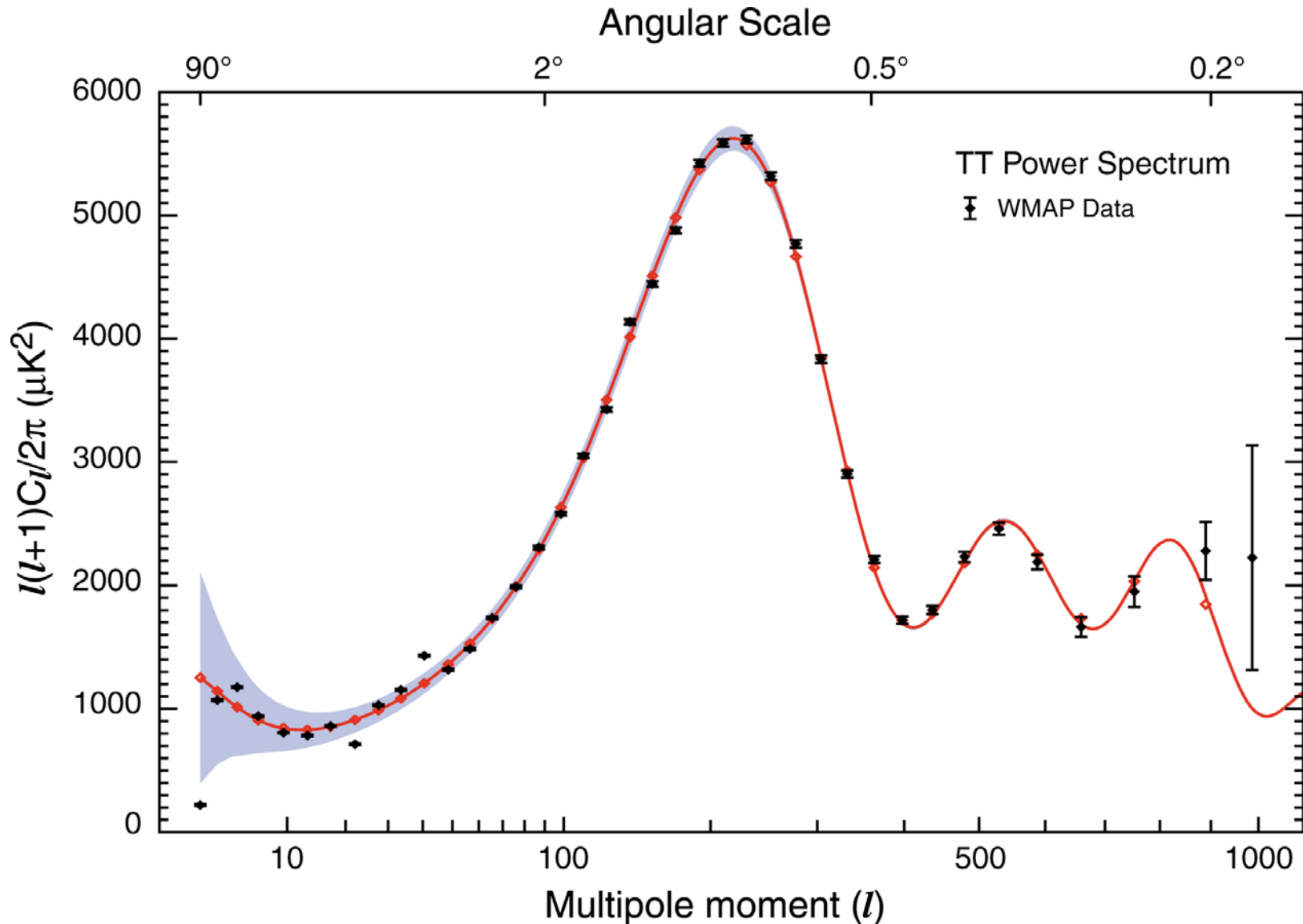
Legendre-Entwicklung der CMB-Anisotropie

$$C(\theta) = \left\langle \frac{\Delta T(\vec{n})}{T} \cdot \frac{\Delta T(\vec{m})}{T} \right\rangle_{\cos \theta = \vec{n} \cdot \vec{m}}$$

