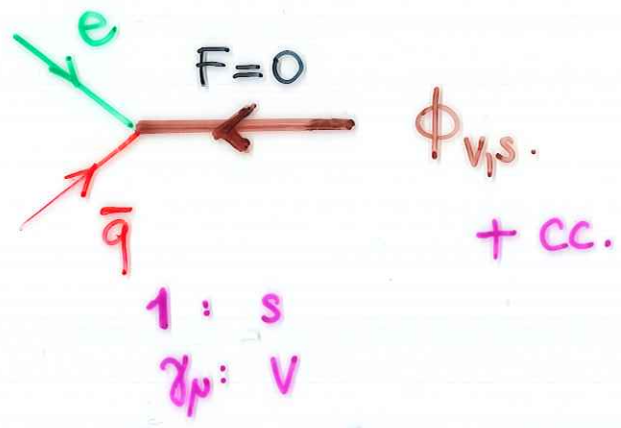
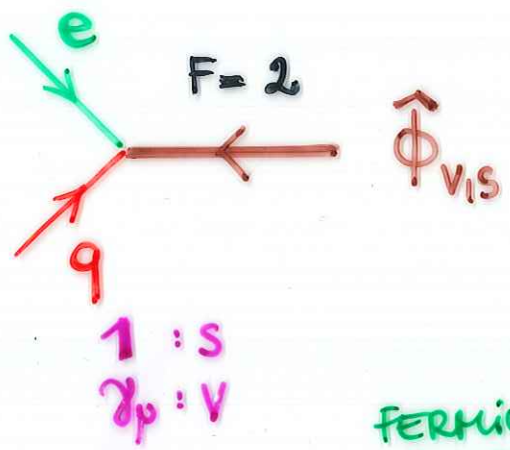
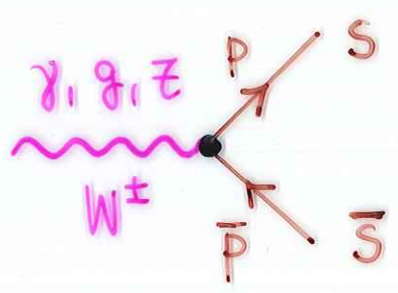


# LEPTOQUARKS

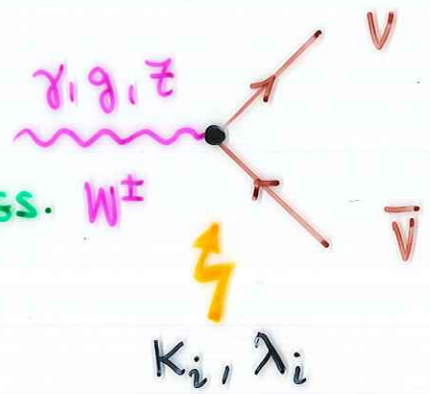


FERMIONIC COUPLINGS

BUCHMÜLLER, RÜCKL, WYLER 1987

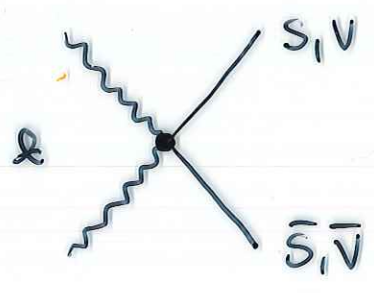


BOSONIC (GAUGE) COUPLINGS.



POMAROL et al. 1993 k

JB, E. BOOS, A. KRYUKOV  $\geq 1994$  i, k, lambda



OFTEN CONSIDERED: - B & L CONSERVING COUPLINGS

- FAMILY DIAGONAL

-  $SU_{2L} \times U_{1Y} \times SU_{3C}$  INVARIANT

- DIMENSIONLESS COUPLINGS

$\phi_{V1S}$  EITHER  $3_c$  OR  $\bar{3}_c$

# EXCLUDED MASS RANGES

→ NEXT TALK

CURRENTLY

- BEST LIMITS: TEVATRON

1<sup>ST</sup> GENERATION LQ'S:

DO S:  $M > 175, 147, 71 \text{ GeV}$  95% CL.

Br(eq): 1, 0.5, 0

$\mu \equiv \sqrt{s}$ , ! (BORN)

V: LARGER BOUNDS, DEPENDING ON  $K_E, \lambda_e$ .

CDF or DO:

2<sup>nd</sup> GEN. S:  $M < 141 \text{ GeV}$  95% CL

3<sup>rd</sup> GEN. S:  $M < 99 \text{ GeV}$  --

V:  $M < 170 \text{ GeV}$  (MC case only!)

INTERPRETING THE HIGH  $Q^2$   
EXCESS @ HERA AS  $\sigma(S, \nu \rightarrow eq)$

$$\Gamma_s = \frac{\lambda_s^2}{16\pi} M_s, \quad \Gamma_\nu = \frac{\lambda_\nu^2}{24\pi} M_\nu$$

$\Gamma \ll M$

WUDKA  
BWR  
DOBADO et al } '87

$\sigma(eq) = \frac{\pi^2}{s} \alpha \left(\frac{\lambda}{e}\right)^2 q(x = \frac{M^2}{s}, \langle Q^2 \rangle) J(\phi) b(\phi)$

$$J(\phi) = \begin{cases} 1: S \\ 2: \nu \end{cases} \quad b(\phi) = \text{Br}(\phi_{\nu, S} \rightarrow eq)$$

$$\sigma(eq) = 338 \text{ pb } b(\phi) \left(\frac{\lambda}{e}\right)^2 \begin{cases} \nu: 2 \\ S: 1 \end{cases} \begin{cases} u: x \quad 0.56 \dots 0.25 \\ \bar{u}: x \quad 0.005 \dots 0.001 \\ d: x \quad 0.15 \dots 0.05 \\ \bar{d}: x \quad 0.014 \dots 0.003 \end{cases}$$