$$C(\theta) = \frac{1}{4\pi} \sum_l (2l + 1) C_l P_l(\cos \theta).$$

$$\Delta\theta \approx \frac{\pi}{l} \approx \frac{200^\circ}{l}.$$

CMB-Anisotropie: Multipol-Leistungsspektrum

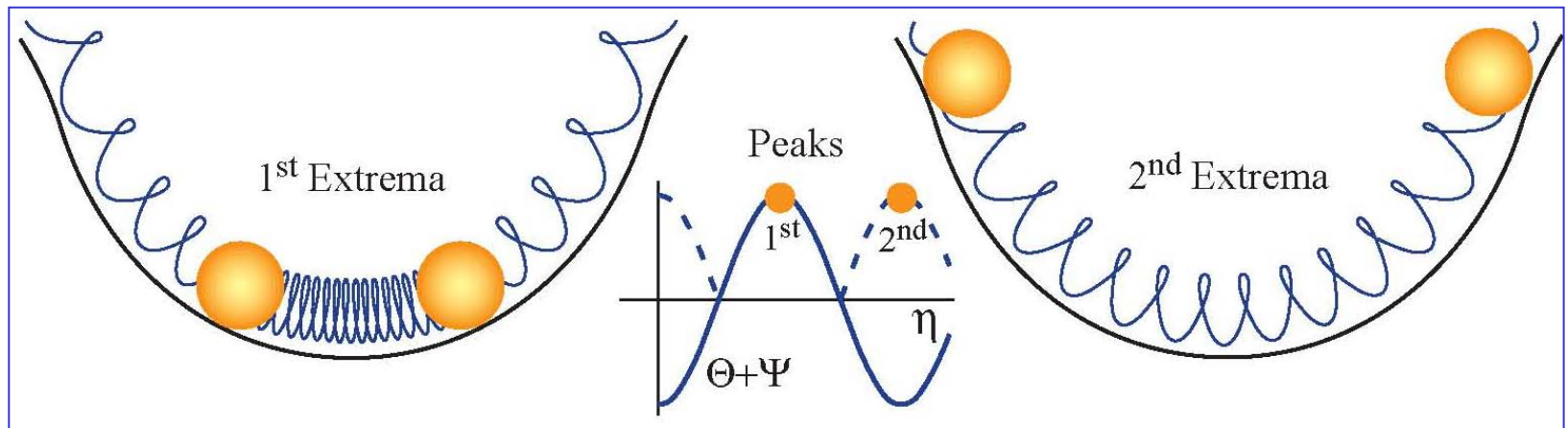


Akustische Schwingungen

Schallhorizont zur Zeit t

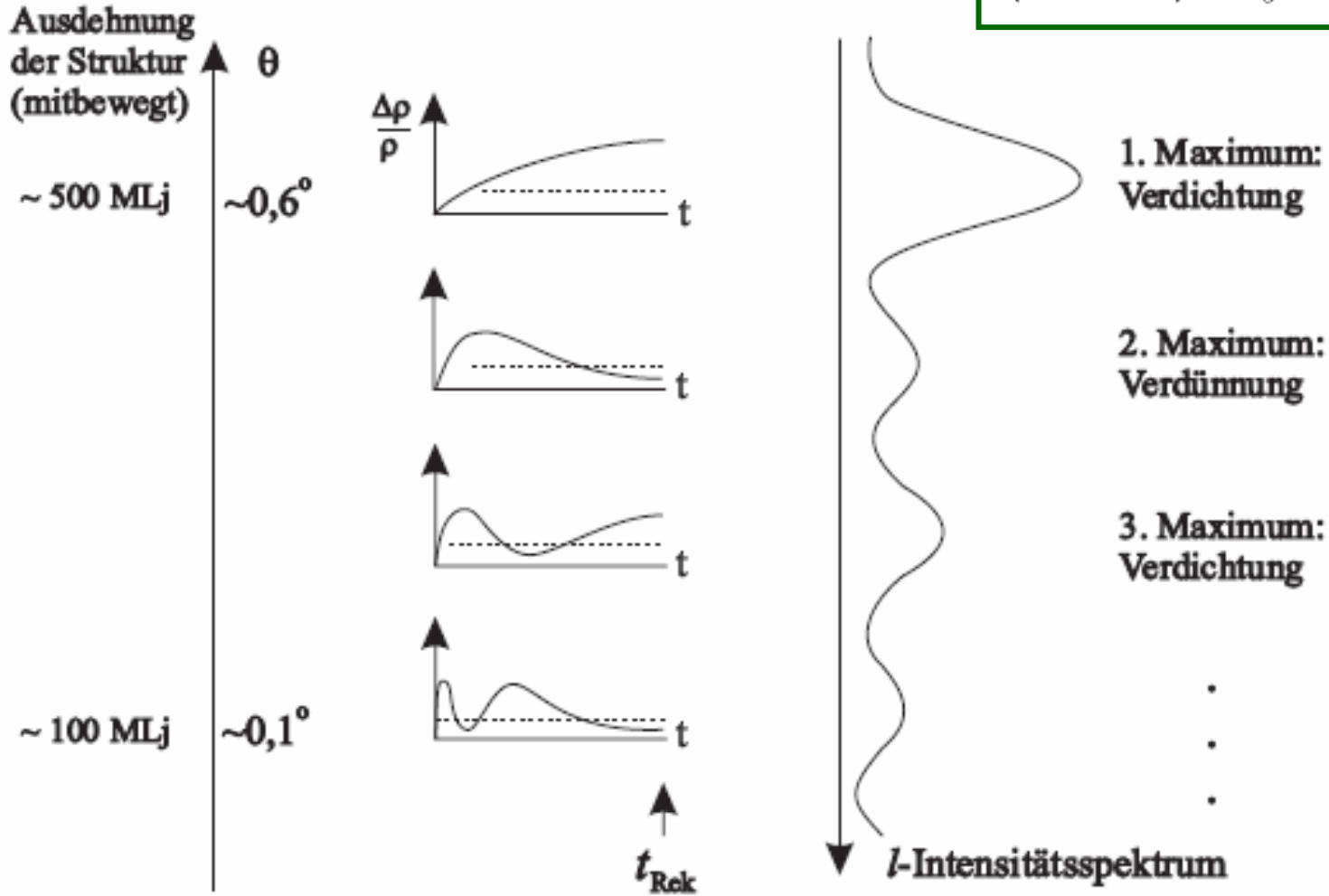
$$d_s(t) \approx \frac{v_s}{H(t)}$$

$$\left. \begin{aligned} v_s &= \sqrt{\frac{\partial p}{\partial \rho}} \\ p &= \frac{1}{3} \rho c^2 \end{aligned} \right\} \Rightarrow v_s = \frac{1}{\sqrt{3}} c$$



‘Acoustic Peaks’

$$\langle |\hat{\phi} + \hat{\Theta}|^2 \rangle = \frac{1}{9} V[\hat{\phi}] \cos^2(v_s k \eta).$$



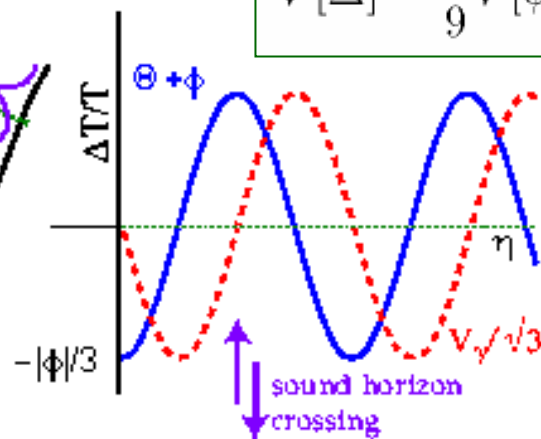
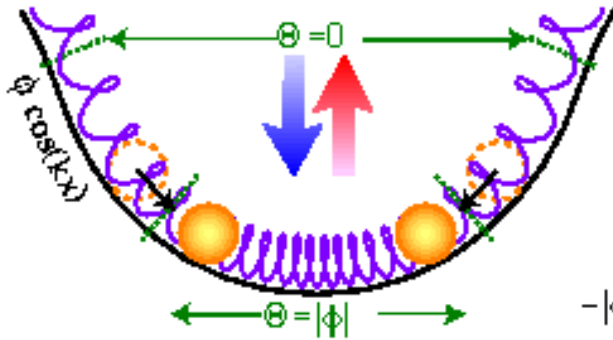
Akustische Schwingungen