$x: 0.4 \dots 0.5$   
 $\langle Q^2 \rangle \sim 20000 \text{ GeV}^2$

$$\mathcal{L}_{H1} = 14 \text{ pb}^{-1}, \quad \mathcal{L}_{ZEUS} = 20 \text{ pb}^{-1}, \quad \epsilon = 0.8$$

H1:	$\frac{\lambda_s}{e\sqrt{6}}$	: 0.06 ... 0.09	0.61 ... 1.36	0.11 ... 0.19	0.36 ... 0.79 (BORN)
		$u$	$\bar{u}$	$d$	$\bar{d}$
7# NC		↑	#4 NC	↑	
		$\lambda_\nu = \lambda_s / \sqrt{2}$	$\lambda_{ZEUS} = 0.55 \lambda_{H1}$		

# SU<sub>2L</sub> × U<sub>1Y</sub> QUANTUM NUMBERS

F = 0.

$e^+ u \rightarrow Q_{em} = \frac{5}{3}$

		lq	νq
S:	$R_2^+$	$\lambda_L$	0
V:	$\tilde{u}_{1p}$	$\lambda_R$	0
	$u_{3p}^+$	$\sqrt{2} \lambda_L$	0

$Br(\phi_{S,V} \rightarrow e^+ q) = 1$   
BORN

$e^+ d \rightarrow Q_{em} = \frac{2}{3}$

S:	$R_2^-$	$-\lambda_R$	$\lambda_L$	Br(e <sup>+</sup> q)=1
	$\tilde{R}_2^+$	$\lambda_L$	0	"
V:	$u_{1p}$	$\lambda_L, \lambda_R$	$\lambda_L$	
	$u_{3p}^0$	$-\lambda_L$	$\lambda_L$	

$\pi^0$ -decay: BUCHMÜLLER, WYER 1986 :  $R_2^- : \lambda_L \lambda_R \ll 1$

$u_{3p}^0 : Br(e^+ q) = \frac{1}{2}$

$u_{1p} : Br(e^+ q) \geq \frac{1}{2}$



LOW ENERGY BOUNDS ON THE FERMIONIC COUPLINGS

$$\lambda = \lambda_L, \lambda_R$$

1<sup>ST</sup> GENERATION:

$$S: \frac{\lambda}{e} \lesssim 0.4 \frac{M}{200 \text{ GeV}}$$

$$V: \frac{\lambda}{e} \lesssim 0.2 \frac{M}{200 \text{ GeV}}$$

BUCHMÜLLER, WYLER '86

DAVIDSON et al. '94

LEURER '94

$S_0, \tilde{S}_0, \tilde{S}_{1/2}$

$V_1, V_{1/2}$

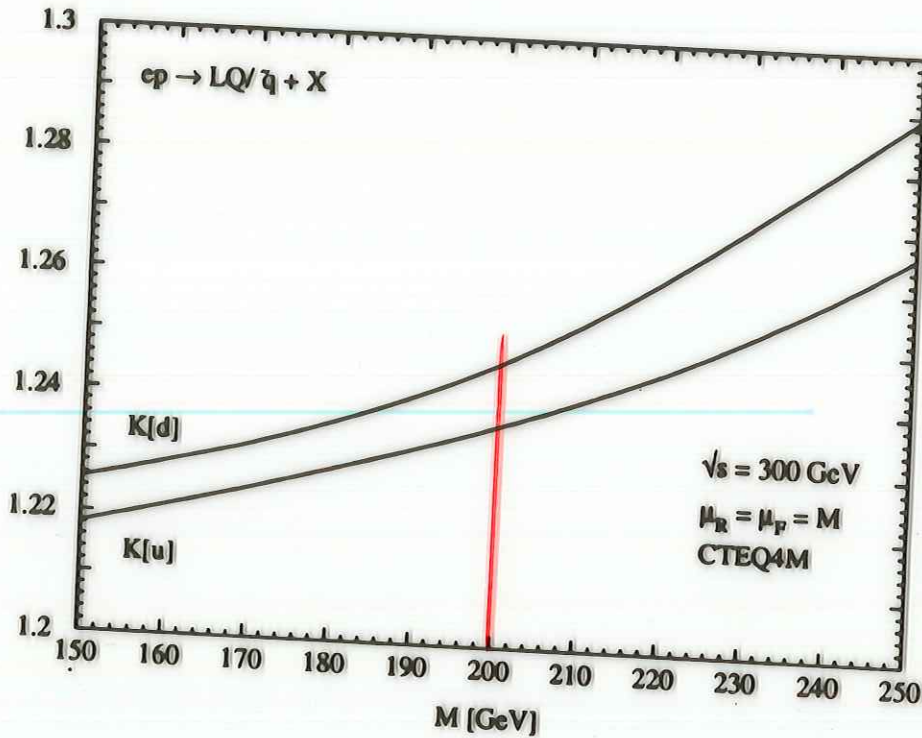
( $e \sim 0.3$ )

SOMETIMES  $\lambda_L \gg \lambda_R$  or  $\lambda_R \gg \lambda_L$  REQUESTED

- MESON DECAYS, MESON-ANTIMESON MIXING, LEPTON DECAYS etc.

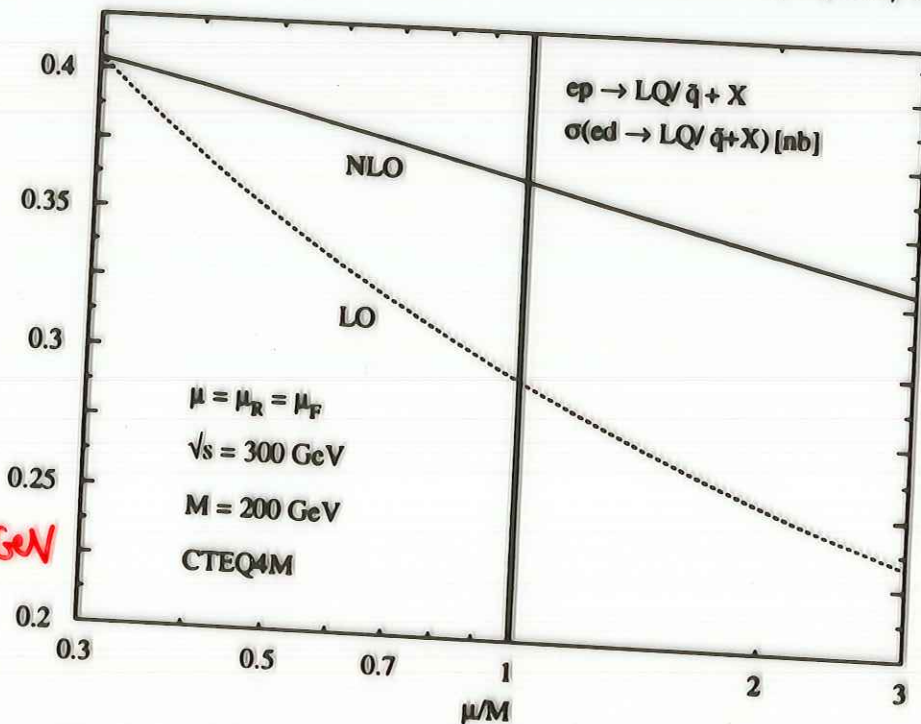
$O(\alpha_s)$  K-FACTOR

KUNSET STIRLING, '97



PLEHN et al. '97  
( $\Gamma \ll M$ )

Figure 2:  $K$ -factors for  $ed, eu \rightarrow LQ/\bar{q}$  as a function of the leptoquark/squark mass.



i.e.  
 $\frac{\lambda}{e}$  IS EVEN  
SMALLER  
THAN ESTI-  
MATED @  
BORN LEVEL.

$\sqrt{K^2} \sim 3 \dots 4 \text{ GeV}$

Figure 3: Comparison of the renormalization and factorization scale dependence in LO and NLO for the cross section for  $\sigma(e + d \rightarrow LQ/\bar{q})$ .

$\langle y \rangle$  :

BUCHMÜLLER, RÜCKL,  
WYLER '87.

S : const.

V :  $\propto (1-y)^2$

$\therefore$  H1 :  $\langle y \rangle = 0.59 \pm 0.02$

$y \in [0.4, 0.9]$

S :  $\langle y \rangle_S = 0.65$

V :  $\langle y \rangle_V = 0.55$  ;  $\langle y \rangle_{dis}^{ep} = 0.54$  !

JB '97

HOW CAN HERA FIND OUT WHETHER THE  
EVENTS WERE DUE TO LEPTOQUARKS ?

→ HIGHER  $\mathcal{L}$

LOOK FOR :

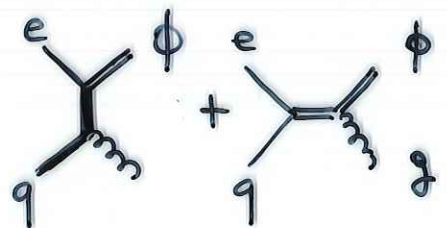
$e q \rightarrow \phi q$

$e q \rightarrow \phi q$

BY FAR  
DOMINANT.

e.g.  
 $p_{\perp} > 5 \text{ GeV} : M(e \text{ jet}) \sim '200 \text{ GeV}'$

+ 1 jet

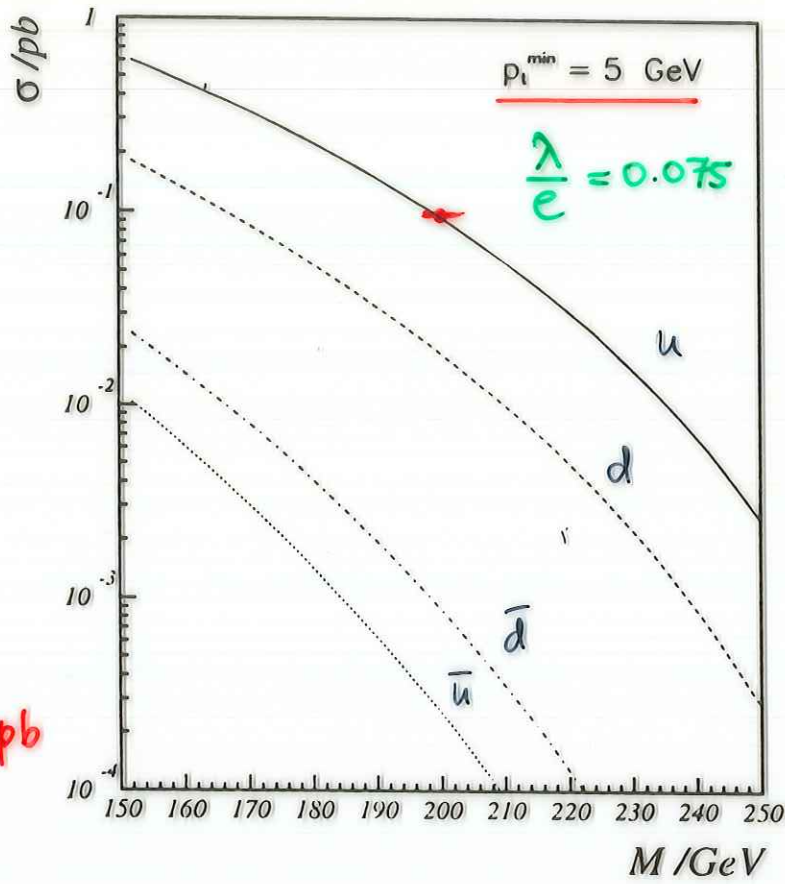


TEST OF LQ PROPAGATION !