Wayne Hu's Tutorial

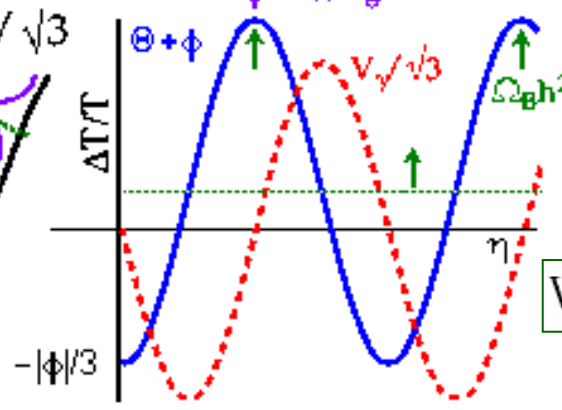
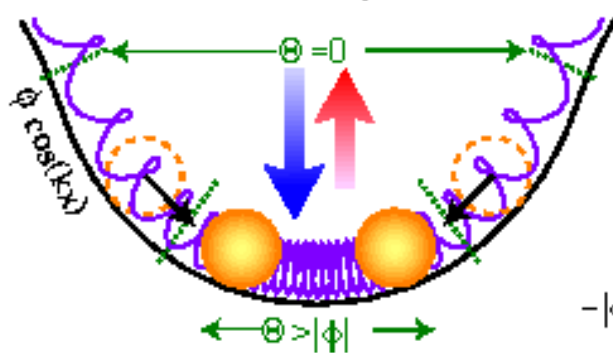
$$V[\Delta] = \frac{1}{9} V[\hat{\phi}] [\sin^2(v_s \eta k) + \cos^2(v_s \eta k)] = \frac{1}{9} V[\hat{\phi}]$$