JB, A. KRYUKOV,

DESY 97-067

$\sigma(eq \rightarrow sg) \sim 0.09 \text{ pb}$   
 $q=u$

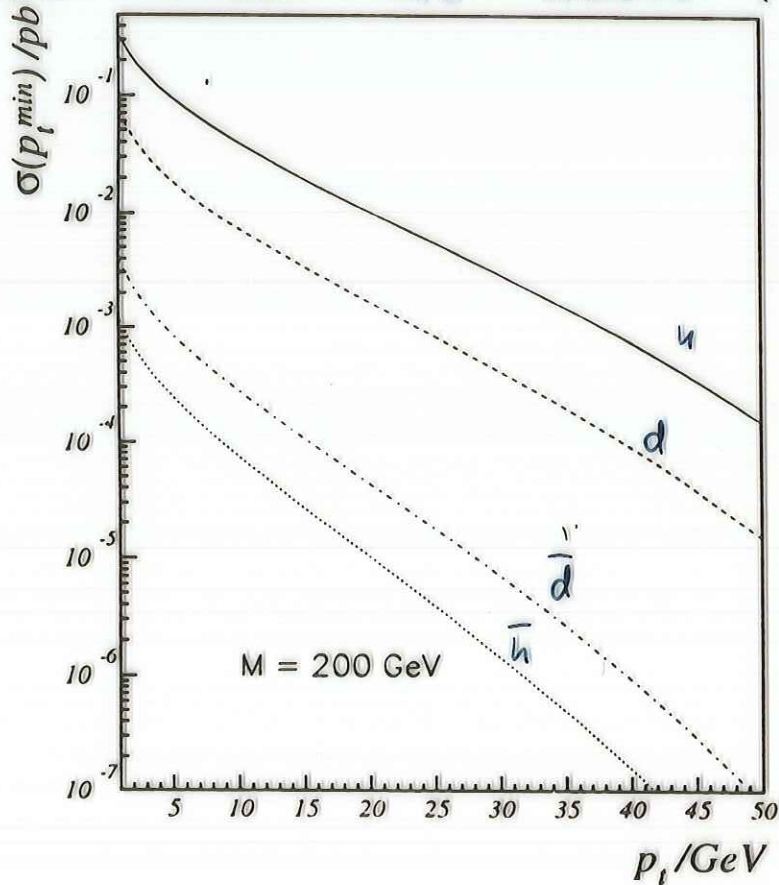


JB, A. KRYUKOV  
 DESY 97-067.

Eq  
 DOBADO et al.  
 '87

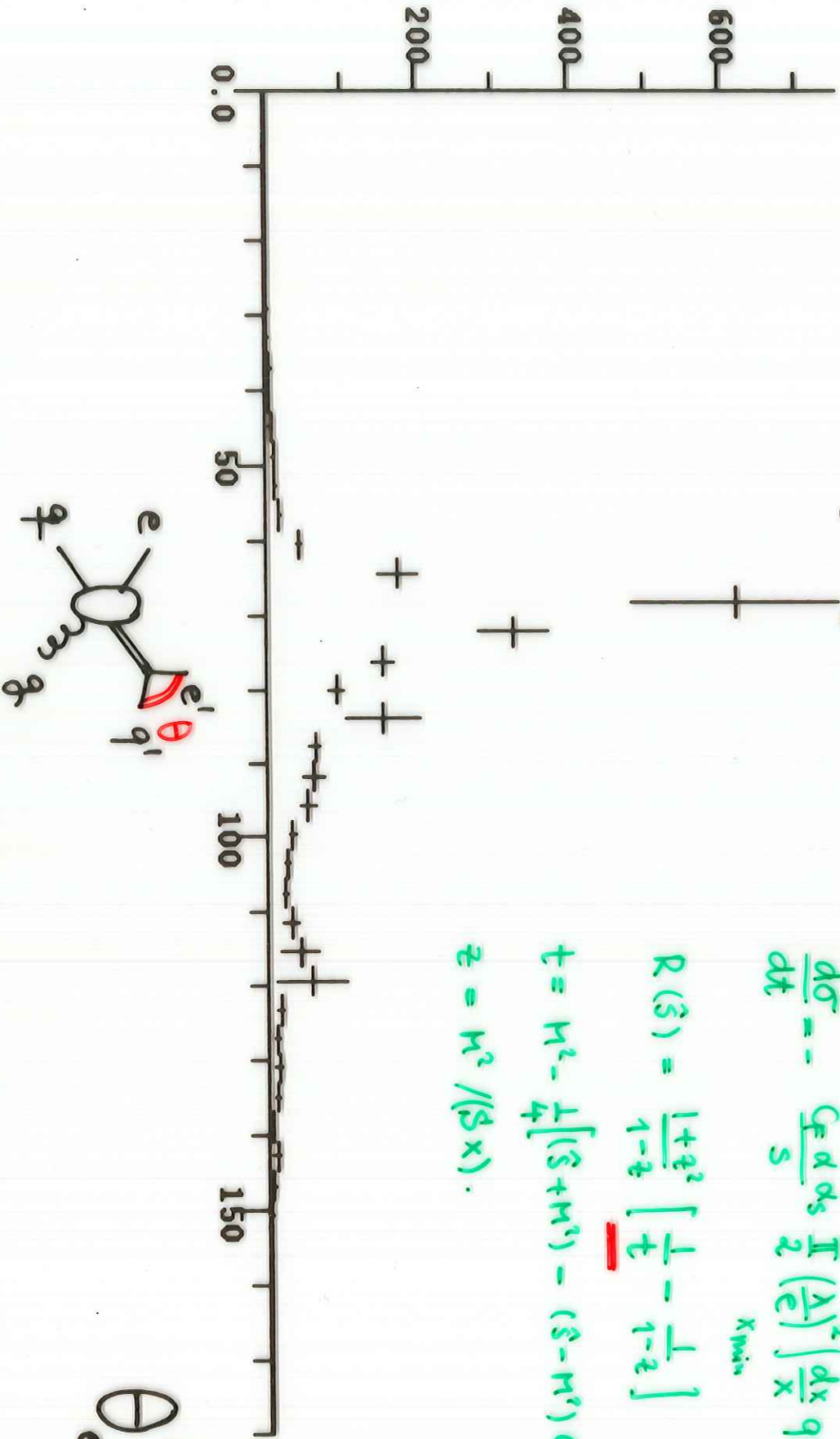
CTEQ3 LO  
 $\mu = M$

THE ABOVE CURVES FOR  $d, \bar{d}, \bar{u}$  SCALE UP FOR CORRESPONDINGLY LARGER  $\lambda/e$  - VALUES (cf. ABOVE).





arb. units



$$\frac{d\sigma}{dt} = - \frac{C e^2 \alpha_s}{s} \int_{x_{min}}^1 \frac{(\lambda)^2}{2} \left( \frac{e}{e'} \right)^2 \left| \frac{dx}{x} q(x) \right| R(\hat{s})$$

$$R(\hat{s}) = \frac{1+q^2}{1-q^2} \left[ \frac{1}{t} - \frac{1}{1-q^2} \right]$$

$$t = M^2 - \frac{1}{4} [(\hat{s} + M^2) - (\hat{s} - M^2) \cos \theta^*]$$

$$z = M^2 / (\hat{s} x)$$

$\Theta_{e'q'}^{LRB} / dq'$

$$\lambda = 0, \kappa \neq 0$$

POMAROL et al. '93

$$\lambda, \kappa \neq 0$$

JB, BOOS, KRYUKOV '96.

$\lambda = 0$  DOES NOT YIELD THE SMALLEST CROSS SECT.!

•  $\min_{\kappa, \lambda} \sigma_{q\bar{q}}$  DOES NOT CONTAIN  $\left(\frac{s}{M^2}\right)^\alpha$  TERMS ANYMORE!

JB, BOOS, KRYUKOV '96A.

⚡ RELEVANT FOR TEVATRON!

$$\sigma_{S\bar{S}} (\mu = M = 200 \text{ GeV}) \sim 0.16 \text{ pb}$$

$$\min_{\kappa, \lambda} \sigma_{V\bar{V}} (\mu = M = 200 \text{ GeV}) \sim 0.3 \text{ pb}$$

$$(\sigma_{HC} (\kappa = 1, \lambda = 0) \sim 0.4 \text{ pb}).$$

JB, E. BOOS, A. KRIVUKOV

Oct. 1996

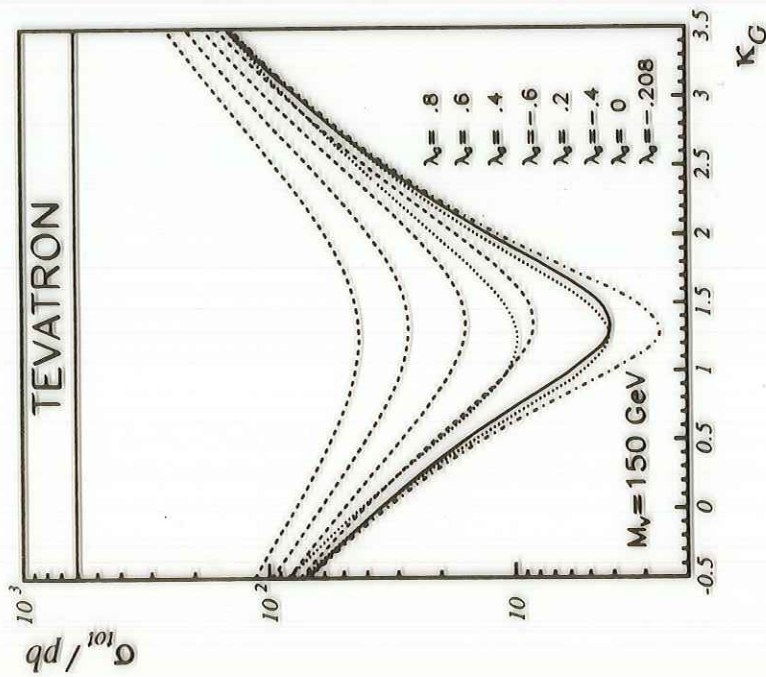


Figure 6a: Dependence of the integrated cross sections for vector leptoquark pair production on the anomalous couplings  $\kappa_G$  and  $\lambda_G$  at the TEVATRON,  $\sqrt{S} = 1.8$  TeV for  $M_V = 150$  GeV. The order of the values of  $\lambda_G$  follows the position of the respective minimum. Dashed lines:  $\lambda_G > 0$ , dotted lines:  $\lambda_G < 0$ , full line:  $\lambda_G = 0$ , dash-dotted line:  $\lambda_G = -0.208$ .