if the sound speed v_s is exactly $c/\sqrt{3}$

(a) Photons: $c_s = c/\sqrt{3}$

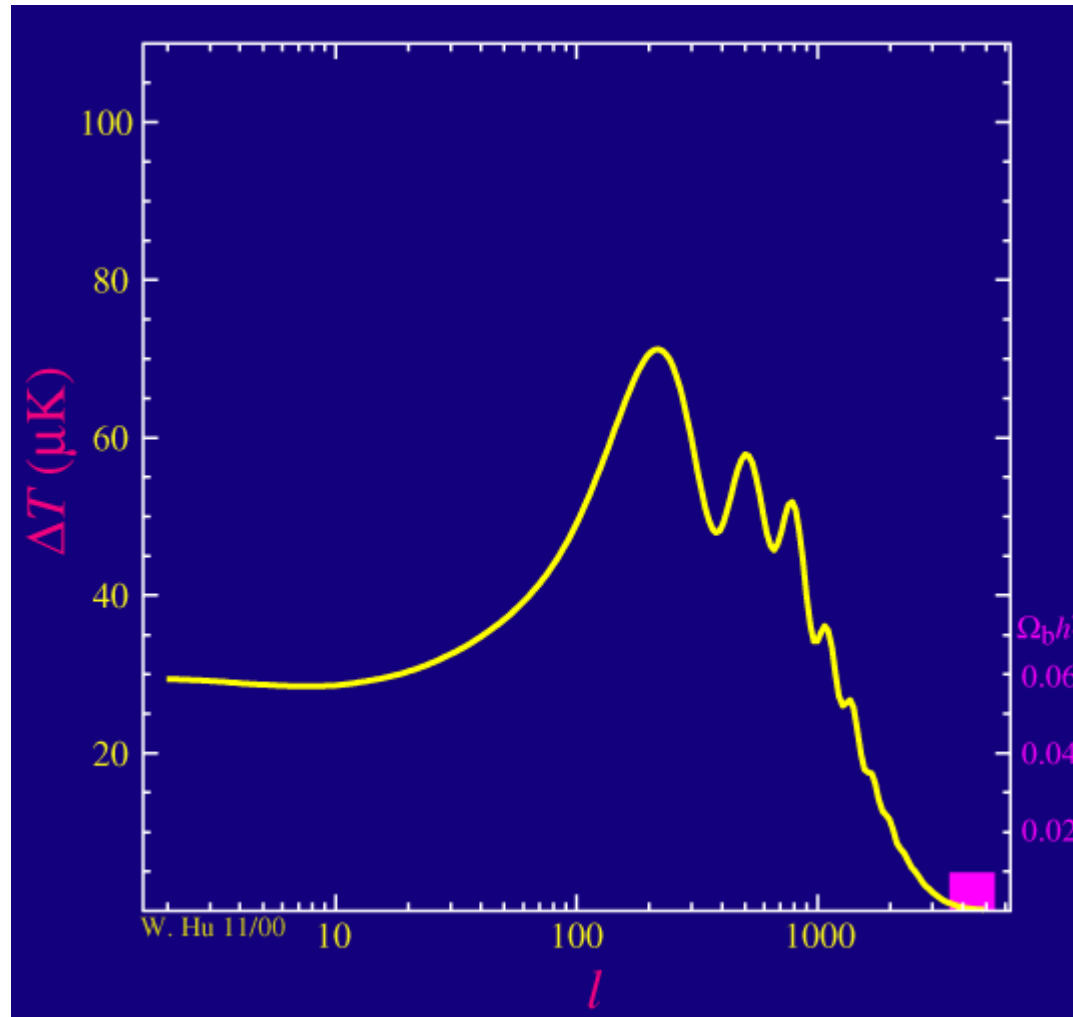


(b) Photons + Baryons: $c_s < c/\sqrt{3}$



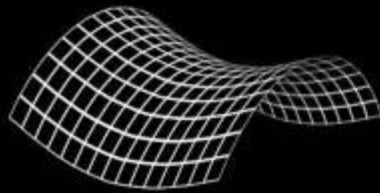
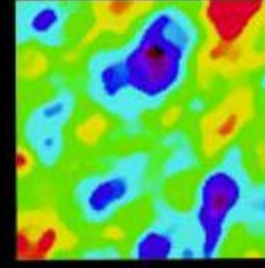
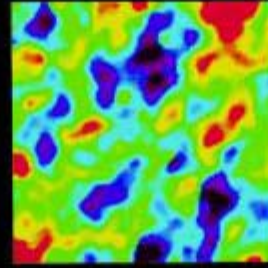
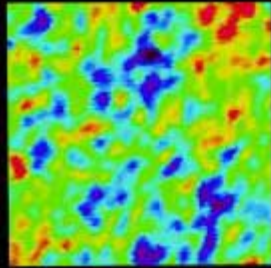
When the sound speed is lower

Was wäre wenn ...