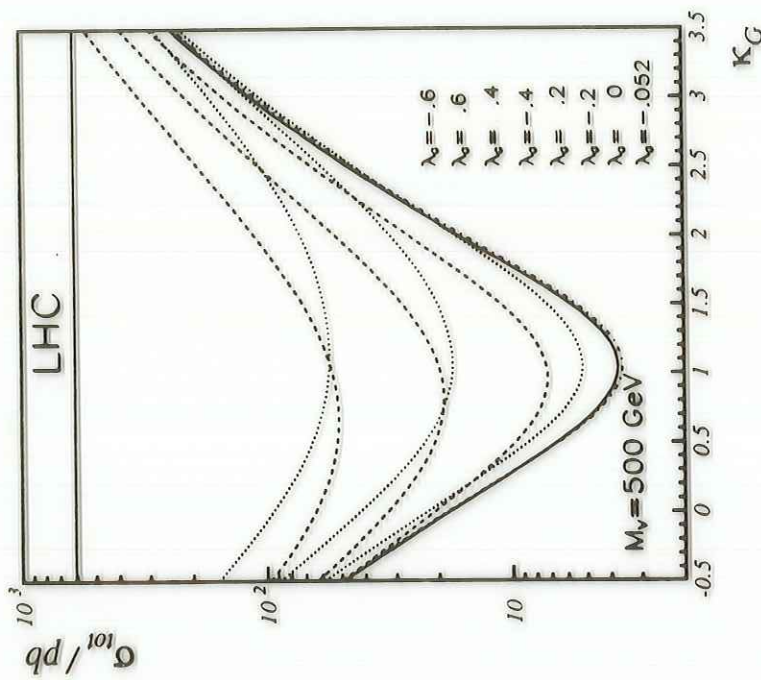


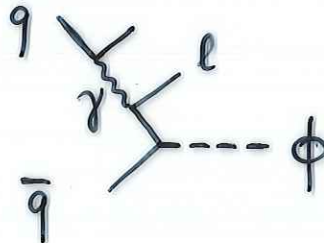
Figure 6b: Dependence of the integrated cross sections for vector leptoquark pair production on the anomalous couplings  $\kappa_G$  and  $\lambda_G$  at LHC,  $\sqrt{S} = 14$  TeV for  $M_V = 500$  GeV. The dash-dotted line corresponds to  $\lambda_G = -0.052$ . The other parameters are the same as in figure 6a.

# P $\bar{P}$ PRODUCTION

## 1) SINGLE PRODUCTION



HEWETT, PAKVASA '89  
(MANY OTHERS LATER  
4. JB '97)  
 $\sigma \propto \lambda^2 \ll 1$ .



OHNEMUS et al. '94  
REYA (prio. comm.)

$\sigma \approx 0.7 \dots 1.3 \text{ fb}$

$\sigma \sim 0.4 \text{ fb}, M \sim 200 \text{ GeV}$

$\therefore \frac{\lambda}{e} \sqrt{b} = 0.075$ .

## 2) PAIR PRODUCTION

$\frac{\lambda}{e} \ll 1$  : DECOUPLING OF FERMIONIC VERTICES

→  $g_s$  KNOWN COUPLING

COMPLETE PREDICTION FOR SCALARS

→ VECTOR LEPTO QUARKS ARE NOT NECESSARILY COUPLING YANG-MILLS LIKE TO GLUONS

$K_G, \lambda_G$  - ANOMALOUS COUPLINGS

$\exists \min_{K_G, \lambda_G} \sigma_{V\bar{V}} > 0$ . JB, BOOS, KEVUKOV '96.

IN THIS SENSE: MODEL 'INDEPENDENT' LIMIT.



## SCALARS :

$$\sigma_{\overline{SS}}^{9\overline{9}} = \frac{2\pi \alpha_s^2}{27 \hat{s}} \beta^3$$

$$\sigma_{\overline{SS}}^{88} = \frac{\pi \alpha_s^2}{96 \hat{s}} \left\{ \beta (41 - 31\beta^2) - (17 - 18\beta^2 + \beta^4) L(\beta) \right\}$$

## ∴ SUSY: SQUARKS

CORRECT IN:

GRIFOLS, MENDEZ '82

ANTONIADIS et al. '84

EHLQ '84

ALTARELLI, RÜCKL '84

DAWSON, EICHEN, QUIGG '85

JB, KRYUKOV, BOOS '96

HARRISON, LLEWELLYN  
SMITH '83 (E!)

## VECTORS :

$$\sigma_{\overline{V\overline{V}}}^{9\overline{9}} = \frac{4\pi \alpha_s^2}{9M_V^2} \sum_{i=0}^5 \chi_i^9(k, \lambda) \tilde{G}_i(\hat{s}, \beta)$$

$$\sigma_{\overline{V\overline{V}}}^{88} = \frac{\pi \alpha_s^2}{96M_V^2} \sum_{i=0}^{14} \chi_i^8(k, \lambda) \tilde{F}_i(s, \beta)$$

$\lambda = k = 0$  :

(Y-M-type)

$$\sigma_{\overline{V\overline{V}}}^{9\overline{9}} = \frac{4\pi \alpha_s^2}{9M_V^2} \left[ \frac{1}{24} \frac{\hat{s}}{M_V^2} + \frac{23 - 3\beta^2}{24} \right]$$

$$\sigma_{\overline{V\overline{V}}}^{88} = \frac{\pi \alpha_s^2}{96M_V^2} [\beta A - L(\beta) \cdot B]$$

$$A = \frac{523}{4} - 90\beta^2 + \frac{93}{4}\beta^4$$

$$B = \frac{3}{4} (65 - 83\beta^2 + 19\beta^4 - \beta^6).$$

ARNOLD, WENDT '86.

BORISOV et al '87.