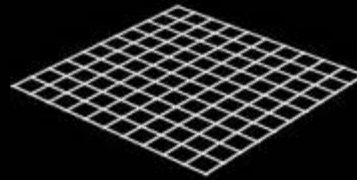


Raumkrümmung

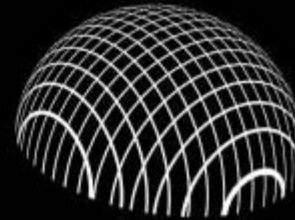
GEOMETRY OF THE UNIVERSE



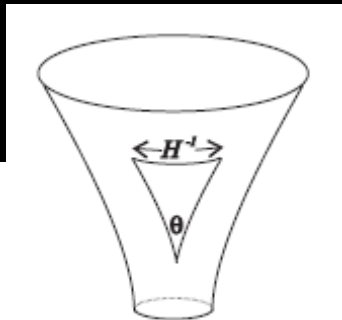
OPEN



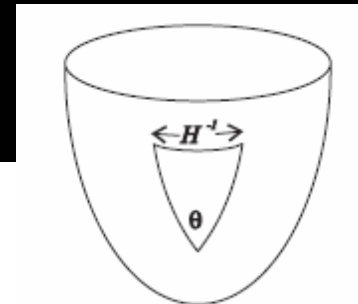
FLAT



CLOSED



$$\Omega_0 < 1$$



$$\Omega_0 > 1$$

Fitte deinen Kosmos

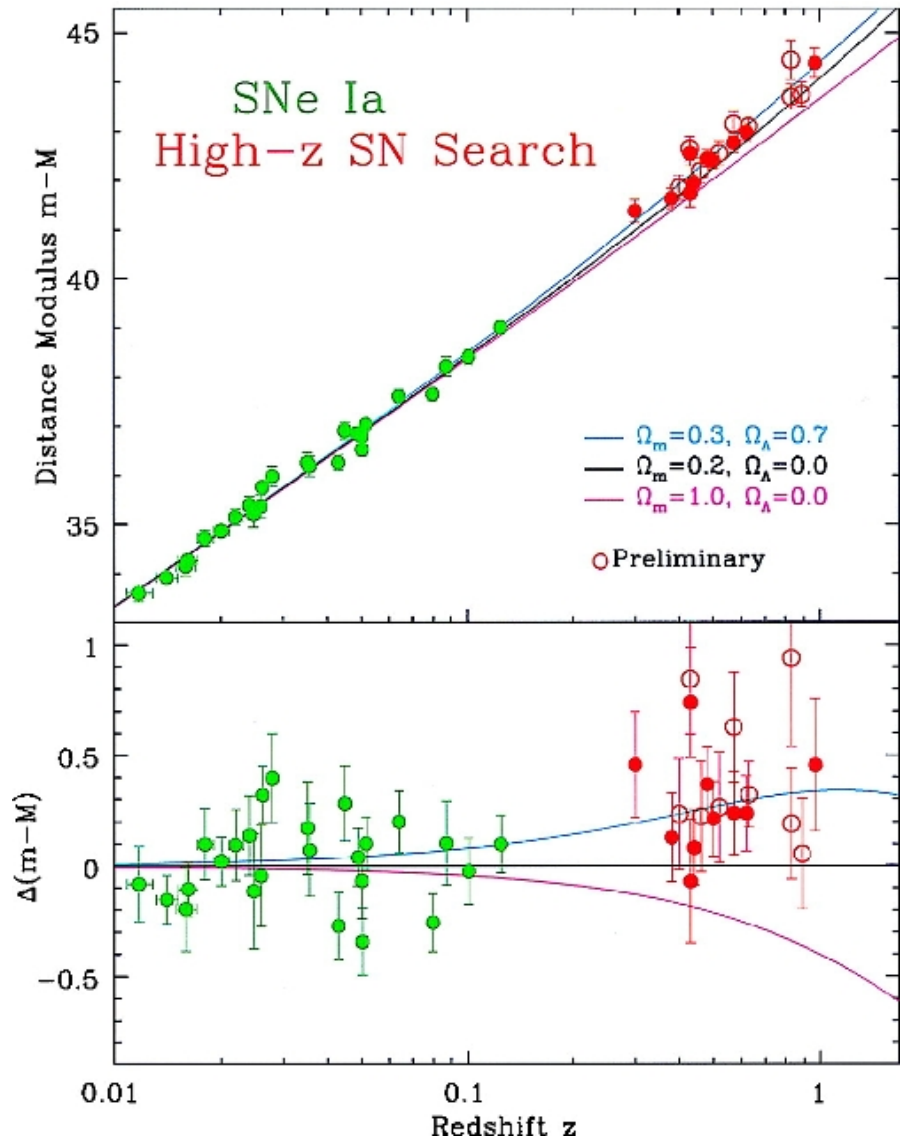
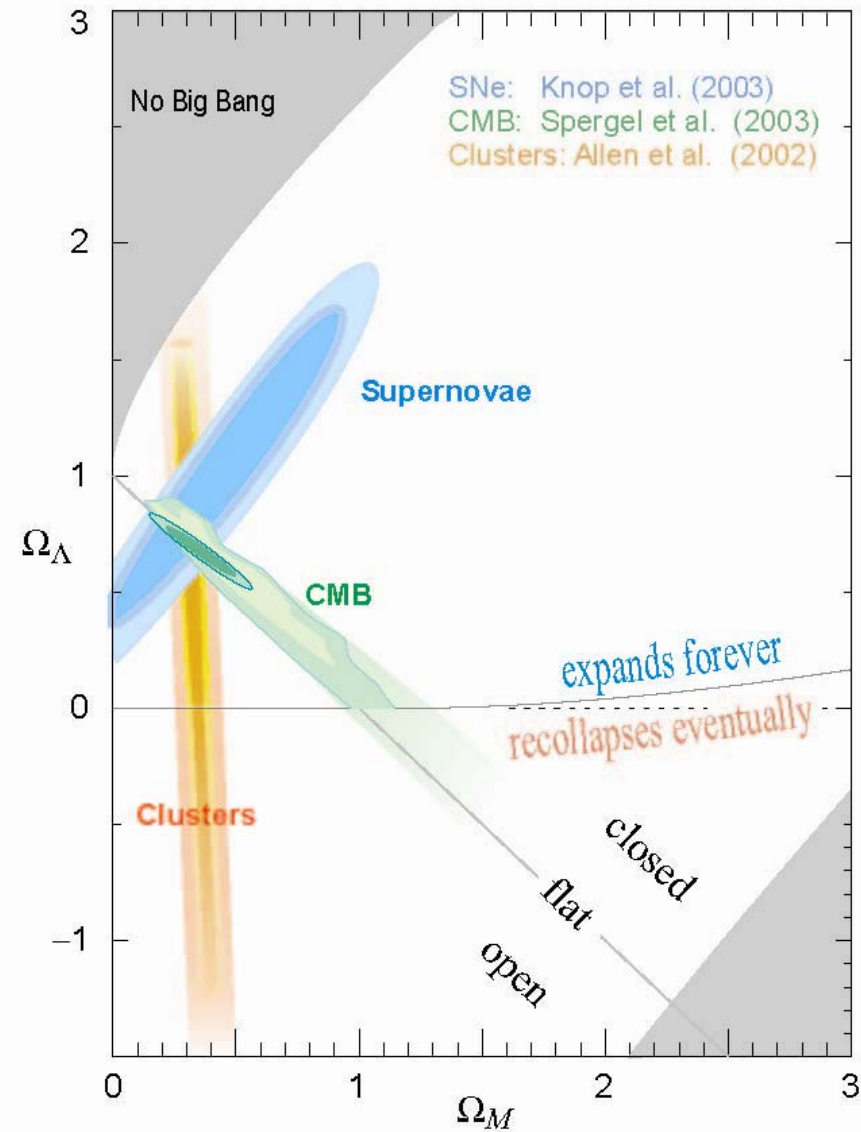
http://wmap.gsfc.nasa.gov/resources/camb_tool/cmb_plot.swf