JB, BOOS, KRYUKOV '96

## B Coefficients of the production cross section of vector leptoquarks

The functions  $F_i(\beta, \cos \theta)$  which determine the differential pair production cross section for  $gg \rightarrow VV$  are:

$$F_0 = [10 - 6\beta^2 + 6\beta^4 + (16 - 6\beta^2)\beta^2 \cos^2 \theta + 3\beta^4 \cos^4 \theta] \cdot (7 + 9\beta^2 \cos^2 \theta) \quad (85)$$

$$F_1 = -4 \cdot (77 + 143\beta^2 \cos^2 \theta + 36\beta^4 \cos^4 \theta) \quad (86)$$

$$F_2 = -8 \cdot (7 + 11\beta^2 \cos^2 \theta - 18\beta^4 \cos^4 \theta) \quad (87)$$

$$F_3 = 2 \cdot (117 + 165\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) + 2 \frac{\beta^2}{M_Q^2} (8 - \beta^2 \cos^2 \theta - 7\beta^4 \cos^4 \theta) + \frac{7}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 \quad (88)$$

$$F_4 = -4 \cdot (19 + 27\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) + 10 \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (7 - \beta^2 \cos^2 \theta) \quad (89)$$

$$F_5 = 2 \cdot (19 + 27\beta^2 \cos^2 \theta + 18\beta^4 \cos^4 \theta) - \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (65 + 29\beta^2 \cos^2 \theta) \quad (90)$$

$$F_6 = \frac{1}{8} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (97 + 2\beta^2 \cos^2 \theta - 115\beta^4 \cos^4 \theta) + \frac{\beta^2}{M_Q^2} \frac{9}{4} (1 - \beta^2 \cos^2 \theta)^2 \quad (90)$$

$$F_7 = -81 - 87\beta^2 \cos^2 \theta - \frac{1}{2} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (39 + 14\beta^2 \cos^2 \theta) - \frac{7}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 \quad (91)$$

$$F_8 = 127 + 129\beta^2 \cos^2 \theta - \frac{1}{2} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (99 + 3\beta^2 \cos^2 \theta) \quad (92)$$

$$+ \frac{1}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (-23 + 18\beta^2 \cos^2 \theta)$$

$$F_9 = -71 - 57\beta^2 \cos^2 \theta + \frac{1}{2} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (170 + 21\beta^2 \cos^2 \theta) \quad (93)$$

$$+ \frac{1}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (-59 + 40\beta^2 \cos^2 \theta + 27\beta^4 \cos^4 \theta) - \frac{9}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 \quad (93)$$

$$F_{10} = 5(1 - \beta^2 \cos^2 \theta) - \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (21 + 2\beta^2 \cos^2 \theta) \quad (94)$$

$$+ \frac{1}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (74 + 9\beta^2 \cos^2 \theta)$$

$$+ \frac{1}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (-15 + 8\beta^2 \cos^2 \theta)$$

$$F_{11} = 3 + 5\beta^2 \cos^2 \theta + \frac{5}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (4 - \beta^2 \cos^2 \theta) \quad (95)$$

$$+ \frac{1}{32} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (25 + 13\beta^2 \cos^2 \theta)$$

$$F_{11} = -4 \cdot (3 + 5\beta^2 \cos^2 \theta) - 5 \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 + \frac{1}{8} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (35 - 13\beta^2 \cos^2 \theta) \quad (96)$$

$$F_{12} = 6 \cdot (3 + 5\beta^2 \cos^2 \theta) - \frac{15}{2} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (2 + \beta^2 \cos^2 \theta) \quad (97)$$

$$+ \frac{1}{16} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (-23 + 54\beta^2 \cos^2 \theta - 39\beta^4 \cos^4 \theta)$$

$$+ \frac{1}{64} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (119 - 49\beta^2 \cos^2 \theta)$$

$$F_{13} = -4 \cdot (3 + 5\beta^2 \cos^2 \theta) + 5 \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (5 + \beta^2 \cos^2 \theta) - \frac{1}{8} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (119 + 13\beta^2 \cos^2 \theta) \quad (98)$$

$$+ \frac{1}{32} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (79 - 15\beta^2 \cos^2 \theta)$$

$$F_{14} = 3 + 5\beta^2 \cos^2 \theta - \frac{5}{4} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (8 + \beta^2 \cos^2 \theta) + \frac{1}{32} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta) (321 - 324\beta^2 \cos^2 \theta - 13\beta^4 \cos^4 \theta) \quad (99)$$

$$+ \frac{11}{64} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (-23 + 7\beta^2 \cos^2 \theta)$$

$$+ \frac{1}{256} \frac{\beta^2}{M_Q^2} (1 - \beta^2 \cos^2 \theta)^2 (135 - 22\beta^2 \cos^2 \theta + 15\beta^4 \cos^4 \theta).$$

The coefficients  $\bar{F}_i(\beta)$  for the integrated cross section for  $gg \rightarrow VV$  are:

$$\bar{F}_0 = \beta \left( \frac{523}{4} - 90\beta^2 + \frac{93}{4}\beta^4 \right) - \frac{3}{4} (65 - 83\beta^2 + 19\beta^4 - \beta^6) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (100)$$

$$\bar{F}_1 = -4\beta(41 - 9\beta^2) - \frac{87}{2} (1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (101)$$

$$\bar{F}_2 = 36\beta(1 - \beta^2) - 25(1 - \beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (102)$$

$$\bar{F}_3 = \beta(75 - 9\beta^2) + \frac{7}{4}\beta \frac{\beta^2}{M_Q^2} - \frac{1}{4}(1 - 61\beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (103)$$