Kosmologische Parameter

Sensitivität des CMB-Multipolspektrums

Parameter	Symbol	Value
Hubble parameter	h	0.73 ± 0.03
Total matter density	Ω_m	$\Omega_m h^2 = 0.128 \pm 0.008$
Baryon density	Ω_b	$\Omega_b h^2 = 0.0223 \pm 0.0007$
Cosmological constant	Ω_Λ	See Ref. 2
Radiation density	Ω_r	$\Omega_r h^2 = 2.47 \times 10^{-5}$
Neutrino density	Ω_ν	See Sec. 21.1.2
Density perturbation amplitude	σ_8	0.76 ± 0.05
Density perturbation spectral index	n	$n = 0.958 \pm 0.016$
Tensor to scalar ratio	r	$r < 0.65$ (95% conf)
Ionization optical depth	τ	$\tau = 0.089 \pm 0.030$
Bias parameter	b	See Sec. 21.3.4

Kosmologische Konstante



Was wir gelernt haben

- The Universe recombined at $z \simeq 1100$ and started to become ionized again at $z \simeq 10$.
- The geometry of the Universe is close to flat.
- Both Dark Matter and Dark Energy are required.
- Gravitational instability is sufficient to grow all of the observed large structures in the Universe.
- Topological defects were not important for structure formation.
- There are ‘synchronized’ super-Hubble modes generated in the early Universe.
- The initial perturbations were adiabatic in nature.
- The perturbations had close to Gaussian (*i.e.*, maximally random) initial conditions.