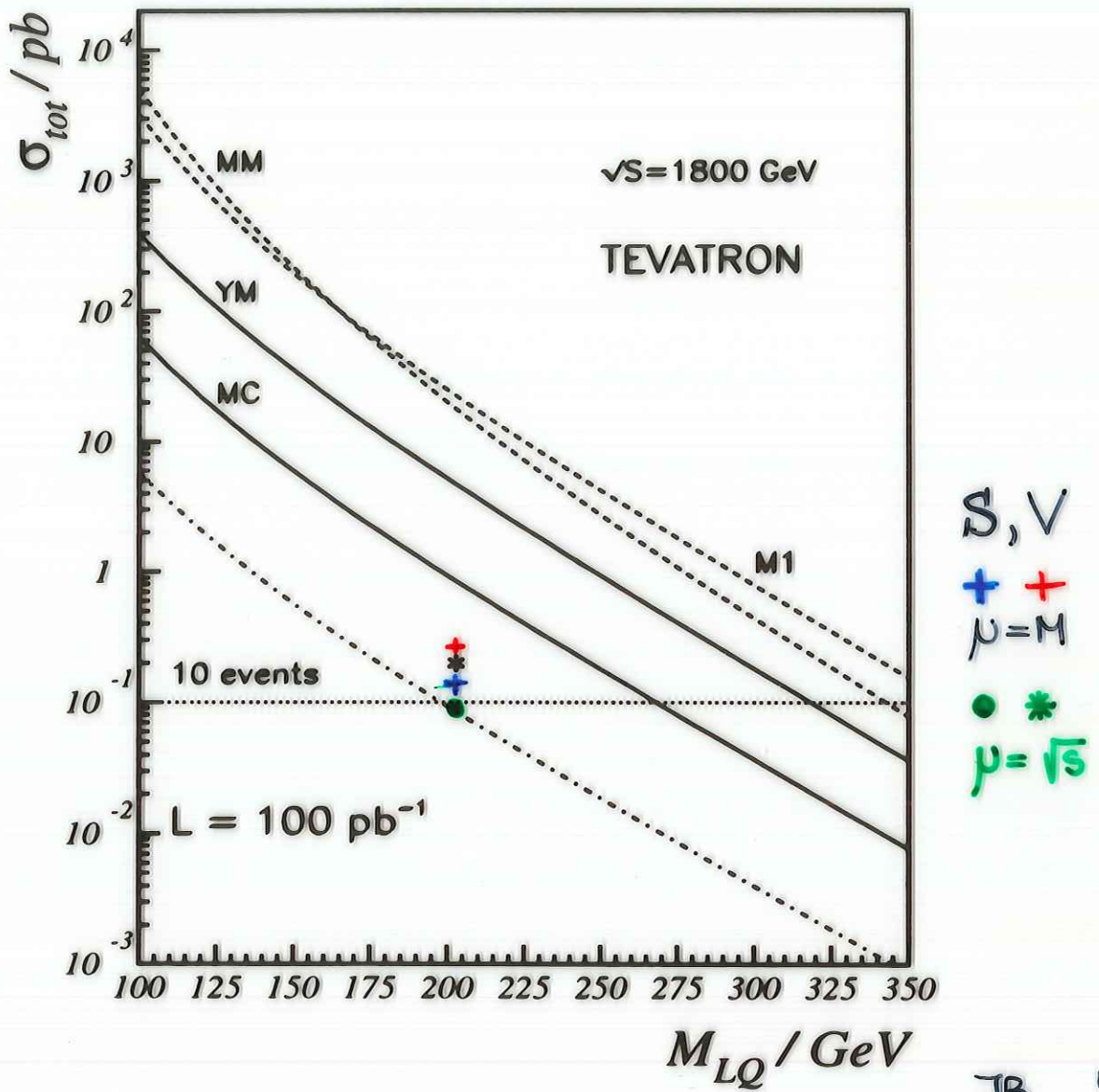
$$\bar{F}_4 = -2\beta(20 - 9\beta^2) + \frac{1}{2}(91 - 31\beta^2) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (104)$$

$$\bar{F}_5 = \beta \left( \frac{209}{6} - 9\beta^2 \right) + \frac{263}{12}\beta \frac{\beta^2}{M_Q^2} + \frac{3}{2}\beta \frac{\beta^2}{M_Q^2} - \left( \frac{219}{4} - \frac{31}{4}\beta^2 + \frac{\beta^2}{M_Q^2} \right) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (104)$$

$$\bar{F}_6 = -9\beta - \frac{7}{4}\beta \frac{\beta^2}{M_Q^2} - \left( \frac{103}{8} + \frac{3}{8}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (105)$$

$$\bar{F}_7 = \frac{55}{2}\beta - \frac{17}{4}\beta \frac{\beta^2}{M_Q^2} - \left( \frac{185}{8} - \frac{1}{8}\beta^2 \right) \log \left| \frac{1+\beta}{1-\beta} \right| \quad (106)$$





JB '97

Figure 1: Integrated cross sections for scalar vector leptiquark pair production at the TEVATRON,  $\sqrt{s} = 1.8 TeV$  choosing the renormalization and factorization scale by  $\mu = \sqrt{s}$ . Dash-dotted line : scalar leptiquarks; fill lines : YM : Yang-Mills type coupling  $\kappa_G = \lambda_G \equiv 0$ ; MC : minimal vector coupling  $\kappa_G = 1, \lambda_G = 0$ ; dashed lines : other choices for the anomalous couplings : MM :  $\kappa_G = \lambda_G = -1$ , M1 :  $\kappa_G = -1, \lambda_G = +1$ . The asterisk denotes the minimum of the pairproduction cross section for vector leptiquarks with respect to the anomalous couplings at  $M_V = 200 GeV$ .



Figure 1: Diagrams describing lepton-antilepton pair production via gluon-gluon fusion. Here the dashed lines denote both scalar and vector leptons.

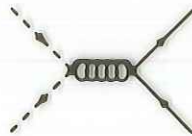


Figure 2: Diagram for the subprocess  $q\bar{q} \rightarrow \phi\bar{\phi}$ .